

Lecture 20: Subtyping & OO Languages

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Subtyping

- Can be added to non-OO languages
- Matching structures and signatures similar
 - but more restricted.
- Provides support for using values from new types in old (unexpected) contexts

Subtype Polymorphism

S is a *subtype* of T , written $S <: T$,

iff

a value of type S can be used in any context expecting a value of type T ,

i.e., S can masquerade as a T .

Subsumption: $e: S \ \& \ S <: T \Rightarrow e: T$.

Immutable Records

Records without field update (like Haskell/ML):

Sandwich = { bread: BreadType;
 filling: FoodType }

s: Sandwich = { bread = rye;
 filling = pastrami }

Only operation is extracting field:

... s.filling ...

Specializing Record Types

```
CheeseSandwich = {bread: BreadType;
                  filling: CheeseType;
                  sauce: SauceType}
```

```
c_s: CheeseSandwich = {bread = white;
                      filling = cheddar;
                      sauce = mustard}
```

Subtyping Immutable Records

If $r: \{l_i: T_i\}_{1 \leq i \leq k}$ then expect $r.l_i: T_i$.

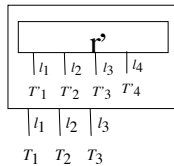
When is $\{l_i: T'_i\}_{1 \leq i \leq n} <: \{l_i: T_i\}_{1 \leq i \leq k}$?

Suppose $r': \{l_i: T'_i\}_{1 \leq i \leq n}$

When can r' *masquerade* as elt of $\{l_i: T_i\}_{1 \leq i \leq k}$?

Need $r'.l_i: T_i$.

Masquerading



$$\{l_i: T'_i\}_{1 \leq i \leq n} <: \{l_i: T_i\}_{1 \leq i \leq k}$$

iff

$k \leq n$ and for all $1 \leq i \leq k$, $T'_i <: T_i$.

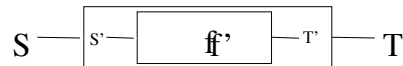
Functions

If $f: S \rightarrow T$ and $s: S$ then $f(s): T$

When is $S' \rightarrow T' <: S \rightarrow T$?

If $f': S' \rightarrow T'$, need $f'(s): T$.

Subtyping Functions



$$S' \rightarrow T' <: S \rightarrow T$$

iff

$$S <: S' \text{ and } T' <: T.$$

Contravariant for parameter types.
Covariant for result types.

Variables

Variables can be *suppliers* & *receivers* of values.

$$x := x + 1$$

If x is a variable of type T , write $x: \text{ref } T$.

When is $\text{ref } T' <: \text{ref } T$?

To replace variable $x: \text{ref } T$ by $x': \text{ref } T'$ in:

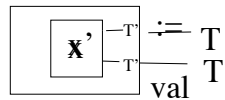
- expression: ... x ...

Need $T' <: T$

- assignment: $x := e$ where $e: T$.

Need $T <: T'$.

Variables



Supplier: covariant;

Receiver: contravariant

$$\text{ref } T' <: \text{ref } T \text{ iff } T' \approx T$$

Exercises

Updatable Records:

When is $\{l_i : T'_i\}_{1 \leq i \leq n} <: \{l_i : T_i\}_{1 \leq i \leq k}$?

... $r.l_i := e$...

More Exercises

Arrays:

- If $S <: T$, is Array of $S <:$ Array of T ?

Java says yes, but ...

not safe!

With few exceptions, for $F: \text{Types} \rightarrow \text{Types}$,

$S <: T \not\Rightarrow F(S) <: F(T)$.

Object-Oriented Languages

Roots in ADT Languages

- Ada and Modula-2 internal reps
 - couldn't be instantiated dynamically
 - no type or other method of organizing, despite similarity to records
 - provide better modules for building large systems
- Called object-based

Responding to the “SOFTWARE CRISIS!”

Qualities Desired in Software

- Correctness
- Robustness
- Extensibility *Almost all supported by ADT's*
- Reusability
- Compatibility

Object-Oriented Languages

- Objects that are data abstractions
- Objects have associated object type (classes or interfaces)
- Classes may *inherit* attributes from superclass
- Computations proceed by sending messages
- Subtype polymorphism
- Support dynamic method invocation

Programming Objects in ML

```
exception Empty;
fun newStack(x) =
  let
    val store = ref [x]
  in
    {push = fn y => store := y::(!store);
     pop = fn z => case !store of
                   nil => raise Empty
                   | (y::ys) => (store := ys; y)
    }
  end;

val myStack = newStack(0);
#push(myStack)(1);
#pop(myStack)();
```

Parameter z ignored, used to delay evaluation really parameterless function

Weakness of ML

- No subtyping
- No this/self
- No inheritance
- *Similar issues in trying to do objects in LISP or other functional languages.*
- *Haskell doesn't have state!*

OO Keywords

- Object
- Message
- Class
- Instance
- Method
- Subtype
- Subclass

Objects

- Internal data abstractions
- Hide representation
- Have associated state
- Methods have access to its state
- Self

Object Types

- Allow objects to be first class
- Allow use in assignment, parameters, components of structures
- Allow objects to be classified via subtyping