

Admin

- Final project comments: - Use pre-existing code - Get your data now!
 - Use pre-existing data sets
 - Finding good references Google scholar (<u>http://scholar.google.com/</u>) Other papers
- · Final project proposals due tomorrow at 6pm
- · Some written problems will be posted tomorrow

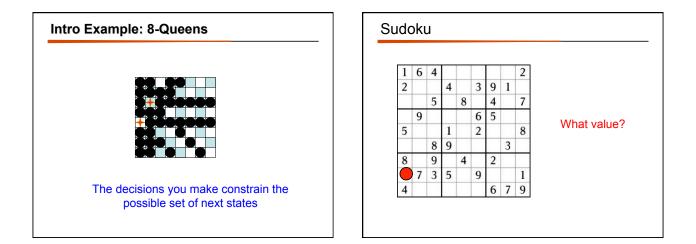
Quick search recap

- Search
 - uninformed
 - BFS, DFS, IDS - informed
 - A*, IDA*, greedy-search
- · Adversarial search
 - assume player makes the optimal move
 - minimax and alpha-beta pruning
- Local search (aka state space search)
 - start random, make small changes
 - dealing with local minima, plateaus, etc.
 - · random restart, randomization in the approach, simulated annealing, beam search, genetic algorithms

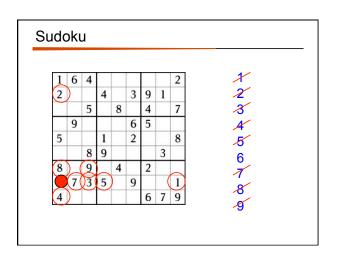
Intro Example: 8-Queens

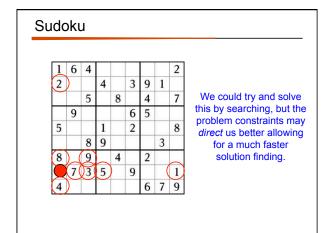
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Where should I put the queens in columns 3 and 4?



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		5		8		4		7	3	3	
	9				6	5			2		
5			1		2			8	5		
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	7	3	5		9			1	6		
4						6	7	9	ç		





Constraint satisfaction problem

Another form of search (more or less)!

- Set of **variables**: *x*₁, *x*₂, ..., *x*_n
- Domain for each variable indicating possible values: $D_{x1}, D_{x2}, ..., D_{xn}$
- Set of constraints: C₁, C₂, ..., C_m
 Each constraint limits the values the variables can take • $x_1 \neq x_2$
 - $x_1 < x_2$
 - $x_1 + x_2 = x_3$
 - $x_4 < x_5^2$

Goal: an assignment of values to the variables that satisfies all of the contraints

Applications?

Applications

Scheduling:

I'd like to try and meet this week, just to touch base and see how everything is going. I'm free: Me

Anytime Tue., Wednesday after 4pm, Thursday 1-4pm

- I can do Tuesday 11-2:30, 4+, Wednesday 5-6, Thursday 11-2:30 **S1**
- I can do anytime Tuesday (just before or after lunch is best), not Wednesday, or Thursday afternoon. P2
- I'm free Tuesday and Thursday from 2:45-4 or so, and also Wednesday any time after 3. **S**2
- **S**3 I can meet from 4-5 on Tuesday or Wednesday after 5.

Applications

Scheduling

CSSI MWILLING M
CS51: MW (1-12:15 CAN) T 146 11:15-4 40 CS55: TR 9:35 11:35 CAN) M MURP.
CS62: MWF 9 14 (30) W 1:15-2:30 2.
CS105: TR 2:45- 4 . W F lab: 11-12:15
CS131 : MWF 10 AM (1) 1:15-2:30
CS159: MW 1:15 213 (16)

Applications

Scheduling

- manufacturing
- Hubble telescope time usage
- Airlines
- Cryptography
- computer vision (image interpretation)
- ...

Why CSPs?

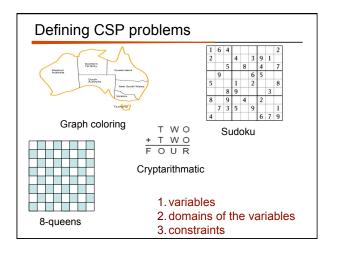
"Constraint programming represents one of the closest approaches computer science has yet made to the Holy Grail of programming: the user states the problem, the computer solves it." Eugene C. Freuder, Constraints, April 1997

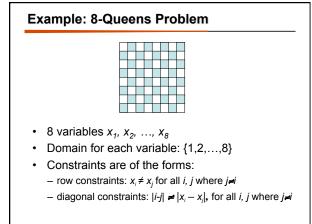
Why CSPs?

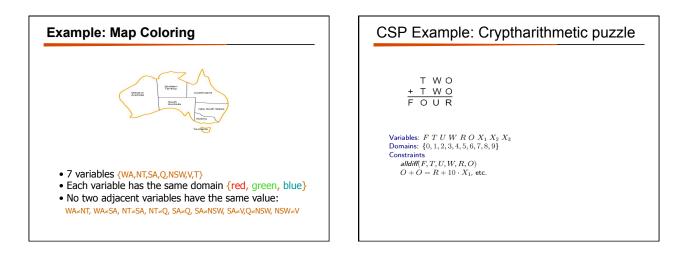
If you can represent it in this standard way (set of variables with a domain of values and constraints), the successor function and goal test can be written in a generic way that applies to **all** CSPs

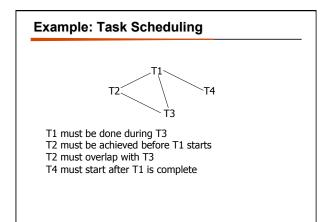
We can develop effective generic heuristics that require **no domain specific expertise**

The **structure** of the constraints can be used to simplify the solution process









Many different constraint types

Unary constraints: involve only a single variable (x₁ != green)

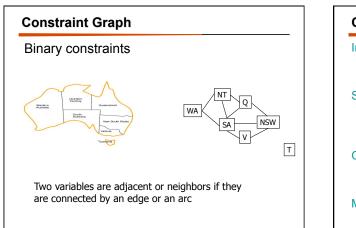
Binary constraints: involve two variables

Higher order constraints: involve 3 or more variables (e.g. all- diff(a,b,c,d,e))

 all higher order constraints can be rewritten as binary constraints by introducing additional variables!

Preference constraints - no absolute - they indicate which solutions are preferred

- I can meet between 3-4, but I'd prefer to meet between 2-3
- Electricity is cheaper at night
- Workers prefer to work in the daytime



CSP as a Search Problem

Initial state:

- {} no assignments

Successor function:

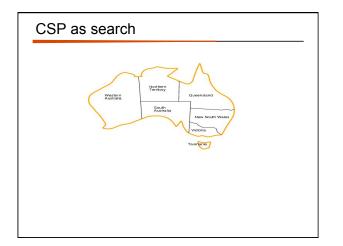
any assignment to an unassigned variable that does not conflict

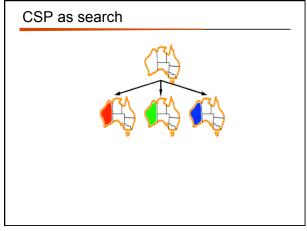
Goal test:

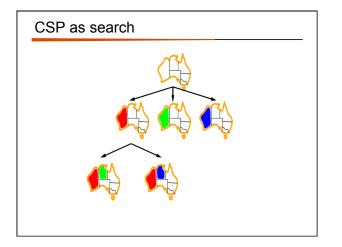
- all variables assigned to?

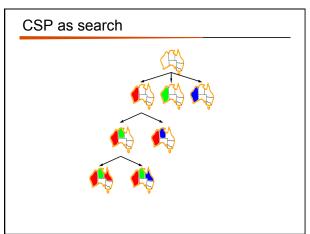
Max search depth?

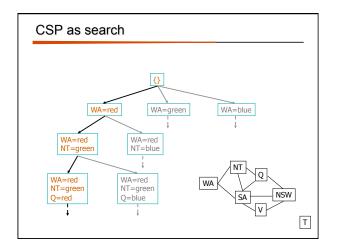
- number of variables

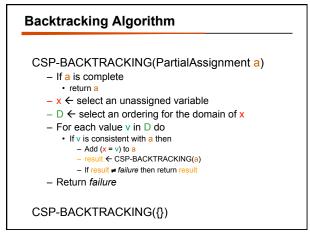


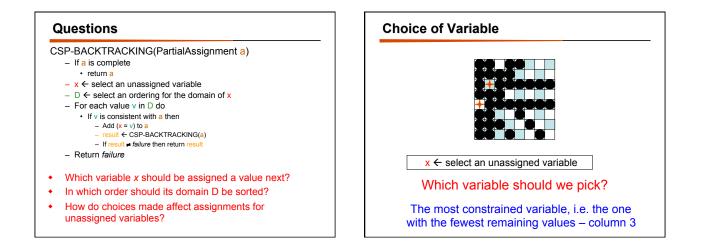


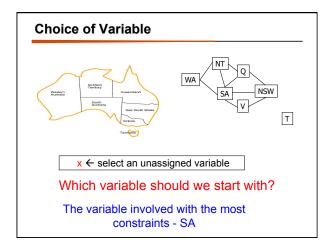


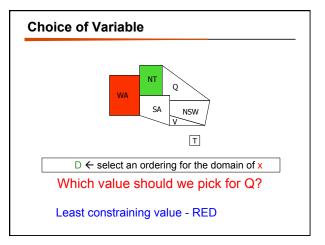


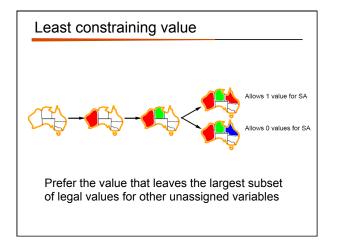












Why CSPs?

Notice that our heuristics work for **any** CSP problem formulation

- unlike our previous search problems!

- does not require any domain knowledge
 - mancala heuristics
 - straight-line distance

Eliminating wasted search

One of the other important characteristics of CSPs is that we can prune the domain values without actually searching (searching implies guessing)

Our goal is to avoid searching branches that will ultimately dead-end

How can we use the information available at early on to help with this process?

Constraint Propagation ...

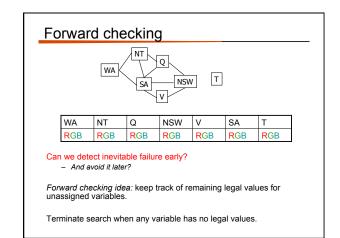
... is the process of determining how the possible values of one variable affect the possible values (domains) of other variables

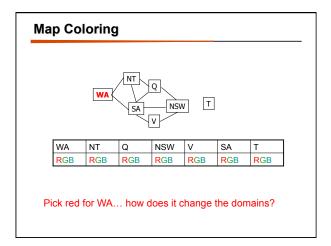


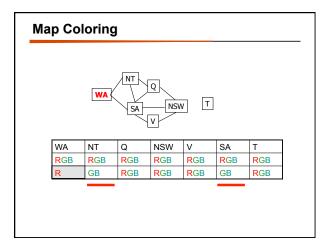
Forward Checking

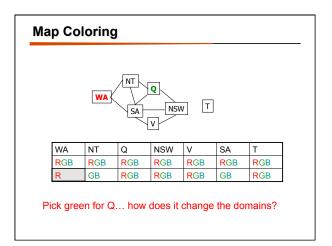
After a variable X is assigned a value v, look at each unassigned variable Y that is connected to X by a constraint and delete from Y's domain any value that is inconsistent with v



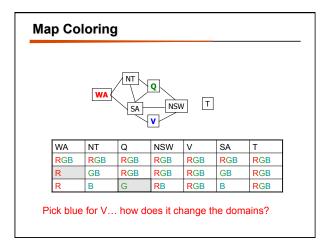




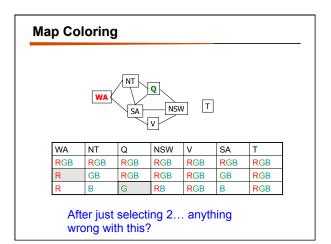


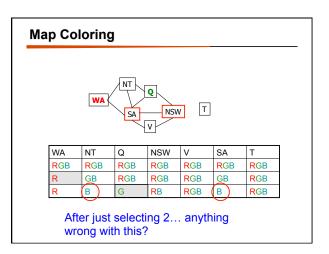


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Removal of Arc Inconsistencies

Given two variables x_i and x_k that are connected by some constraint

We have the current remaining domains D_{xi} and D_{xk}

- For every possible label in D_{xj} if using that label leaves no possible labels in D_{xk}
 - Then get rid of that possible label

See full pseudocode in the book

Arc consistency: AC-3 algorithm

What happens if we remove a possible value during an arc consistency check?

- may cause other domains to change!

When do we stop?

- keep running repeatedly until no inconsistencies remain - can get very complicated to keep track of which to check

Arc consistency: AC-3 algorithm

systematic way to keep track of which arcs still need to be checked

AC-3

- keep track of the set of possible constraints/arcs that may need to be checked
- grab one from this set
- if we make changes to variable's domain, add all of it's constraints into the set
- keep doing this until no constraints exist

Solving a CSP

Search:

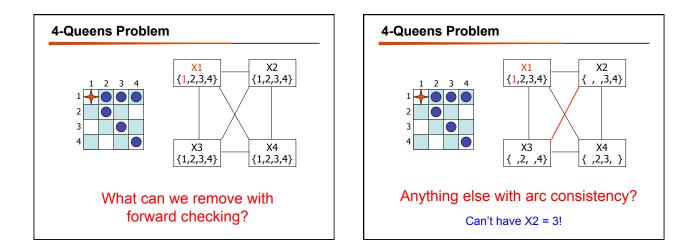
- can find good solutions, but must examine nonsolutions along the way

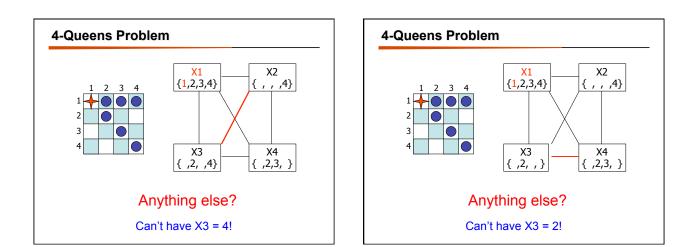
Constraint Propagation:

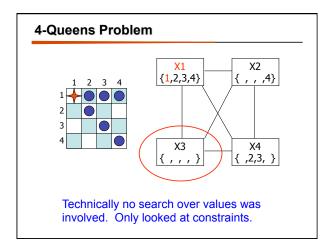
- can rule out non-solutions, but this is not the same as finding solutions

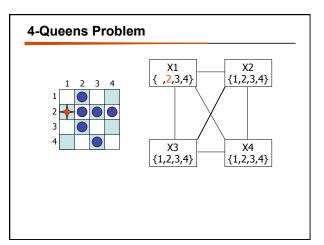
Interweave constraint propagation and search

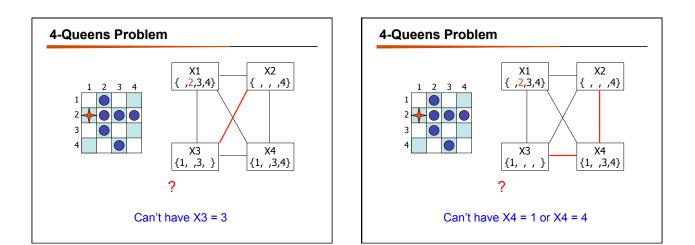
- Perform constraint propagation at each search step.

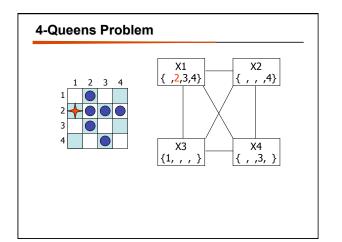


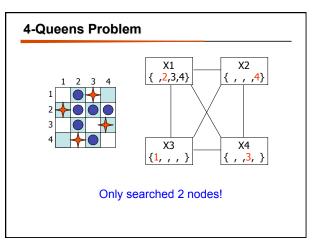












CSP Summary

Key: allow us to use heuristics that are problem independent

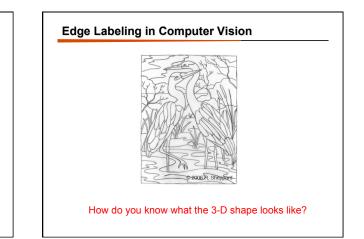
CSP as a search problem

- Backtracking algorithm
 General heuristics

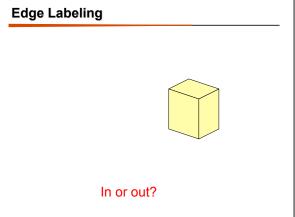
Forward checking

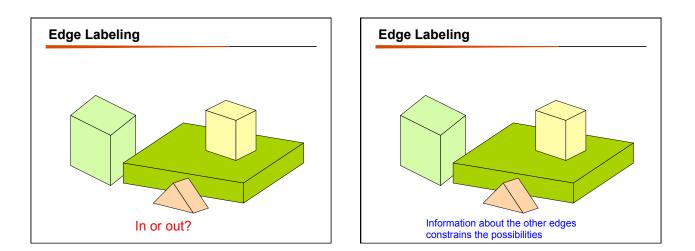
Constraint propagation

Interweaving CP and backtracking









Labels of Edges

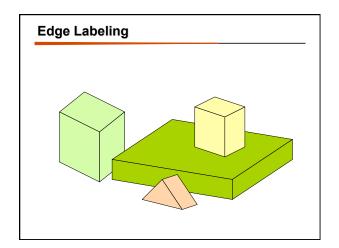
Convex edge:

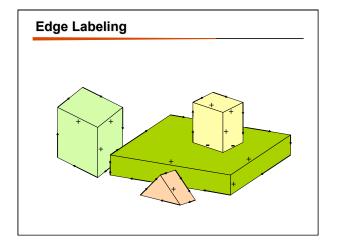
two surfaces intersecting at an angle greater than 180°
 often, "sticking out", "towards us"

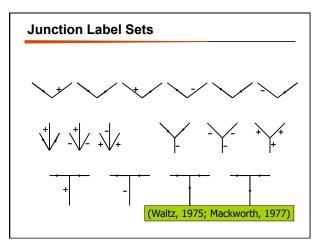
Concave edge

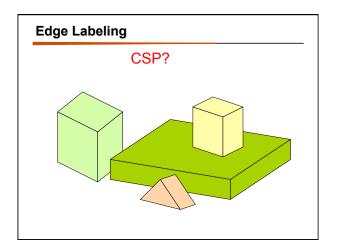
- two surfaces intersecting at an angle less than 180°
 often, "folded in", "away from us"
- + convex edge, both surfaces visible
- concave edge, both surfaces visible

 \leftarrow convex edge, only one surface is visible and it is on the right side of \leftarrow









Edge Labeling as a CSP

A variable is associated with each junction

The domain of a variable is the label set of the corresponding junction

Each constraint imposes that the values given to two adjacent junctions give the same label to the joining edge

