

Admin

Assignment 1 grading

Assignment 2 Due Sunday at midnight









Linear models

A linear model in *n*-dimensional space (i.e. n features) is define by n+1 weights:

In two dimensions, a line: $0 = w_1 f_1 + w_2 f_2 + b \qquad \text{(where } \mathsf{b} = \mathsf{-a}\text{)}$

In three dimensions, a plane:

 $0 = w_1 f_1 + w_2 f_2 + w_3 f_3 + b$

In *n*-dimensions, a hyperplane

$$0 = b + \sum_{i=1}^{\infty} w_i f_i$$















































8







9













Perceptron learning algorithm A trick... repeat until convergence (or for some # of iterations): for each training example $(f_1, f_2, ..., f_n, label)$: Let positive label = 1 and negative label = -1check if it's correct based on the current model if label positive and feature positive: if not correct, update all the weights: increase weight (increase weight = predict more positive) if label positive and feature positive: else if label positive and feature negative: increase weight (increase weight = predict more positive) decrease weight (decrease weight = predict more positive) else if label positive and feature negative: else if label negative and feature positive: decrease weight (decrease weight = predict more positive) decrease weight (decrease weight = predict more negative) else if label negative and feature positive: else if label negative and negative weight: decrease weight (decrease weight = predict more negative) increase weight (increase weight = predict more negative) else if label negative and negative weight: increase weight (increase weight = predict more negative)

label * f_i

1*1=1

1*-1=-1

-1*1=-1

-1*-1=1



Perceptron learning algorithm

repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^n w_i f_i$

if prediction * label \leq 0: // they don't agree for each w; $w_i = w_i + f_i^*$ |abel b = b +|abel

Perceptron learning algorithm

repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^{n} w_i f_i$

if prediction * label \leq 0: // they don't agree for each w_i: $w_i = w_i + f_i^*$ label b = b + label

Would this work for non-binary features, i.e. real-valued?





















Convergence

repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^n w_i f_i$

if prediction * label \leq 0: // they don't agree for each w_i: $w_i = w_i + f_i^*$ |abel b = b +abel

Why do we also have the "some # iterations" check?



Convergence

repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^{n} w_i f_i$

if prediction * label ≤ 0 : // they don't agree for each w; $w_i = w_i + f_i^*$ |abel b = b +|abel

Also helps avoid overfitting! (This is harder to see in 2-D examples, though)

Ordering

repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^{n} w_i f_i$

if prediction * label \leq 0: // they don't agree for each w_i: $w_i = w_i + f_i^*$ label b = b + label

What order should we traverse the examples? Does it matter?

















Ordering

- repeat until convergence (or for some # of iterations): randomize order of training examples
- for each training example ($f_1, f_2, ..., f_n$, label):

prediction =
$$b + \sum_{i=1}^{n} w_i f_i$$

if prediction * label \leq 0: // they don't agree for each w_i: $w_i = w_i + f_i^*$ |abel b = b +abel







Voted perceptron learning

Training

- every time a mistake is made on an example:
- store the weights (i.e. before changing for current example)
- store the number of examples that set of weights got correct

Classify

- calculate the prediction from ALL saved weights
- multiply each prediction by the number it got correct (i.e a weighted vote) and take the sum over all predictions
- said another way: pick whichever prediction has the most votes











Voted perceptron learning

Training

- every time a mistake is made on an example:
- store the weights (i.e. before changing for current example)
- store the number of examples that set of weights got correct

Classify

- calculate the prediction from ALL saved weights
- multiply each prediction by the number it got correct (i.e a weighted vote) and take the sum over all predictions
- said another way: pick whichever prediction has the most votes

Any issues/concerns?

Voted perceptron learning

Training

- every time a mistake is made on an example:
- store the weights (i.e. before changing for current example)
- store the number of examples that set of weights got correct

Classify

- calculate the prediction from ALL saved weights
- multiply each prediction by the number it got correct (i.e a weighted vote) and take the sum over all predictions
- said another way: pick whichever prediction has the most votes
 - 1. Can require a lot of storage
 - 2. Classifying becomes very, very expensive







repeat until convergence (or for some # of iterations): for each training example ($f_1, f_2, ..., f_n$, label): $prediction = b + \sum_{i=1}^{n} w_i f_i$

if prediction * label \leq 0: // they don't agree for each w; $w_i = w_i + f_i^*$ label b = b + label

Why is it called the "perceptron" learning algorithm if what it learns is a line? Why not "line learning" algorithm?























History of Neural Networks

McCulloch and Pitts (1943) – introduced model of artificial neurons and suggested they could learn

Hebb (1949) – Simple updating rule for learning

Rosenblatt (1962) - the perceptron model

Minsky and Papert (1969) – wrote Perceptrons

Bryson and Ho (1969, but largely ignored until 1980s) – invented back-propagation learning for multilayer networks