

Admin

Assignment grading

Assignment 9

Midterm 2

Final project

- No formal class Tuesday: figure out project ideas
- □ 11/23 (Wed) submit project proposal

Quick exercise

Write down on the paper (don't write your name):

- Something you're happy about right now
- 2) Something you're worried about right now

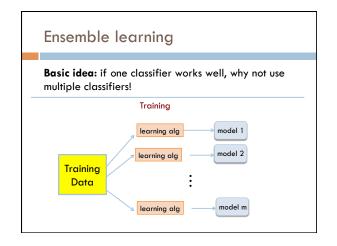
Fold the piece of paper

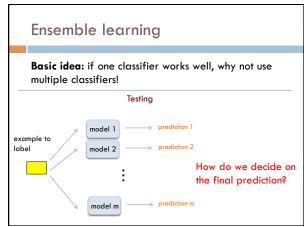
l'll collect them, redistribute them and we'll read them out loud $% \left(1\right) =\left(1\right) \left(1\right) \left$

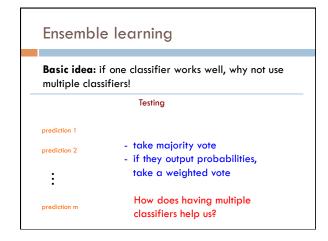
If you don't want to participate, just leave the paper blank

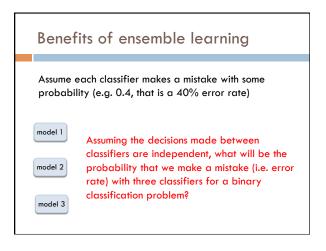
Ensemble learning

Basic idea: if one classifier works well, why not use multiple classifiers!









Benefits of ensemble learning

Assume each classifier makes a mistake with some probability (e.g. 0.4, that is a 40% error rate)

model 1	model 2	model 3	prob
С	С	С	.6*.6*.6=0.216
С	С	I	.6*.6*.4=0.144
С	I	С	.6*.4*.6=0.144
С	I	I	.6*.4*.4=0.096
I	С	С	.4*.6*.6=0.144
I	С	I	.4*.6*.4=0.096
I	I	С	.4*.4*.6=0.096
I	I	I	.4*.4*.4=0.064

Benefits of ensemble learning

Assume each classifier makes a mistake with some probability (e.g. 0.4, that is a 40% error rate)

model 1	model 2	model 3	prob
С	С	С	.6*.6*.6=0.216
С	С	I	.6*.6*.4=0.144
С	I	С	.6*.4*.6=0.144
С	I	I	.6*.4*.4=0.096
I	С	С	.4*.6*.6=0.144
I	С	I	.4*.6*.4=0.096
I	I	С	.4*.4*.6=0.096
I	I	I	.4*.4*.4=0.064

0.096+ 0.096+ 0.096+ 0.064 = **35% error!**

Benefits of ensemble learning

3 classifiers in general, for r = probability of mistake for individual classifier:

$$p(error) = 3r^2(1-r) + r^3$$

binomial distribution

r	p(error)
0.4	0.35
0.3	0.22
0.2	0.10
0.1	0.028
0.05	0.0073

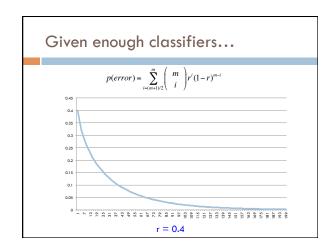
Benefits of ensemble learning

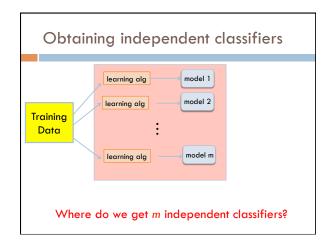
5 classifiers in general, for r = probability of mistake for individual classifier:

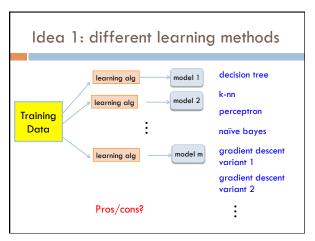
$$p(error) = 10r^3(1-r)^2 + 5r^4(1-r) + r^5$$

r	p(error) 3 classifiers	p(error) 5 classifiers
0.4	0.35	0.32
0.3	0.22	0.16
0.2	0.10	0.06
0.1	0.028	0.0086
0.05	0.0073	0.0012

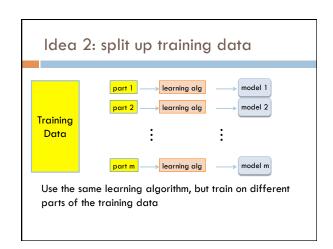
Benefits of ensemble learning $\begin{array}{l} \text{m classifiers in general, for r = probability of mistake} \\ \\ p(error) = \sum_{i=(m+1)/2}^m \binom{m}{i} r^i (1-r)^{m-i} \\ \\ \text{(cumulative probability distribution for the binomial distribution)} \end{array}$

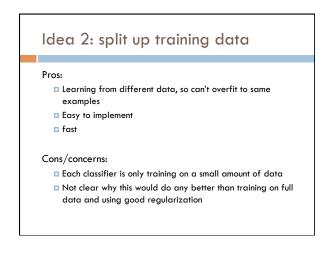


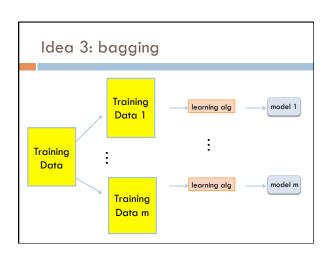


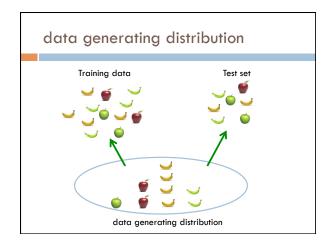


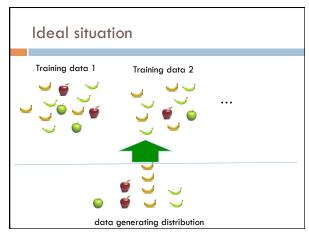
Pros: Lots of existing classifiers already Can work well for some problems Cons/concerns: Often, classifiers are not independent, that is, they make the same mistakes! e.g. many of these classifiers are linear models voting won't help us if they're making the same mistakes

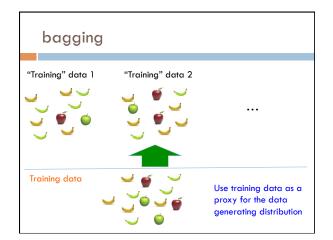




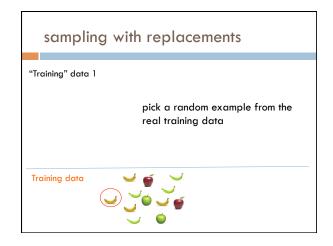


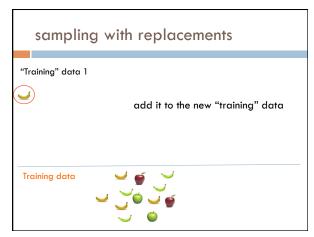


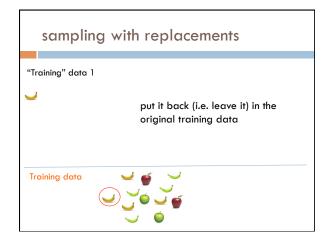


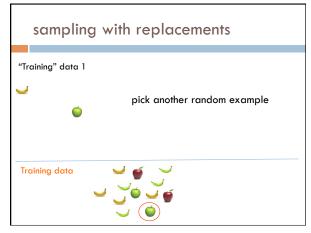


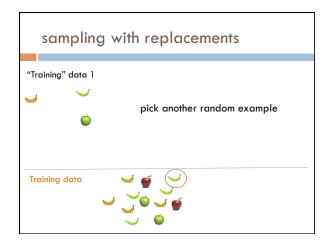


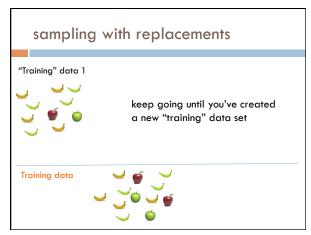








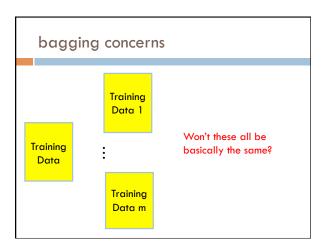


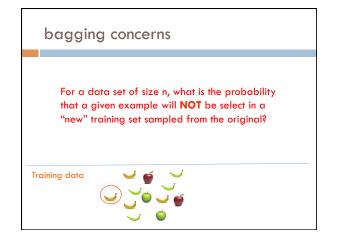


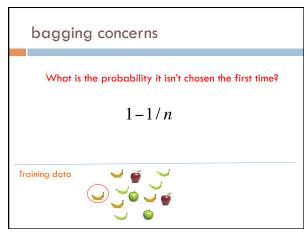
create m "new" training data sets by sampling with replacement from the original training data set (called m "bootstrap" samples)

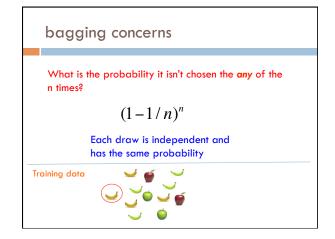
train a classifier on each of these data sets

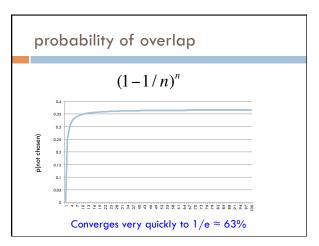
to classify, take the majority vote from the m classifiers

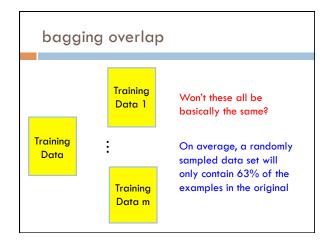




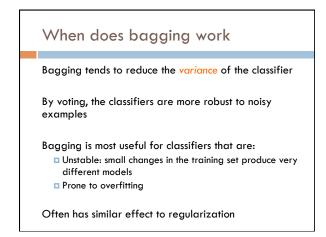


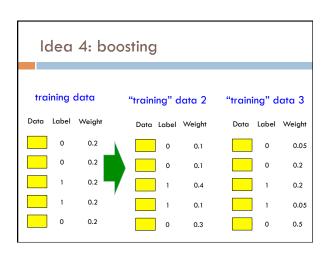


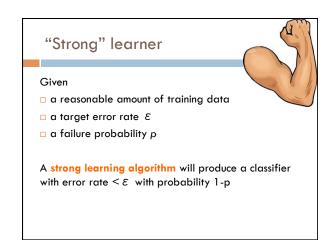


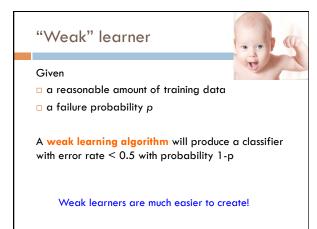


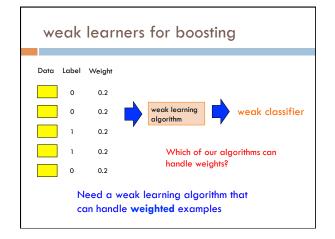
When does bagging work Let's say 10% of our examples are noisy (i.e. don't provide good information) For each of the "new" data set, what proportion of noisy examples will they have? They'll still have ~10% of the examples as noisy However, these examples will only represent about a third of the original noisy examples For some classifiers that have trouble with noisy classifiers, this can help



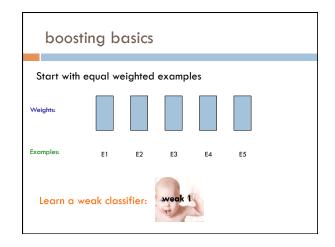


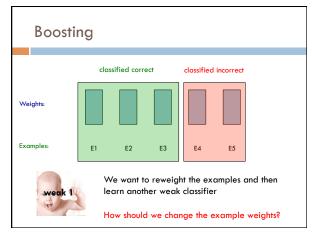


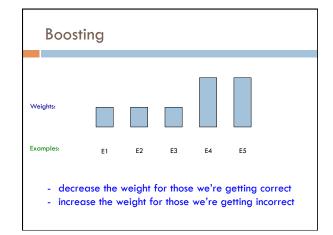


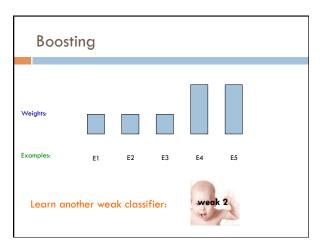


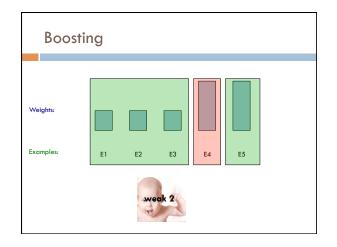
Training: start with equal example weights for some number of iterations: learn a weak classifier and save change the example weights Classify: get prediction from all learned weak classifiers weighted vote based on how well the weak classifier did when it was trained (i.e. in relation to training error)

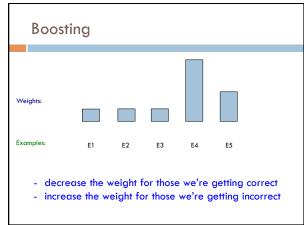


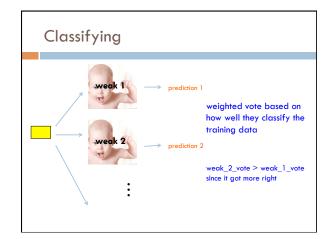


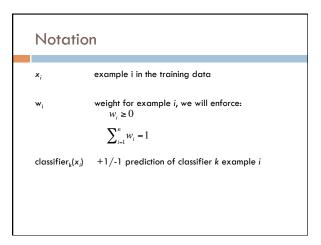












for k = 1 to iterations:

- classifier, = learn a weak classifier based on weights
- calculate weighted error for this classifier

$$\varepsilon_k = \sum_{i=1}^n w_i * 1[label_i \neq classifier_k(x_i)]$$

calculate "score" for this classifier:

$$\alpha_{_{\!\mathit{k}}} = \frac{1}{2} \log \biggl(\frac{1-\varepsilon_{_{\!i}}}{\varepsilon_{_{\!i}}} \biggr)$$
 change the example weights

$$w_i = \frac{1}{Z} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

AdaBoost: train

 $classifier_k = learn a weak classifier based on weights$

weighted error for this classifier is:

$$\varepsilon_k = \sum\nolimits_{i=1}^n w_i *1[label_i \neq classifier_k(x_i)]$$

What does this say?

AdaBoost: train

 $classifier_k = learn a weak classifier based on weights$

weighted error for this classifier is:

$$\varepsilon_k = \sum\nolimits_{i=1}^n w_i * 1[label_i \neq classifier_k(x_i)]$$

What is the range of possible values? did we get the example wrong

weighted sum of the errors/mistakes

AdaBoost: train

 $classifier_k = learn a weak classifier based on weights$

weighted error for this classifier is:

 $\varepsilon_k = \sum\nolimits_{i=1}^n w_i * 1[label_i \neq classifier_k(x_i)]$

get all examples right) and 1 (if we get them all wrong)

Between 0 (if we

weighted sum of the errors/mistakes

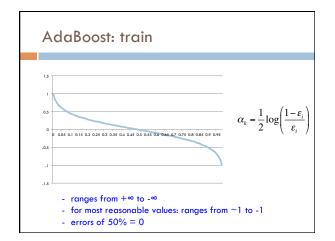
did we get the example wrong

 $classifier_k = learn a weak classifier based on weights$

"score" or weight for this classifier is:

$$\alpha_k = \frac{1}{2} \log \left(\frac{1 - \varepsilon_i}{\varepsilon_i} \right)$$

What does this look like (specifically for errors between 0 and 1)?



AdaBoost: classify

$$classify(x) = sign\left(\sum_{k=1}^{iterations} \alpha_k * classifier_k(x)\right)$$

What does this do?

AdaBoost: classify

$$classify(x) = sign\left(\sum_{k=1}^{iterations} \alpha_k * classifier_k(x)\right)$$

The weighted vote of the learned classifiers weighted by α (remember α generally varies from ~ 1 to -1 training error)

What happens if a classifier has error > 50%

AdaBoost: classify

$$classify(x) = sign\left(\sum_{k=1}^{iterations} \alpha_k * classifier_k(x)\right)$$

The weighted vote of the learned classifiers weighted by α (remember α generally varies from ~ 1 to -1 training error)

We actually vote the opposite!

AdaBoost: train, updating the weights

update the example weights

$$w_i = \frac{1}{7} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

Remember, we want to enforce:

$$w_i \ge 0$$

$$\sum_{i=1}^{n} w_i = 1$$

Z is called the normalizing constant. It is used to make sure that the weights sum to 1

What should it be?

AdaBoost: train

update the example weights

$$w_i = \frac{1}{Z} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

Remember, we want to enforce:

$$w_i \ge 0$$
$$\sum_{i=1}^n w_i = 1$$

normalizing constant (i.e. the sum of the "new" w_i):

$$Z = \sum_{i=1}^{n} w_{i} \exp(-\alpha_{k} * label_{i} * classifier_{k}(x_{i}))$$

AdaBoost: train

update the example weights

$$w_i = \frac{1}{7} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

What does this do?

update the example weights

$$w_i = \frac{1}{Z} w_i \exp\left(-\alpha_k * label_i * classifier_k(x_i)\right)$$

$$\begin{array}{c} \text{correct} & \Rightarrow \text{ positive} \\ \text{incorrect} & \Rightarrow \text{ negative} \\ \\ \text{correct} & \\ \text{incorrect} & \\ \end{array}$$

AdaBoost: train

update the example weights

$$w_i = \frac{1}{Z} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

$$\text{correct} \rightarrow \text{positive}$$

$$\text{incorrect} \rightarrow \text{negative}$$

$$\text{correct} \rightarrow \text{small value}$$

$$\text{incorrect} \rightarrow \text{large value}$$

Note: only change weights based on current classifier (not all previous classifiers)

AdaBoost: train

update the example weights

$$w_i = \frac{1}{Z} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

What does the α do?

AdaBoost: train

update the example weights

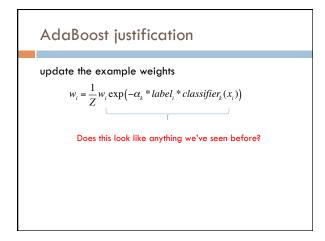
$$w_i = \frac{1}{Z} w_i \exp(-\alpha_k * label_i * classifier_k(x_i))$$

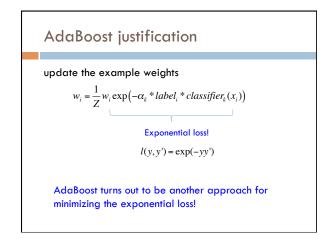
What does the $\,lpha\,$ do?

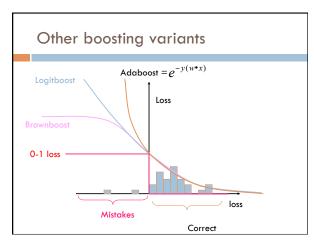
If the classifier was good (<50% error) α is positive: trust classifier output and move as normal If the classifier was back (>50% error) α is negative

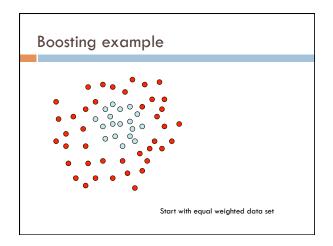
If the classifier was back (>50% error) α is negative classifier is so bad, consider opposite prediction of classifier

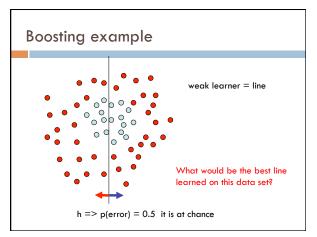
update the example weights $w_i = \frac{1}{Z} w_i \exp\left(-\alpha_k * label_i * classifier_k(x_i)\right)$ $\begin{array}{c} \text{correct positive} \\ \text{incorrect negative} \end{array}$ $\begin{array}{c} \text{correct small value} \\ \text{incorrect large value} \end{array}$ If the classifier was good (<50% error) α is positive If the classifier was back (>50% error) α is negative

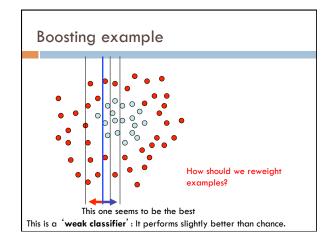


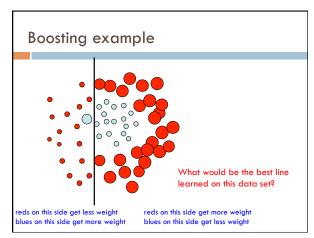


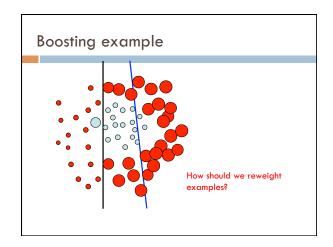


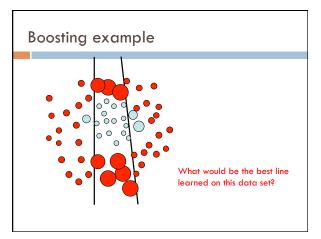


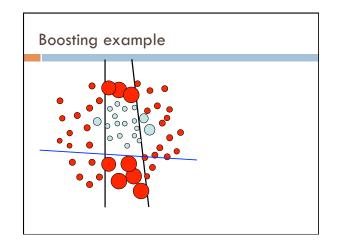


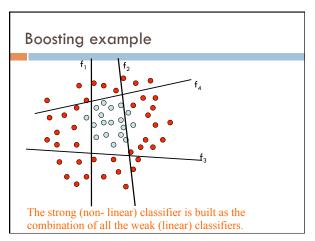












for k = 1 to iterations:

- classifier, = learn a weak classifier based on weights
- weighted error for this classifier is:
- "score" or weight for this classifier is:
- change the example weights

What can we use as a classifier?

AdaBoost: train

for k = 1 to iterations:

- $classifier_k = learn a weak classifier based on weights$
- weighted error for this classifier is:
- "score" or weight for this classifier is:
- change the example weights
- Anything that can train on weighted examples
- For most applications, must be fast! Why?

AdaBoost: train

for k = 1 to iterations:

- $\operatorname{classifier}_{k} = \operatorname{learn} a$ weak classifier based on weights
- weighted error for this classifier is:
- "score" or weight for this classifier is:
- change the example weights
- Anything that can train on weighted examples
- For most applications, must be fast!
 - Each iteration we have to train a new classifier

Boosted decision stumps

One of the most common classifiers to use is a decision tree:

- can use a shallow (2-3 level tree)
- even more common is a 1-level tree
 - called a decision stump ©
 - asks a question about a single feature

What does the decision boundary look like for a decision stump?

Boosted decision stumps

One of the most common classifiers to use is a decision tree:

- can use a shallow (2-3 level tree)
- even more common is a 1-level tree
- called a decision stump ©
- asks a question about a single feature

What does the decision boundary look like for boosted decision stumps?

Boosted decision stumps

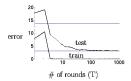
One of the most common classifiers to use is a decision tree:

- can use a shallow (2-3 level tree)
- even more common is a 1-level tree
- called a decision stump ©
- asks a question about a single feature
- Linear classifier!
- Each stump defines the weight for that dimension
- If you learn multiple stumps for that dimension then it's the weighted average

Boosting in practice

Very successful on a wide range of problems

One of the keys is that boosting tends not to overfit, even for a large number of iterations



Using <10,000 training examples can fit >2,000,000 parameters!

Adaboost application example: face detection



Adaboost application example: face detection



Rapid Object Detection using a Boosted Cascade of Simple **Features**

Paul Viola viola@merl.com Mitsubishi Electric Research Labs 201 Broadway, 8th FL Cambridge, MA 02139

Michael Jones
mjones@crl.dec.com
Compaq CRL
One Cambridge Center
Cambridge, MA 02142

Rapid object detection using a boosted cascade of simple features
P Viola, M Jones - ... Vision and Pattern Recognition, 2001, CVPR ..., 2001 - leeexpli
... oversp, Each partition yields a single final detection. The ... set. Experiments on a
Real-World Test Set We tested our system on the MIT+CMU frontal face test set [II].
This set consists of 130 images with 507 labeled frontal faces. A ...
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Rapid object detection using a boosted cascade of simple features P Viola, M Jones - . . Vision and Pattern Recognition, 2001, CVPR ..., 2001 - leexcylo ... overlap, Each partition yields a single final detection. The .. set. Experiments on Real-World Test Set We tested our system on the MIT+CMU frontal face test set [II]. This set consists of 130 images with 507 labeled frontal faces. A consistency of the Co

To give you some context of importance:

The anatomy of a large-scale hyperfextual Web search engine
S Brin, L Page - Computer networks and ISDN systems, 1968 - Elsevier
This is largely because they all have high PageRank. ... However, once the system was running smoothly. S Brin, L PagelComputer Networks and ISDN Systems 30 ... Google employs a number of techniques to improve search quality including page rank, anchor text, and proximity ...

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Modeling word burstiness using the Dirichlet distribution
RE Madsen, D Kauchak, C Elkan - Proceedings of the 22nd international ..., 2005 - d.la.cm.org
Abstract Multimonial distributions are often used to model text documents. However, they do
not capture well the phenomenon that words in a document tend to appear in bursts: if a
word appears once, it is more likely to appear again. In this paper, we propose the ...
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"weak" learners 4 Types of "Rectangle filters" (Similar to Haar wavelet Papageorgiou, et al.) Based on 24x24 grid: 160,000 features to choose from g(x) =sum(WhiteArea) - sum(BlackArea)

