## In-Class Worksheet Discrete Math & Functional Programming— CSCI 054— Spring 2024 Instructor: Osborn

Let T(n) be the number of filled triangles in a Sierpinski's triangle after n interations where T(0) is a single filled triangle. Observe that T(n) = 3T(n-1)

Use induction to prove that  $T(n) = 3^n$ .

Consider the recurrence relation:

$$T(n) = 5T(n-1) - 6T(n-2)$$
  
 $T(0) = 2$   
 $T(1) = 5$ 

Claim:  $\forall n \in \mathbb{Z}_0^+ : T(n) = 2^n + 3^n$ 

- We prove the claim using a proof by strong induction on:
- Base case(s):
- Inductive hypothesis (IHOP):
- Inductive step:
  - We want to show that:
  - Proof:

• Therefore by the principle of mathematical induction: