Adversarial Search

CS51A David Kauchak Spring 2025

Some material borrowed from : Sara Owsley Sood and others

Admin

Assignment 10

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Midterm 2

Recursion (2/25) through informed search (4/15)

Can bring 2-pages of notes (one double-sided or two singled-sided)

Some sample problems posted

A quick review of search

Problem solving via search:

To define the state space, define three things:

- is_goalnext_states
- starting state

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Uninformed search vs. informed search

- what's the difference?
- what are the techniques we've seen?
- pluses and minuses?

3

Why should we study games?

Clear success criteria

Important historically for AI

Fun 😊

Good application of search

 hard problems (chess 35¹⁰⁰ states in search space, 10⁴⁰ legal states)

Some real-world problems fit this model

- game theory (economics)
- multi-agent problems

Types of games

What are some of the games you've played?

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Types of games: game properties

single-player vs. 2-player vs. multiplayer

Fully observable (perfect information) vs. partially observable

Discrete vs. continuous

real-time vs. turn-based

deterministic vs. non-deterministic (chance)

Strategic thinking [?] intelligence

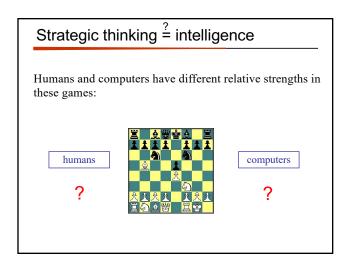
Two-player games have been a focus of AI since its inception...

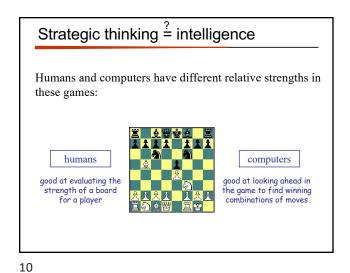


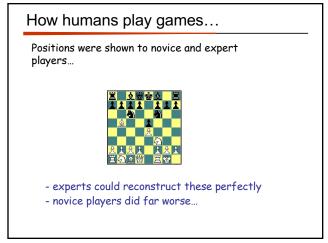
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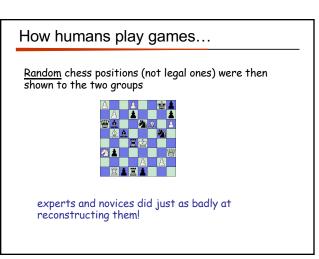
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Important question: Is strategic thinking the same as intelligence?

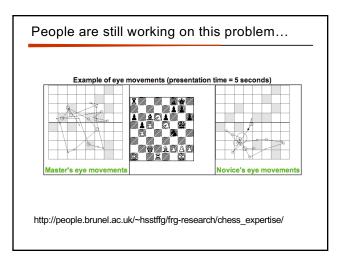


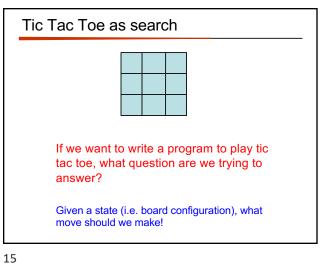


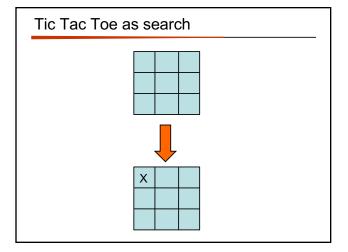


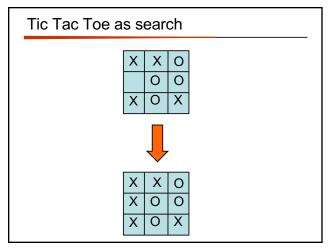


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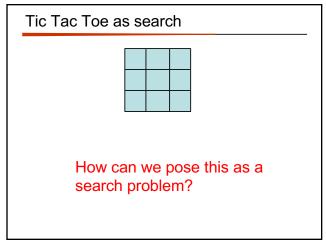


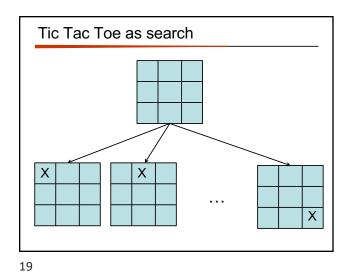


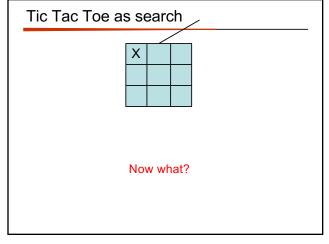


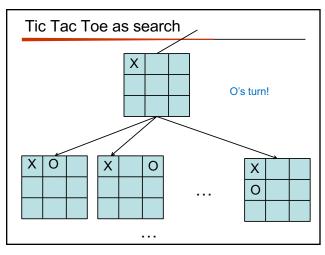


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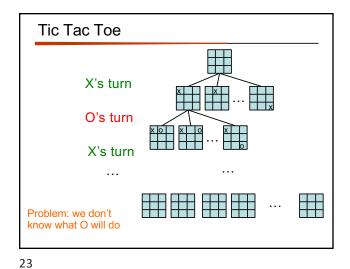


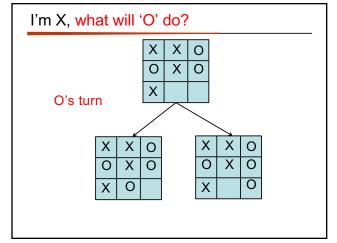


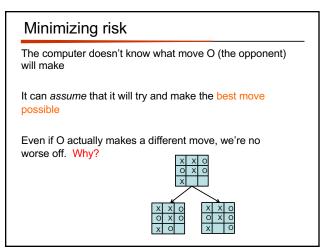


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Optimal Strategy

An Optimal Strategy is one that is at least as good as any other, no matter what the opponent does

- If there's a way to force the win, it will
- Will only lose if there's no other option

Defining a scoring function Χ Χ 0 $X \mid$ 0 Χ Χ 0 X X O O X 0 X O X 0 0 X 0 LOSE WIN TIE 0 -1 +1 Idea: define a function that gives us a "score" for how good each state is higher scores mean better

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Defining a scoring function

Our (X) turn



What should be the score of this state?

+1: we can get to a win

Defining a scoring function

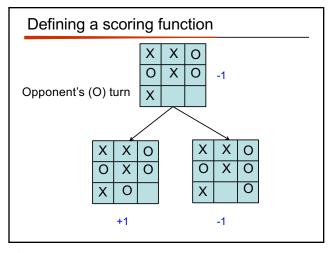
Opponent's (O) turn

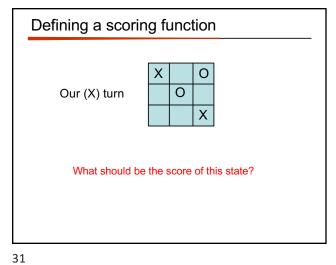


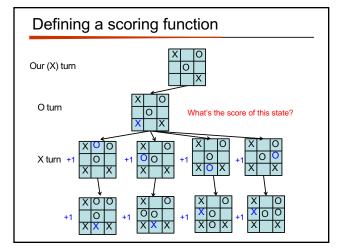
What should be the score of this state?

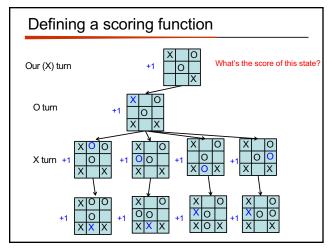
-1: opponent can get to a win

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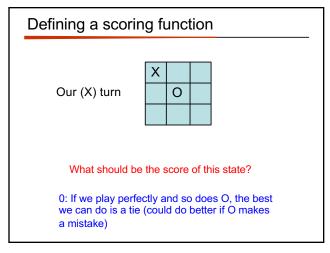


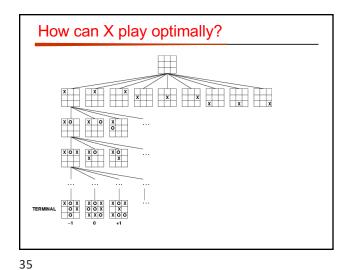


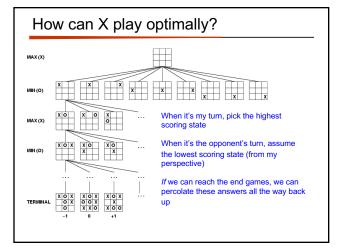




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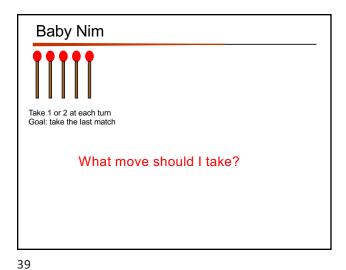
How can X play optimally?

Start from the bottom and propagate the score up:

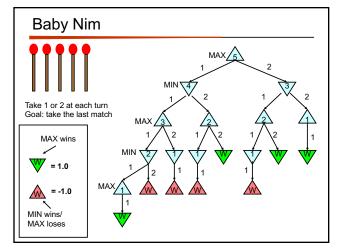
- if X's turn, pick the move that maximizes the utility
- if O's turn, pick the move that minimizes the utility

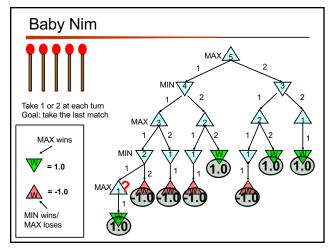
Is this optimal?

Minimax Algorithm: An Optimal Strategy minimax(state) = if state is a terminal state score(state) else if MY turn over all next states, s: return the maximum of minimax(s) else if OPPONENTS turn over all next states, s: return the minimum of minimax(s) Uses recursion to compute the "value" of each state Searches down to the leaves, then the values are "backed up" through the tree as the recursion finishes What type of search is this? What does this assume about how MIN will play? What if this isn't true?

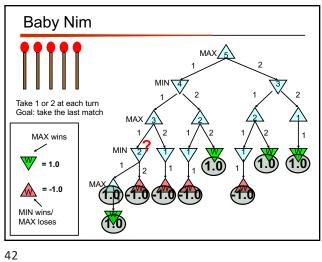


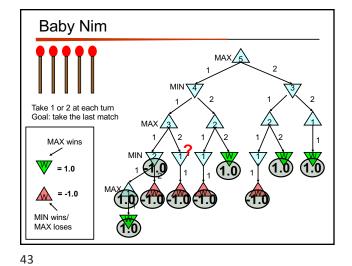
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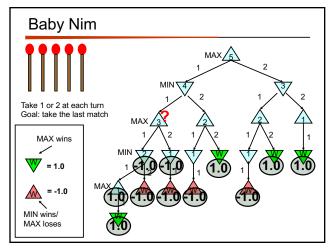


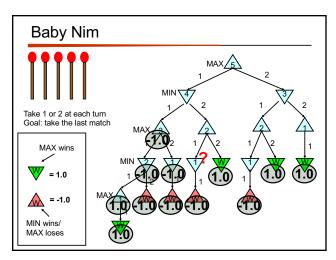


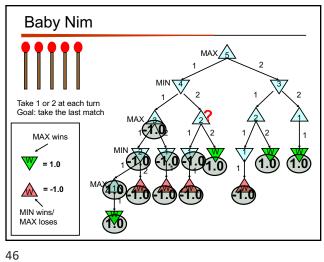
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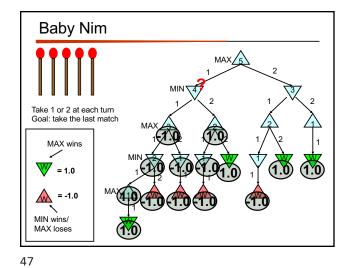


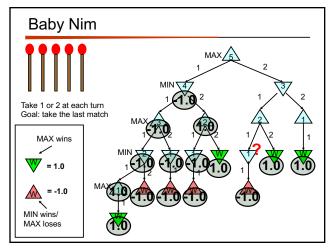


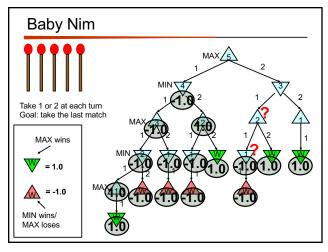


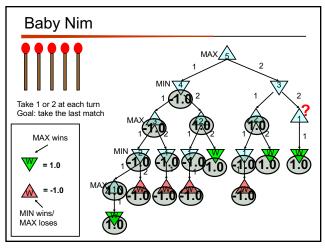


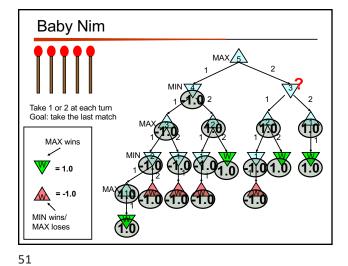


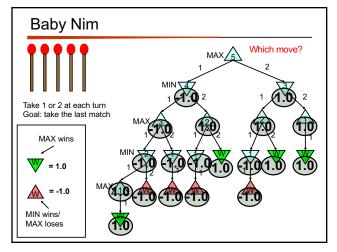


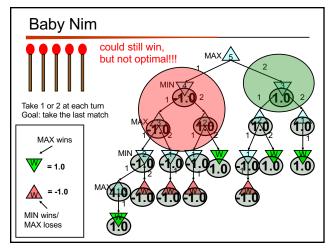




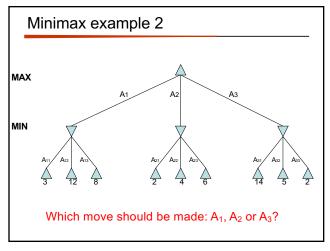


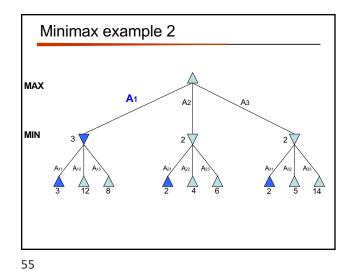


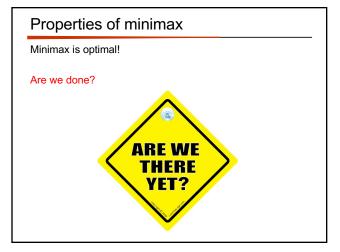


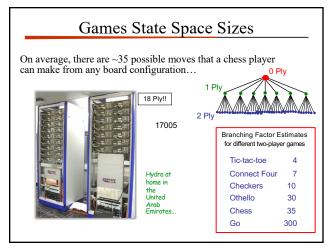


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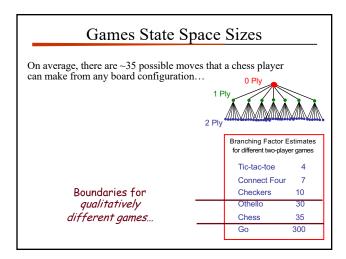


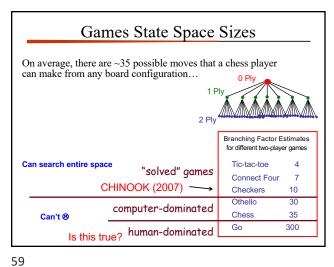


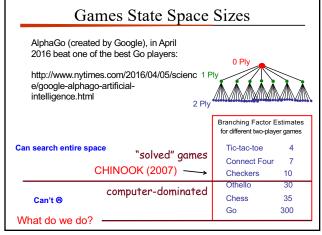


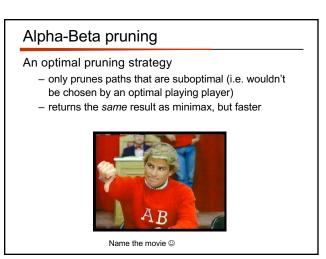


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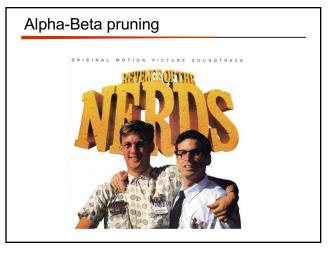


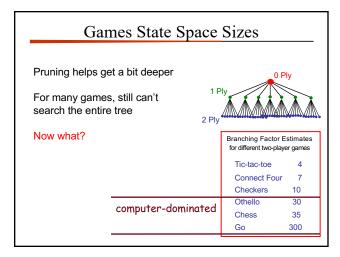


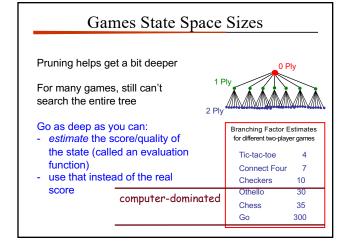


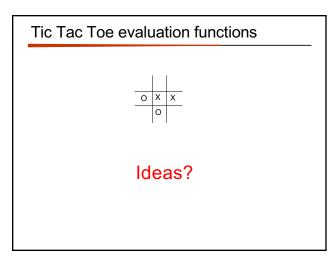


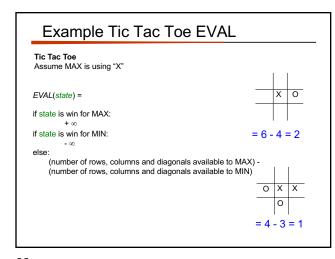
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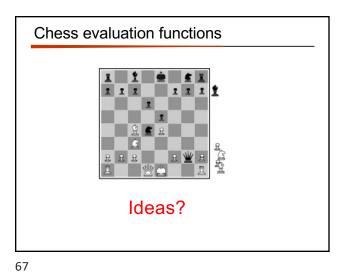


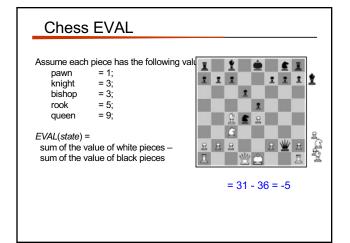


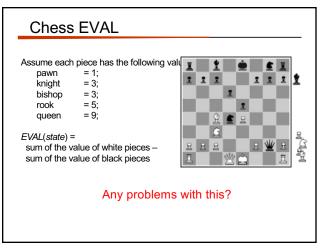




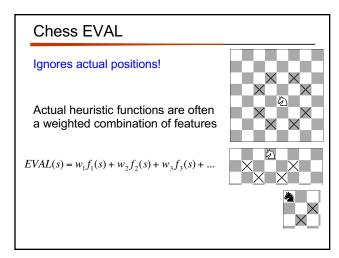








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Chess EVAL

 $EVAL(s) = w_1 f_1(s) + w_2 f_2(s) + w_3 f_3(s) + \dots$ $\begin{array}{c} \text{number} \\ \text{of pawns} \\ \text{of} \\ \text{attacked} \\ \text{knighte}, \\ \text{otherwise} \\ \end{array}$

A feature can be any numerical information about the board

- as general as the number of pawns
- to specific board configurations

Deep Blue: 8000 features!

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history/end-game tables

History

- keep track of the quality of moves from previous games
- use these instead of search

end-game tables

- do a reverse search of certain game configurations, for example all board configurations with king, rook and king
- $-\,$ tells you what to do in ${\it any}$ configuration meeting this criterion
- if you ever see one of these during search, you lookup exactly what to do

end-game tables

Devastatingly good

Allows much deeper branching

- for example, if the end-game table encodes a 20-move finish and we can search up to 14
- can search up to depth 34

Stiller (1996) explored all end-games with 5 pieces

- one case check-mate required 262 moves!

Knoval (2006) explored all end-games with 6 pieces

- one case check-mate required 517 moves!

Traditional rules of chess require a capture or pawn move within 50 or it's a stalemate

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Opening moves

At the very beginning, we're the farthest possible from any goal state

People are good with opening moves

Tons of books, etc. on opening moves

Most chess programs use a database of opening moves rather than search

Nim

K piles of coins

On your turn you must take one or more coins from one pile

Player that takes the last coin wins

Example:

https://www.goobix.com/games/nim/