

Foxes and Chickens

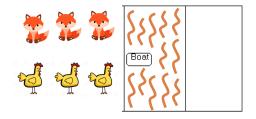
Three foxes and three chickens wish to cross the river. They have a small boat that will carry up to two animals. Everyone can navigate the boat. If at any time the foxes outnumber the chickens on either bank of the river, they will eat the chickens. Find the smallest number of crossings that will allow everyone to cross the river safely.

What is the "state" of this problem (it should capture all possible valid configurations)?



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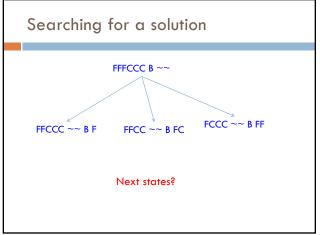
Three foxes and three chickens wish to cross the river. They have a small boat that will carry up to two animals. Everyone can navigate the boat. If at any time the foxes outnumber the chickens on either bank of the river, they will eat the chickens. Find the smallest number of crossings that will allow everyone to cross the river safely. FFFCCC B FFC B FC FC B FFCC They have a small boat that any time the boat. If at any time the foxes outnumber of crossings that will allow everyone to cross the river safely.

Searching for a solution

FFFCCC B ~~

What states can we get to from here?

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Fox and Chickens Solution FFCC |~~~~|B FC FFCCC B|~~~~| F CCC |~~~~|B FFF FCCC B|~~~~| FF |~~~~|B FFCC FC B|~~~~| FC FFCC FF |~~~~|B FCCC B|~~~~| CCC FFF |~~~~|B FFCCC Bl~~~~~| FFCC |~~~~|B FFFCCC How is this solution different than the n-queens problem?

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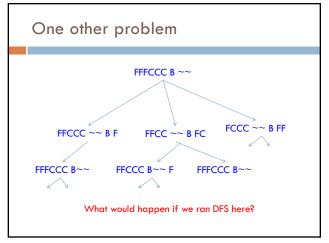
Fox and Chickens Solution FFFCCC B|~~~~~| FFCC |~~~~|B FC FFCCC B|~~~~~| F CCC |~~~~|B FFF FCCC B|~~~~~| FF |~~~~|B FFCC FC FFCC B|~~~~~| FC |~~~~|B FCCC FF FFF B|~~~~| CCC |~~~~|B FFCCC Bl~~~~~| FFCC FC |~~~~|B FFFCCC Solution is not a state, but a sequence of actions (or a sequence of states)

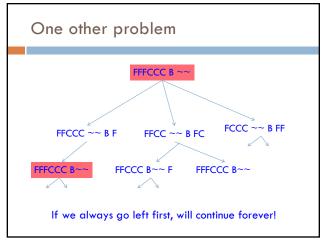
Code!

https://cs.pomona.edu/classes/cs51a/examples/chickens.txt

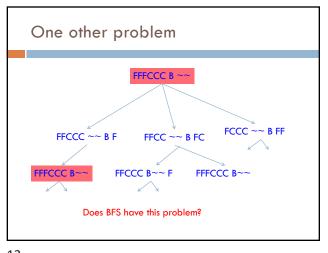
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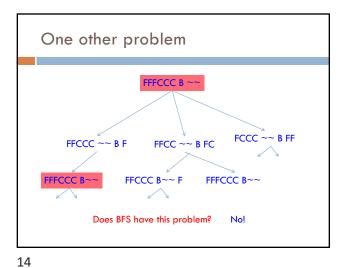
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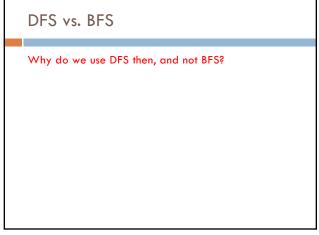


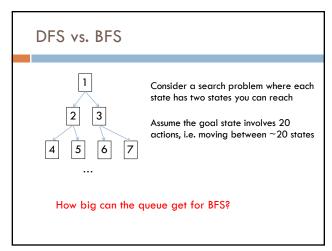


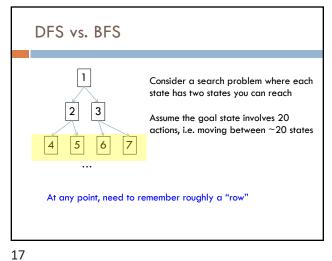
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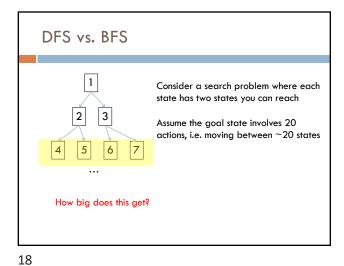


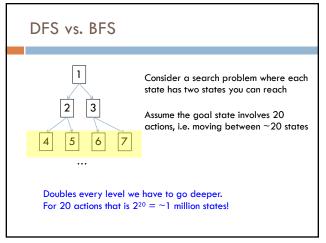


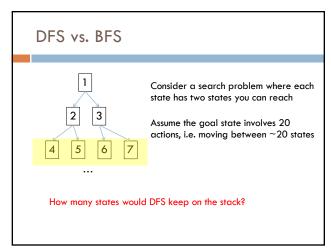


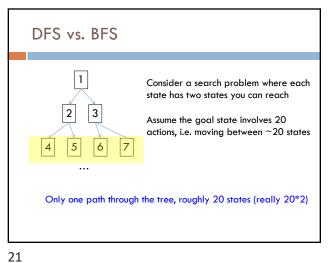


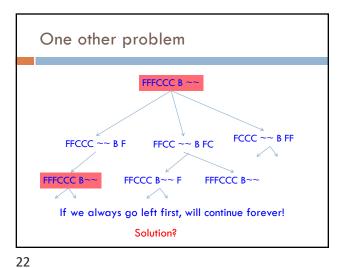






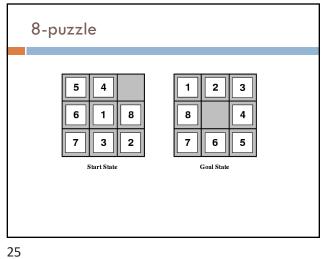


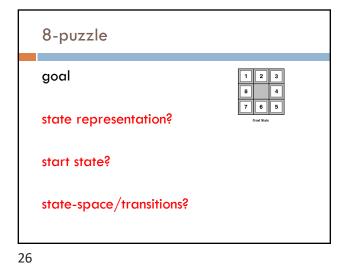


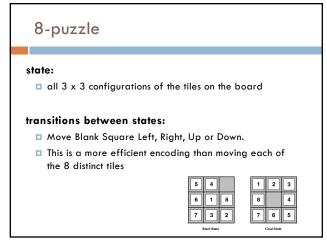


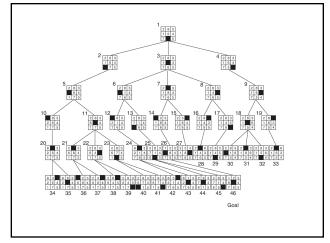
DFS avoiding repeats def dfs(state, visited):
 # note that we've visited this state
 visited[str(state)] = True if state.is_goal():
 return [state]
else:
 result = [] for s in state.next_states():
 # check if we've visited a state already
 if not(str(s) in visited):
 result += dfs(s, visited) return result

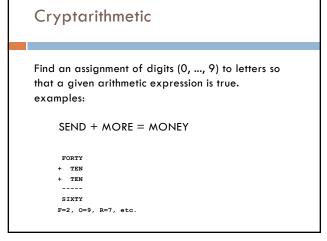
Other search problems What problems have you seen that could be posed as search problems? What is the state? Start state Goal state State-space/transition between states

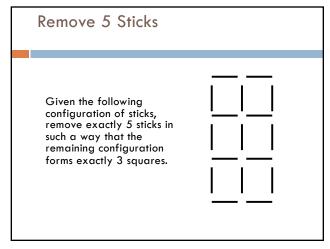


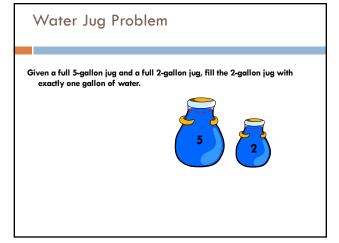


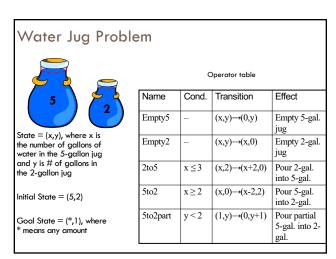




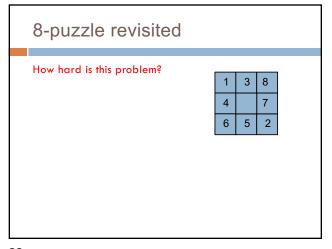


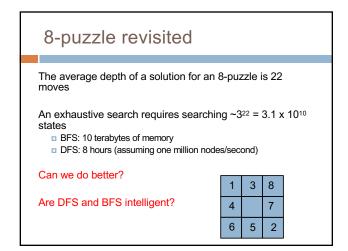


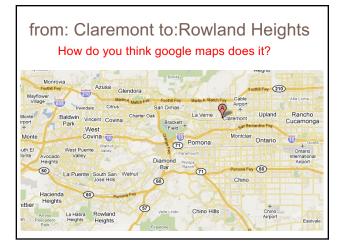


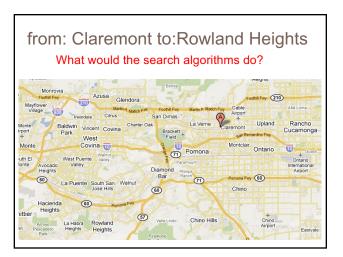


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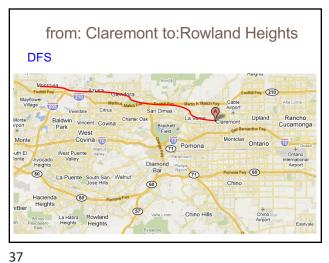


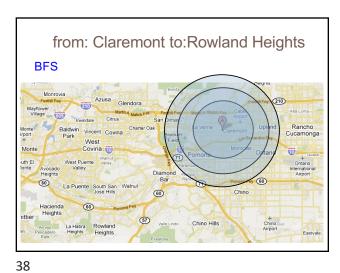


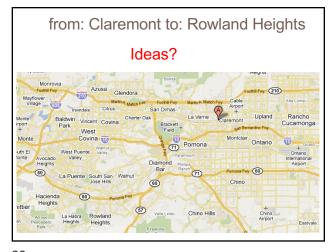


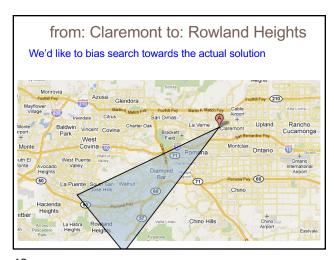


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Informed search

Order to_visit based on some knowledge of the world that estimates how "good" a state is

□ *h*(*n*) is called an evaluation function

Best-first search

- rank to visit based on h(n)
- take the most desirable state in to_visit first
- different approaches depending on how we define *h(n)*

Heuristic

Merriam-Webster's Online Dictionary

Heuristic (pron. \hyu-'ris-tik\): adj. [from Greek heuriskein to discover.] involving or serving as an aid to learning, discovery, or problem-solving by experimental and especially trial-and-error methods

The Free On-line Dictionary of Computing (2/19/13)

heuristic 1. Of or relating to a usually speculative formulation serving as a guide in the investigation or solution of a problem: "The historian discovers the past by the judicious use of such a heuristic device as the 'ideal type'" (Karl J. Weintraub).

41 42

Heuristic function: *h(n)*

An estimate of how close the node is to a goal

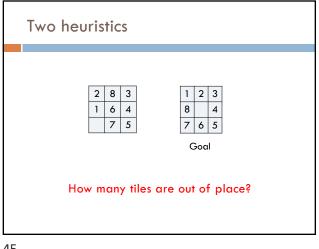
Uses domain-specific knowledge!

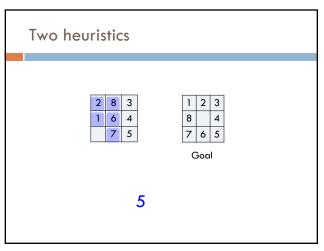
Examples

- Map path finding?
- straight-line distance from the node to the goal ("as the crow flies")
- 8-puzzle?
 - how many tiles are out of place
 - sum of the "distances" of the out of place tiles
- Foxes and Chickens?
 - number of animals on the final bank

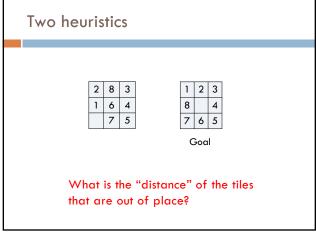
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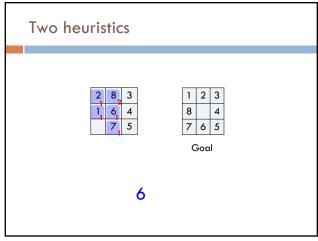
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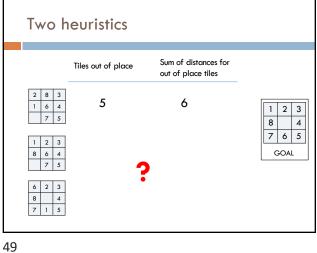


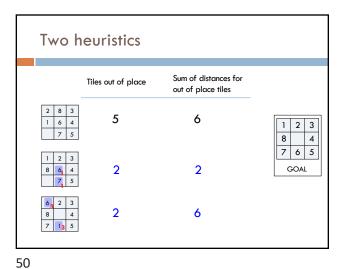
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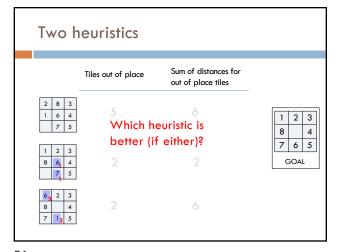


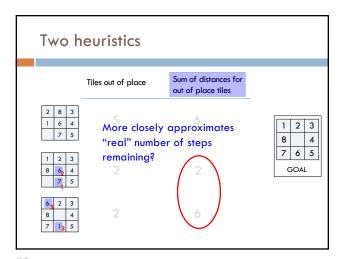


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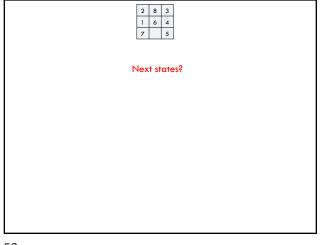


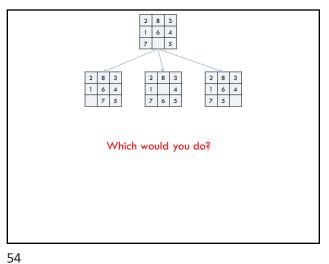




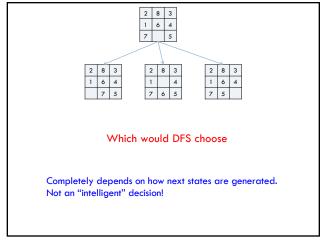


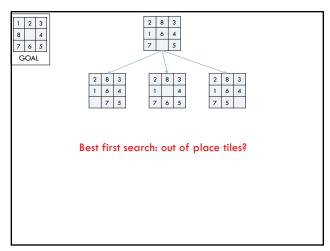
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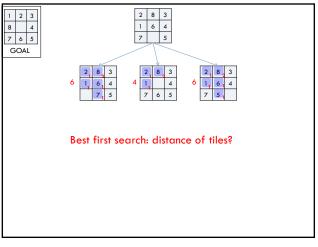
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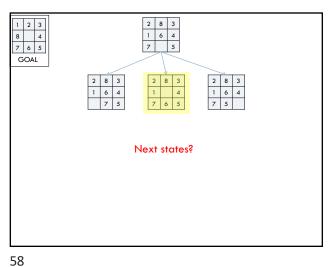




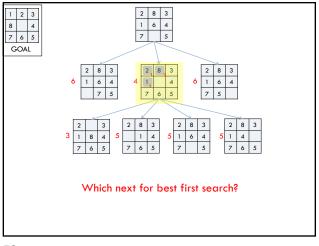
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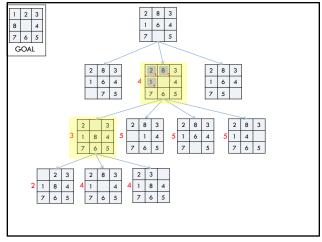
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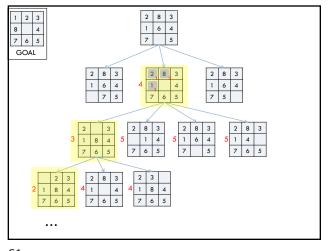


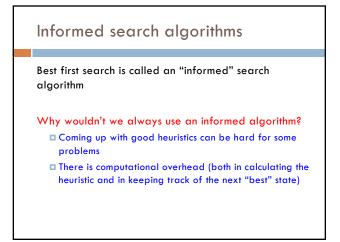
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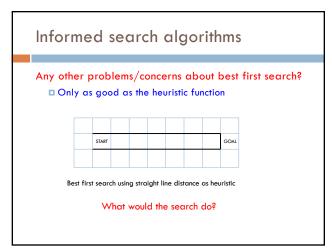
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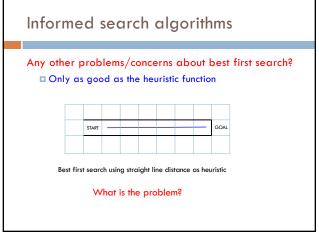


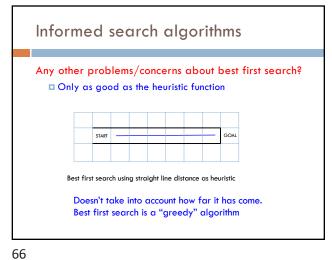
Informed search algorithms

Any other problems/concerns about best first search?



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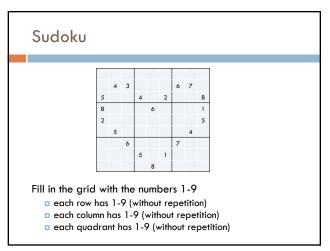
Informed search algorithms

Best first search is called an "informed" search algorithm

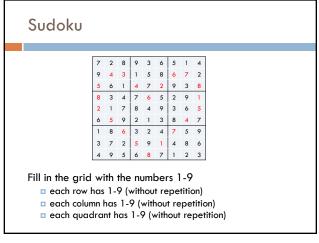
There are many other informed search algorithms:

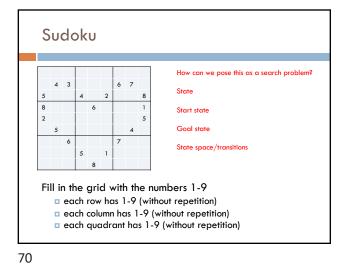
A* search (and variants)

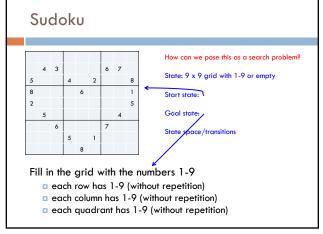
Theta*
Beam search



67 68







Sudoku

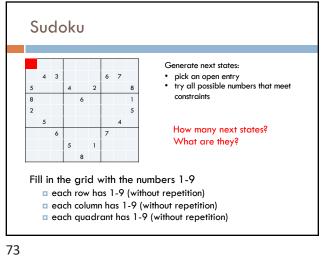
Generate next states:

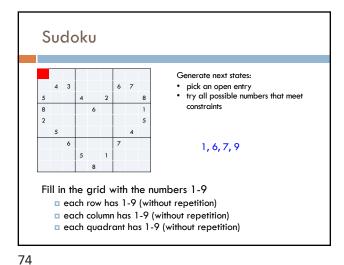
• pick an open entry
• try all possible numbers that meet constraints

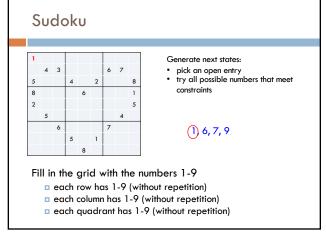
Fill in the grid with the numbers 1-9

• each row has 1-9 (without repetition)
• each quadrant has 1-9 (without repetition)
• each quadrant has 1-9 (without repetition)

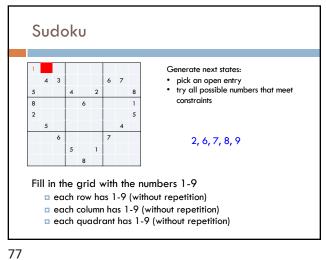
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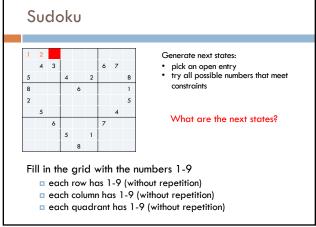


Sudoku Generate next states: pick an open entry try all possible numbers that meet 4 3 constraints How many next states? What are they? Fill in the grid with the numbers 1-9 a each row has 1-9 (without repetition) a each column has 1-9 (without repetition) a each quadrant has 1-9 (without repetition)

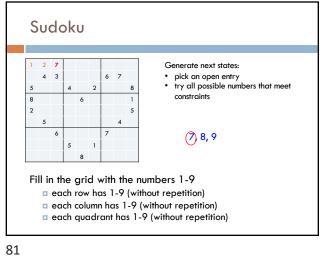


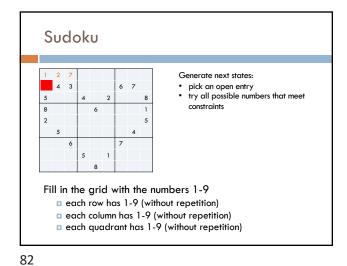
Sudoku Generate next states: pick an open entrytry all possible numbers that meet constraints (2) 6, 7, 8, 9 Fill in the grid with the numbers 1-9 a each row has 1-9 (without repetition) a each column has 1-9 (without repetition) a each quadrant has 1-9 (without repetition)

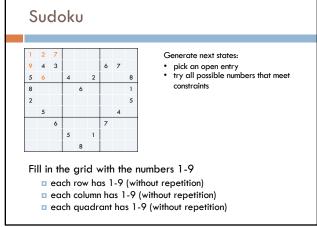
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Sudoku Generate next states: pick an open entry try all possible numbers that meet constraints 7, 8, 9 Fill in the grid with the numbers 1-9 a each row has 1-9 (without repetition) a each column has 1-9 (without repetition) a each quadrant has 1-9 (without repetition)

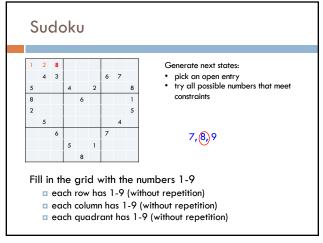






Sudoku Generate next states: pick an open entry try all possible numbers that meet constraints Now what? Try another branch, i.e. go back to a place where we had a decision and try a different one Fill in the grid with the numbers 1-9 a each row has 1-9 (without repetition) a each column has 1-9 (without repetition) a each quadrant has 1-9 (without repetition)

83 84



DFS and BFS will choose entries (and numbers within those entries) randomly

Is that how people do it?

How do you do it?

Heuristics for best first search?

Generate next states:

• pick an open entry

• try all possible numbers that meet constraints

86

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DFS and BFS will choose entries (and numbers within those entries) randomly

Pick the entry that is MOST constrained

People often try and find entries where only one option exists and only fill it in that way (very little search)

Generate next states:

• pick an open entry

• try all possible numbers that meet constraints

Representing the Sudoku board

[1, 6, 7, 9], [1, 2, 6, 7, 8, 9], [1, 2, 7, 8, 9],
[1, 9], 4, 3,
[1, 6, 7, 9], [1, 7, 9]

Which is the most constrained (of the ones above)?

Board is a matrix (list of lists)

Each entry is either:
a number (if we've filled in the space already, either during search or as part of the starting state)
a list of numbers that are valid to put in that entry if it hasn't been filled in yet

