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# CS051A

INTRO TO COMPUTER SCIENCE WITH TOPICS IN AI

18: Problem solving via search and matrices

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Lectures



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Labs

## Lecture 18: Problem solving via search and matrices

- ▶ Problem solving via search
- ▶ Matrices
- ▶ Assignment 9

### Search algorithm

Keep track of a list of states that we *could* visit; we'll call it **to\_visit**.

General idea:

- ▶ take a state off the to\_visit list
- ▶ if it's the goal state
  - ▶ we're done!
- ▶ if it's not the goal state
  - ▶ Add all of the next possible states to the to\_visit list
- ▶ repeat

# Search algorithms

- ▶ add the start state to to\_visit
- ▶ Repeat
  - ▶ take a state off the to\_visit list
  - ▶ if it's the goal state
    - ▶ we're done!
  - ▶ if it's not the goal state
    - ▶ Add all of the next possible states to the to\_visit list
- ▶ Depth first search (DFS): to\_visit is a stack
- ▶ Breadth first search (BFS): to\_visit is a queue

### Implementing the state space

- ▶ What the “world” looks like.
  - ▶ We’ll define the world as a collection of **discrete** states.
  - ▶ States are connected if we can get from one state to another by taking a particular action.
  - ▶ The set of all possible states is called the **state space**.

# Implementing the state space

- ▶ What the “world” looks like.
  - ▶ We’ll define the world as a collection of **discrete** states.
  - ▶ States are connected if we can get from one state to another by taking a particular action.
  - ▶ The set of all possible states is called the **state space**.
- ▶ State:
  - ▶ Is this the goal state? (**is\_goal** function)
  - ▶ What states are connected to this state? (**next\_states** function)

### Search variants implemented

- ▶ add the start state to to\_visit
- ▶ Repeat
  - ▶ take a state off the to\_visit list
  - ▶ if it's the goal state
    - ▶ we're done!
  - ▶ if it's not the goal state
    - ▶ Add all of the next possible states to the to\_visit list

```
def dfs(start_state):
    s = Stack()
    return search(start_state, s)

def bfs(start_state):
    q = Queue()
    return search(start_state, q)

def search(start_state, to_visit):
    to_visit.add(start_state)

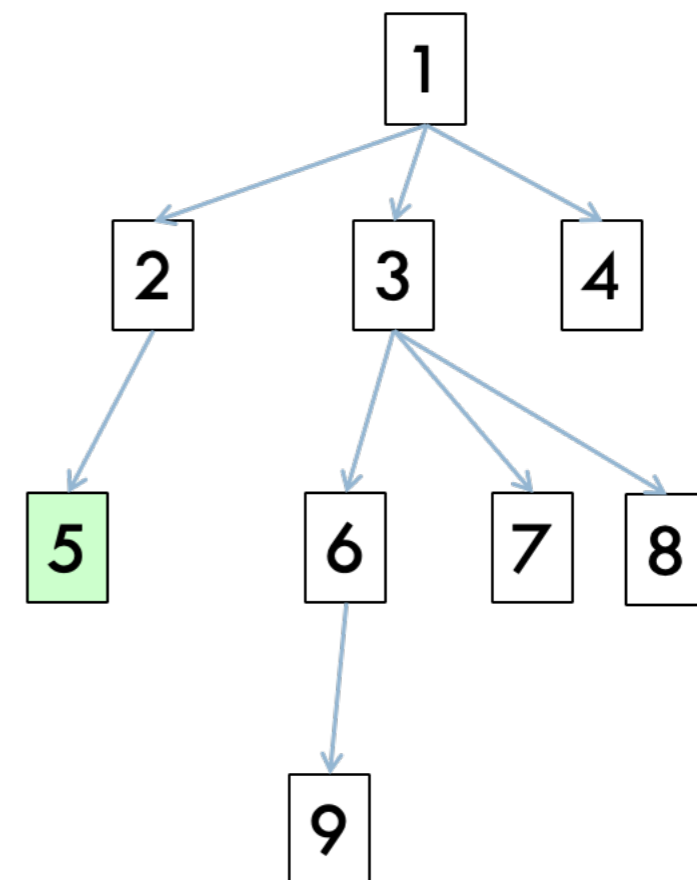
    while not to_visit.is_empty():
        current = to_visit.remove()

        if current.is_goal():
            return current
        else:
            for s in current.next_states():
                to_visit.add(s)

    return None
```

In what order would this variant visit the states?

```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```

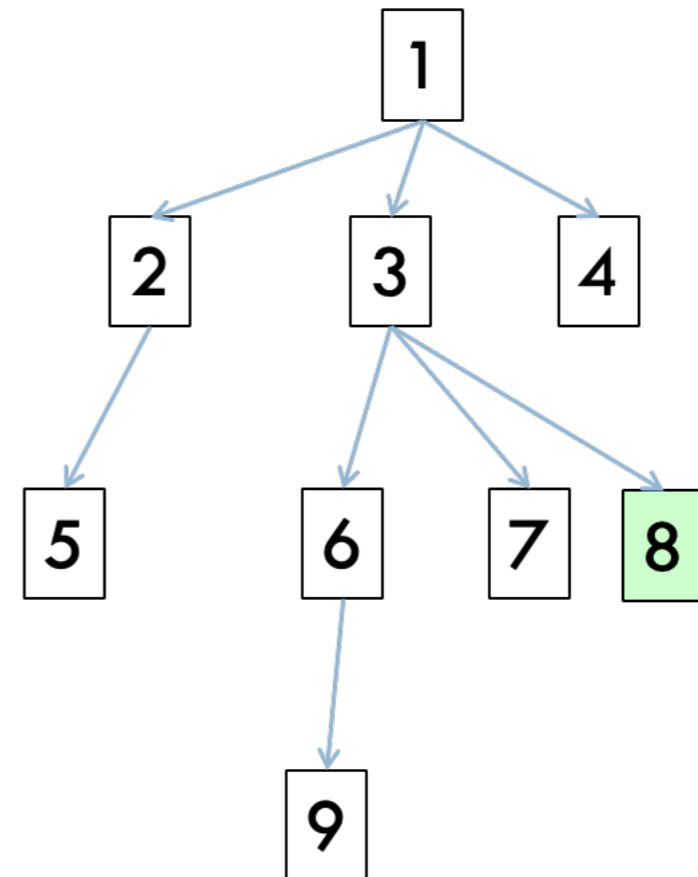


- ▶ Order: 1, 2, 5



In what order would this variant visit the states?

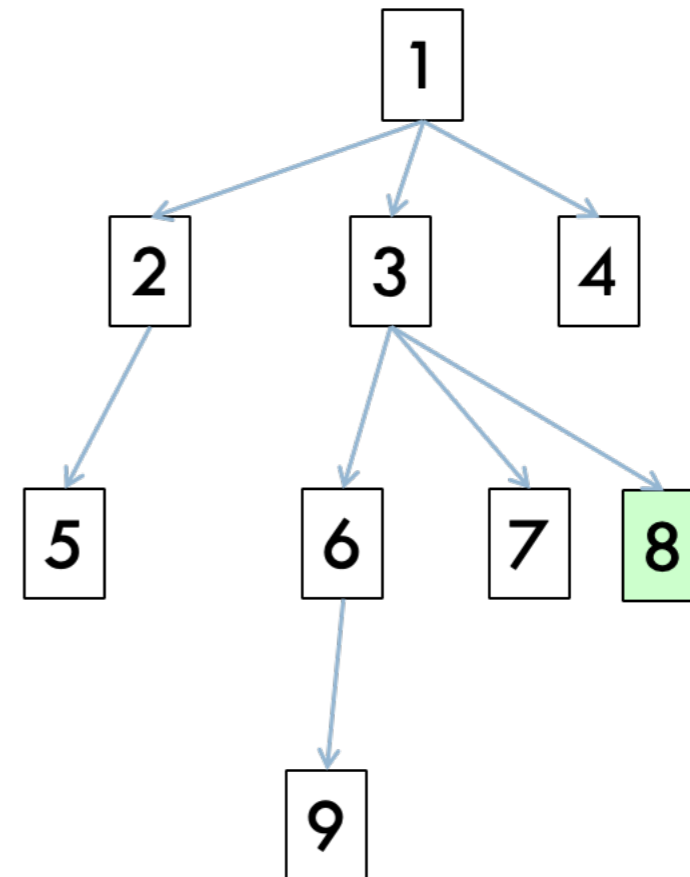
```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```



- ▶ Order: 1, 2, 5, 3, 6, 9, 7, 8

In what order would this variant visit the states?

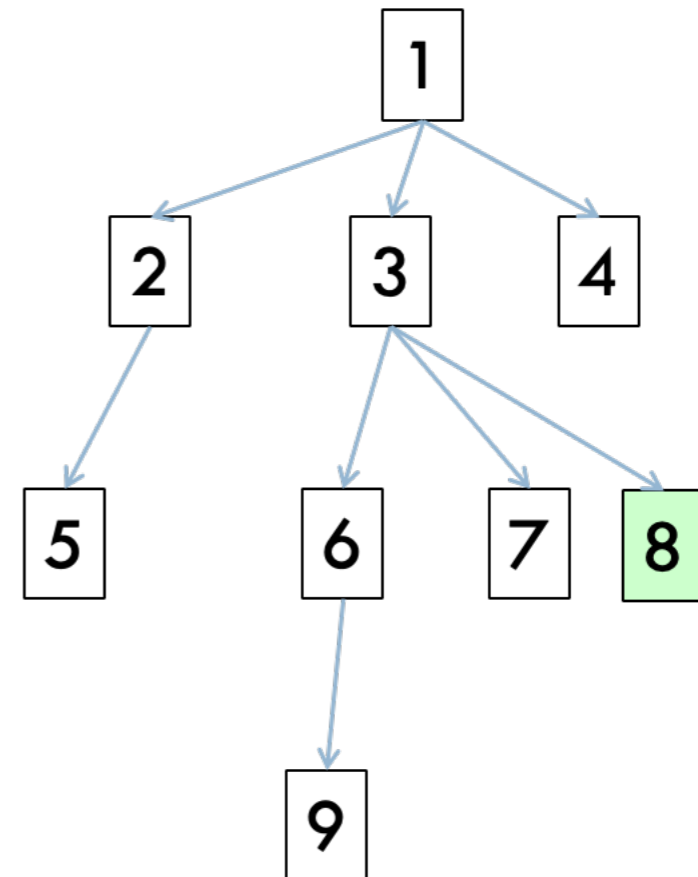
```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```



- ▶ Order: 1, 2, 5, 3, 6, 9, 7, 8
- ▶ What search algorithm is this?

In what order would this variant visit the states?

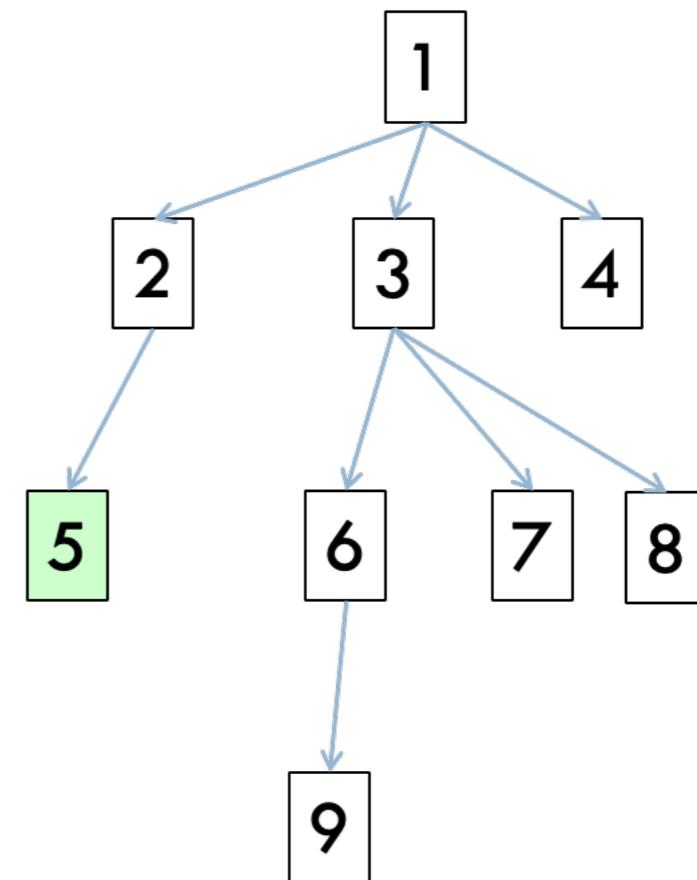
```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```



- ▶ Order: 1, 2, 5, 3, 6, 9, 7, 8
- ▶ DFS!

## DFS with a stack

```
def dfs(start_state):  
    s = Stack()  
    return search(start_state, s)  
  
def search(start_state, to_visit):  
    to_visit.add(start_state)  
  
    while not to_visit.is_empty():  
        current = to_visit.remove()  
  
        if current.is_goal():  
            return current  
        else:  
            for s in current.next_states():  
                to_visit.add(s)  
  
    return None
```

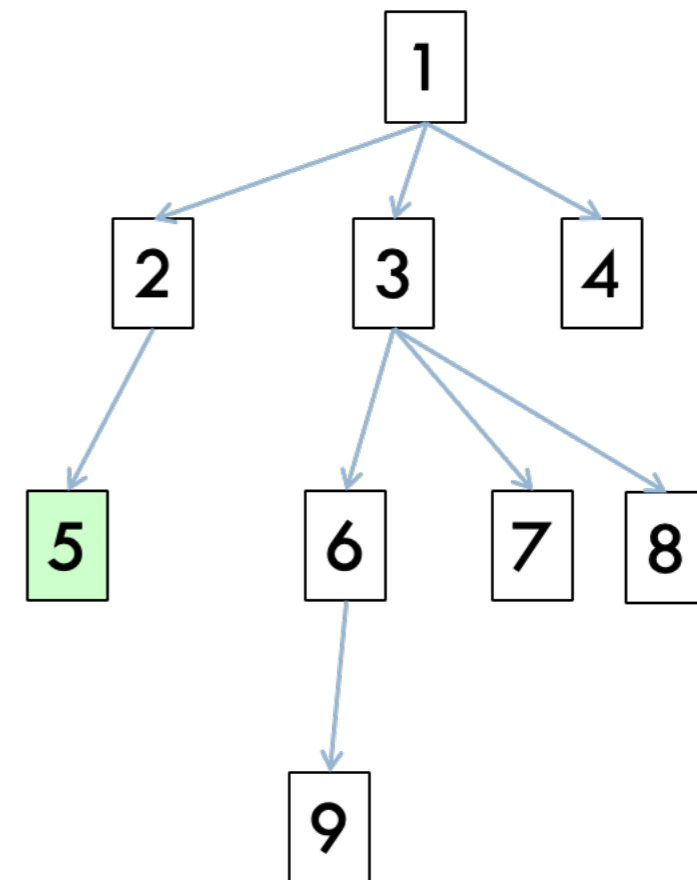


- ▶ Order: 1, 4, 3, 8, 7, 6, 9, 2, 5

## One last DFS variant

```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```

```
def dfs(state):  
    if state.is_goal():  
        return [state]  
    else:  
        result = []  
        for s in state.next_states():  
            result += dfs(s)  
        return result
```

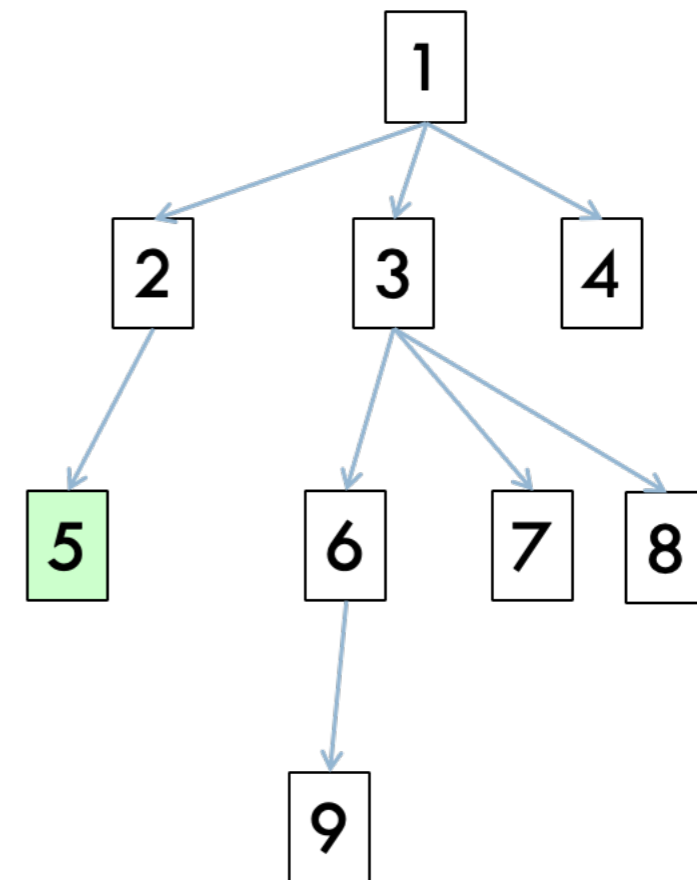


- ▶ How is this different?

## One last DFS variant

```
def search(state):  
    if state.is_goal():  
        return state  
    else:  
        for s in state.next_states():  
            result = search(s)  
            if result != None:  
                return result  
        return None
```

```
def dfs(state):  
    if state.is_goal():  
        return [state]  
    else:  
        result = []  
        for s in state.next_states():  
            result += dfs(s)  
        return result
```



- ▶ Return ALL solutions found, not just one.

## Lecture 18: Problem solving via search and matrices

- ▶ Problem solving via search
- ▶ **Matrices**
- ▶ Assignment 9

# What is a matrix?

- ▶ A matrix is a two-dimensional structure, e.g.,

0 1 0

1 8 2

5 0 3

- ▶ It has rows and columns.

- ▶ The second row is: 1 8 2

- ▶ The second column is:

1

8

0

- ▶ Since we are computer scientists, we'll start indexing at 0. That means that the first row is row 0 and the first column is column 0.



# Indexing into matrices

- ▶ Individual entries in a matrix can be references by specifying a row and a column.
- ▶ 
$$\begin{matrix} 0 & 1 & 0 \\ 1 & 8 & 2 \\ 5 & 0 & 3 \end{matrix}$$
- ▶ Let's say that the matrix above is called  $m$ , what entry does  $m[1][2]$  represent?
  - ▶ In math, we might write this as  $m(1, 2)$ .
  - ▶ 1 = second row, 2 = third column, that is  $m[1][2]$  is 2.
- ▶ How would we get at the 3 in the above matrix?
  - ▶  $m[2][2]$

## Implementing matrices in Python

- ▶ We can use lists of lists!

```
>>> m = [[0, 1, 0], [1, 8, 2], [5, 0, 3]]
```

```
>>> m
```

```
[[0, 1, 0], [1, 8, 2], [5, 0, 3]]
```

```
>>> m[1][2]
```

```
2
```

```
>>> m[2][2]
```

```
3
```

- ▶ Could also have constructed this as:

```
>>> m = []
```

```
>>> m.append([0, 1, 0])
```

```
>>> m.append([1, 8, 2])
```

```
>>> m.append([5, 0, 3])
```

```
>>> m
```

```
[[0, 1, 0], [1, 8, 2], [5, 0, 3]]
```

```
>>> m[1][2]
```

```
2
```

```
>>> m[2][2]
```

```
3
```

# Implementing matrices in Python

- ▶ what does `m[1]` represent?
  - ▶ the second row!

```
>>> m[1]  
[1, 8, 2]
```

- ▶ matrices are just lists of lists.

### matrix.py

- ▶ what do `zero_matrix` and `zero_matrix2` do?
  - ▶ They both create a `size x size` matrix with all entries zero.
  - ▶ `zero_matrix` does this an entry at a time.
  - ▶ `zero_matrix2` does this a row at a time.

```
>>> zero_matrix(3)
[[0, 0, 0], [0, 0, 0], [0, 0, 0]]
>>> zero_matrix2(2)
[[0, 0], [0, 0]]
>>> zero_matrix(1)
[[0]]
>>> m = zero_matrix(2)
>>> m
[[0, 0], [0, 0]]
>>> m[1][1] = 100
>>> m
[[0, 0], [0, 100]]
```

### matrix.py

- ▶ what does `random_matrix` do?
  - ▶ It creates a `size x size` matrix with random ints between 0 and `size x size`

```
>>> random_matrix(3)
[[6, 2, 1], [2, 6, 1], [0, 3, 9]]
>>> random_matrix(3)
[[5, 3, 9], [7, 4, 1], [8, 2, 3]]
>>> random_matrix(3)
[[6, 9, 7], [8, 4, 7], [1, 6, 5]]
```

## matrix.py

- ▶ How would we print out a matrix in a more normal form (one row at a time)?
  - ▶ iterate through the rows and print each out.
  - ▶ Look at the `print_matrix` and `print_matrix2` function.
- ▶ What does the `identity` function do?
  - ▶ It creates an identity size by size matrix with all zeros except for ones along the diagonal
- ▶ How would we sum up all the numbers in a matrix?
  - ▶ Iterate over each entry and add them up
  - ▶ Look at the `matrix_sum` function.
  - ▶ What does `len(m)` give us?
    - ▶ the number of rows (remember, list of lists)
  - ▶ what does `len(m[row])` give us?
    - ▶ the number of columns (in that row, technically)
  - ▶ Look at the `matrix_sum2` and `matrix_sum3` functions.
    - ▶ They use the `sum` function to sum up each row and then add that to the total.

### copying matrices

- ▶ Be careful when you want to create a deep copy of a matrix. See the code below. What's the problem?

```
>>> m = [[1, 2], [3, 4]]
```

```
>>> n = m[:]
```

```
>>> n[0][0] = 0
```

```
>>> n
```

```
[[0, 2], [3, 4]]
```

```
>>> m
```

```
[[0, 2], [3, 4]]
```

### copying matrices

- ▶ If you want to copy a matrix and avoid aliasing issues, you should either:
  - ▶ use the copy module  
`import copy`  
`copy.deepcopy(m)`
  - ▶ or by creating a deep copy of each row and appending it to a new list.

```
>>> m = [[1, 2], [3, 4]]
>>> n = []
>>> for row in m:
...     n.append(row[:])
...
>>> n
[[1, 2], [3, 4]]
>>> n[0][0] = 0
>>> n
[[0, 2], [3, 4]]
>>> m
[[1, 2], [3, 4]]
```



### `tic_tac_toe.py`

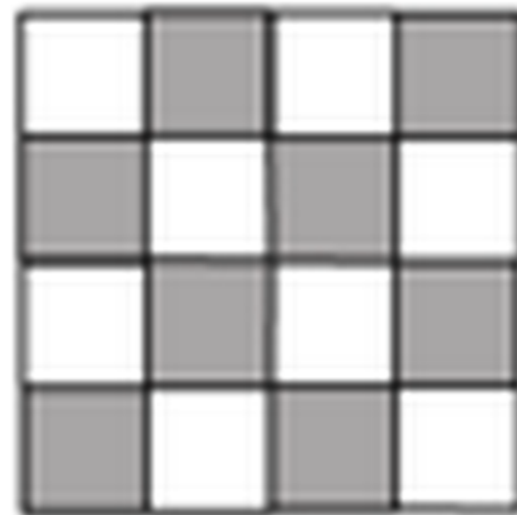
- ▶ How would you represent a tic tac toe board?
  - ▶ As a 3 by 3 matrix.
  - ▶ Each entry has one of three values:
    - ▶ empty
    - ▶ X
    - ▶ O

## Lecture 18: Problem solving via search and matrices

- ▶ Problem solving via search
- ▶ Matrices
- ▶ Assignment 9

### N-queens problem

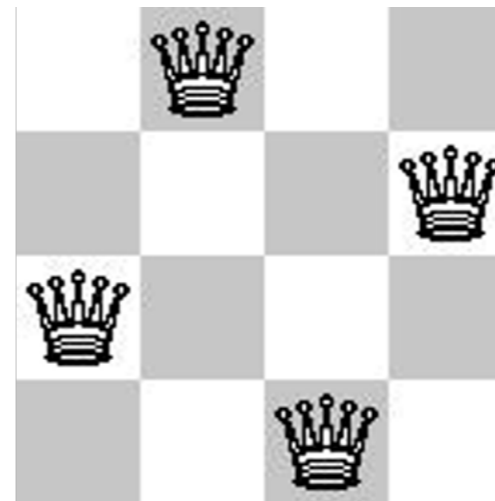
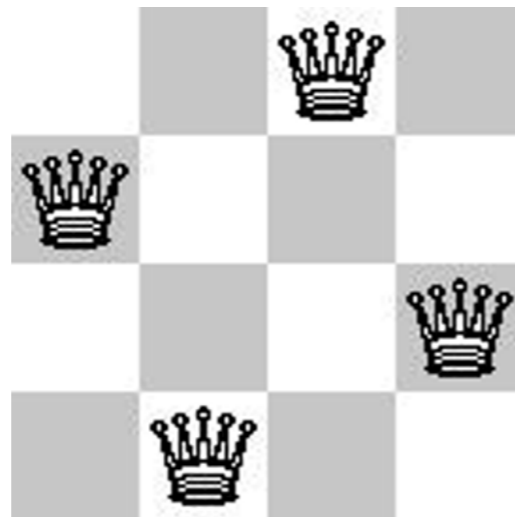
- ▶ Place  $N$  queens on an  $N$  by  $N$  chess board such that none of the  $N$  queens are attacking any other queen.



Solution(s)?

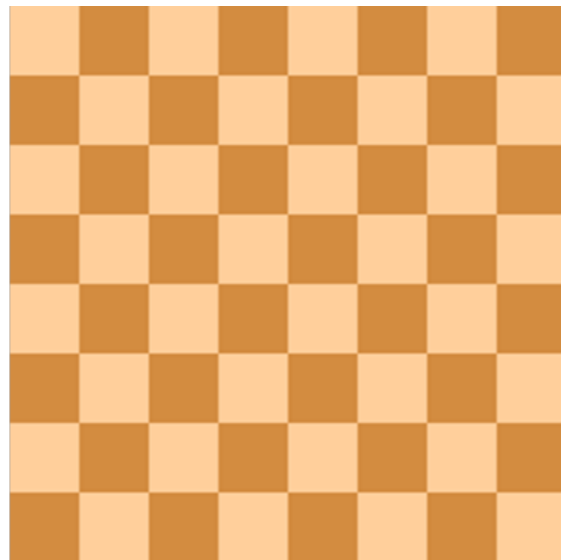
# N-queens problem

- ▶ Place  $N$  queens on an  $N$  by  $N$  chess board such that none of the  $N$  queens are attacking any other queen.



### N-queens problem

- ▶ Place  $N$  queens on an  $N$  by  $N$  chess board such that none of the  $N$  queens are attacking any other queen.



Solution(s)?

### N-queens problem

- ▶ Place  $N$  queens on an  $N$  by  $N$  chess board such that none of the  $N$  queens are attacking any other queen.
- ▶ How do we solve this with search:
  - ▶ What is a state?
  - ▶ What is the start state?
  - ▶ What is the goal?
  - ▶ How do we transition from one state to the next?

# Search algorithm

- ▶ add the **start state** to to\_visit
- ▶ Repeat
  - ▶ take a state off the to\_visit list
  - ▶ **if it's the goal state** **Is this a goal state?**
    - ▶ we're done!
  - ▶ if it's not the goal state **What states can I get to from the current state?**
    - ▶ Add all of the **next possible states** to the to\_visit list
- ▶ *Any problem that we can define these three things can be plugged into the search algorithm!*

## Resources

- ▶ [search\\_variants.py](#)
- ▶ [matrix.py](#)
- ▶ [tic\\_tac\\_toe.py](#)
- ▶ [https://en.wikipedia.org/wiki/Eight\\_queens\\_puzzle](https://en.wikipedia.org/wiki/Eight_queens_puzzle)

## Homework

- ▶ [Assignment 9](#)