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| Admin |
| :--- |
| Assignment 8 out: don't reinvent the wheel |
| Assignment schedule updated for the rest of the |
| semester |
| Groups optional this week |




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Strongly connected

Strongly-Connected(G)

- Run DFS-Visit or BFS from some node u
- If not all nodes are visited: return false
- Create graph $\mathrm{G}^{\mathrm{R}}$
- Run DFS-Visit or BFS on $G^{R}$ from node $u$
- If not all nodes are visited: return false
- return true


Runtime?

Strongly-Connected (G)

- Run DFS-Visit or BFS from some node u O(|V|+|E|)
- Run DFS-Visit or BFS from some node $u$ O(IV
- If not all nodes are visited: return false
O(IV)
$\begin{array}{ll}\text { - If not all nodes are visited: return false } & O(|V|) \\ \text { - Create graph } \mathrm{G}^{\mathrm{R}} & \theta(|\mathrm{V}|+\mid \mathrm{El})\end{array}$
- Run DFS-Visit or BFS on $\mathrm{G}^{R}$ from node $u \quad \begin{array}{ll}\quad(|V|+|E|) \\ O(V|+|E|)\end{array}$
- If not all nodes are visited: return false $\mathrm{O}(|\mathrm{V}|)$
- return true
$\mathrm{O}(|\mathrm{V}|+|\mathrm{E}|)$

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Minimum cut property
If the minimum cost edge that crosses the partition is not unique, then some minimum spanning tree contains edge $e$


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$T \leftarrow\left\}^{\operatorname{MakeSet}(v)}\right.$
4 sort the edges of $E$ by weight
for all edges $(u, v) \in E$ in increasing order of weight
add edge to $T$
add edge to $T$
Union $(\operatorname{Find}-\operatorname{SEt}(u), \operatorname{Find}-\operatorname{SET}(v))$
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Running time of Kruskal's
${ }_{\text {KRISKAL (G) }}^{1}$
${ }_{2}^{1}$ for all $v \in V \quad \operatorname{MAKESET}(v)$
$\begin{array}{ll}1 \\ 3 & T \leftarrow 6 \\ 4 & \text { sort the }\end{array}$
sort the edges of $E$ by weight
for all edpes $(u, v) \in E$ in incre
Sor all edges of $(u, v) \in E$ in in increasing order of weight
if $\mathrm{F} w \mathrm{~S}$
if Find-SET(u) $\begin{gathered}\text { ando-SET }(v) \\ \text { add edge to } T\end{gathered}$
add edge to $T$
UNion $(\operatorname{Find}-\operatorname{SET}(u), \operatorname{Fndo}-\operatorname{Set}(v)$


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Correctness of Prim's?
Can we use the min-cut property?

- Given a partion S let edge e be the minimum cost edge that crosses the
partition. Every mininum spanning tree contains edge e.
Let $S$ be the set of vertices visited so far
The only time we add a new edge is if it's the lowest weight edge
from $S$ to $V-S$



