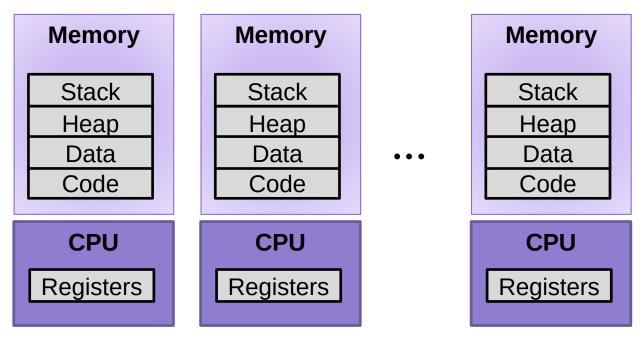
### Lecture 16: Virtual Memory

CS 105 Spring 2025

# Multiprocessing: The Illusion

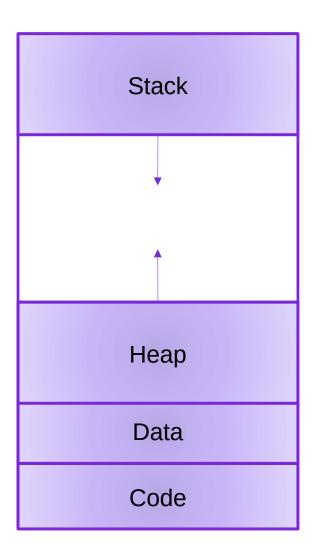


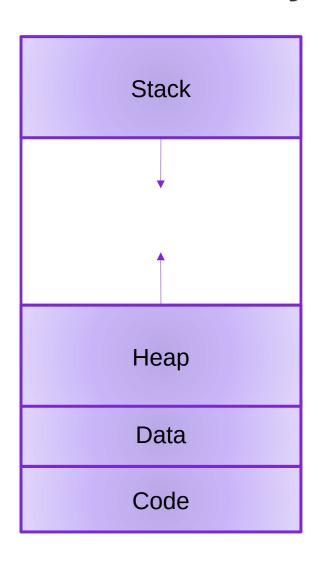
- Process provides each program with two key abstractions:
  - Logical control flow
    - Each program seems to have exclusive use of the CPU
    - Provided by kernel mechanism called context switching
  - Private address space
    - Each program seems to have exclusive use of main memory.
    - Provided by kernel mechanism called virtual memory

## Multiprocessing: The Reality

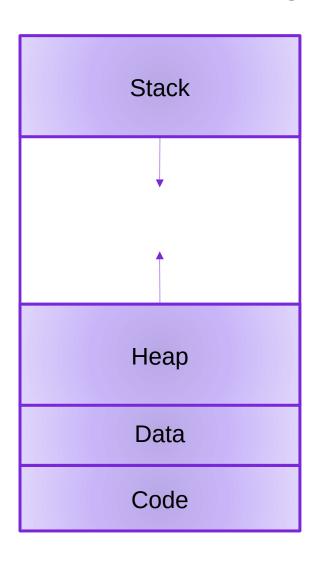
- Computer runs many processes simultaneously
- Running program "top" on Linux/Mac
  - E.g., system has 558 processes, 2 of which are active
  - Identified by Process ID (PID)

top - 11:35:22 up 3:38, 1 user, load average: 1.11, 0.68, 1.10 Tasks: 560 total, 2 running, 558 sleeping, 0 stopped, 0 zombie %Cpu(s): 0.4 us, 1.5 sy, 0.8 ni, 97.3 id, 0.0 wa, 0.0 hi, 0.0 si, 0.0 st

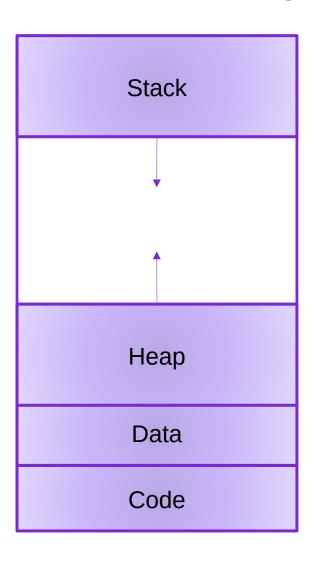




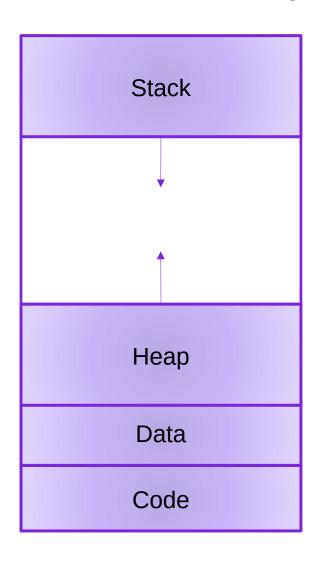
 Isolation: don't want different process states collided in physical memory



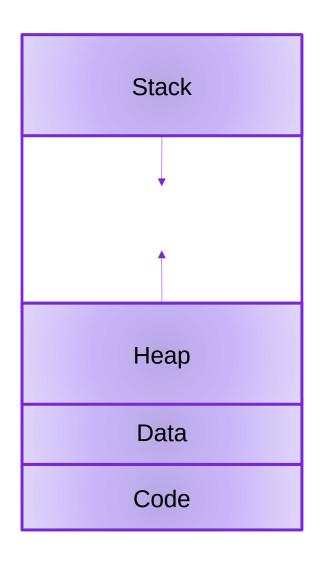
- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory



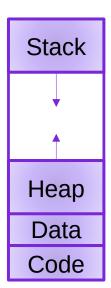
- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
- Sharing: want option to overlap for communication



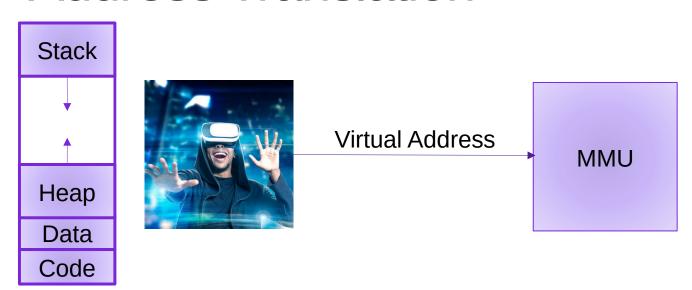
- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
- Sharing: want option to overlap for communication
- Utilization: want best use of limited resource

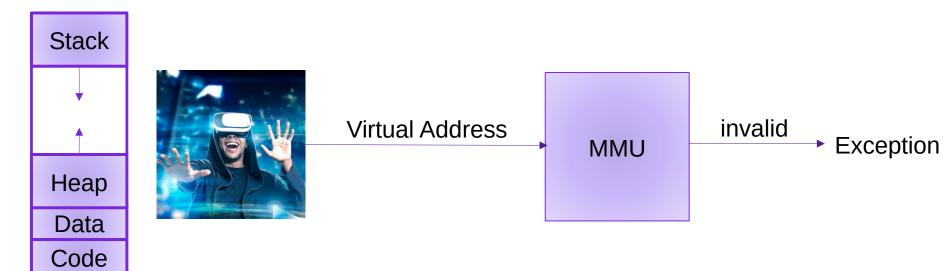


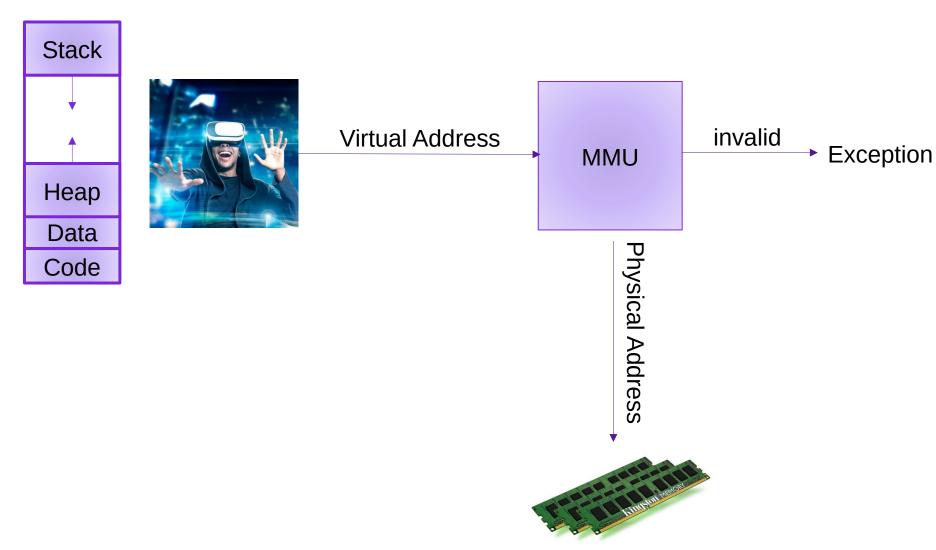
- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
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- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources

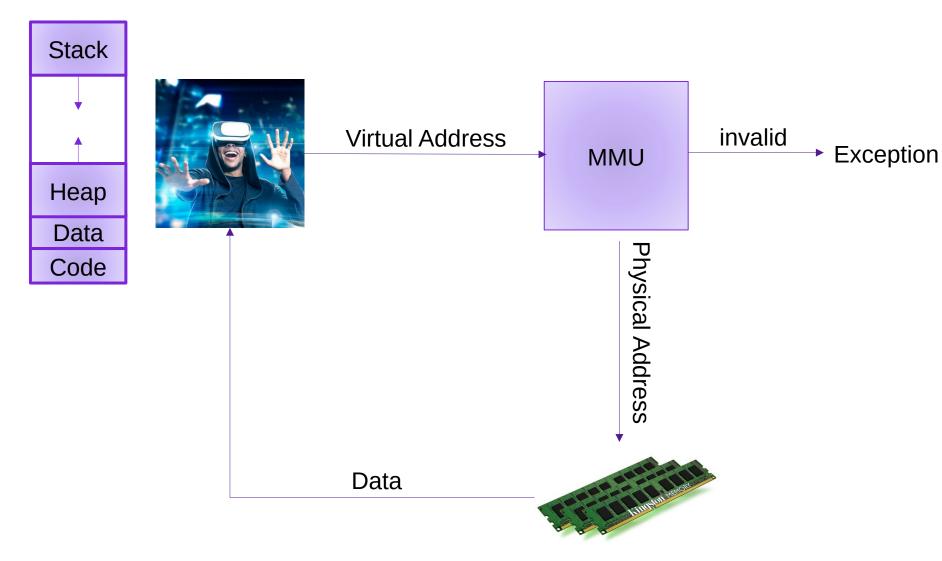


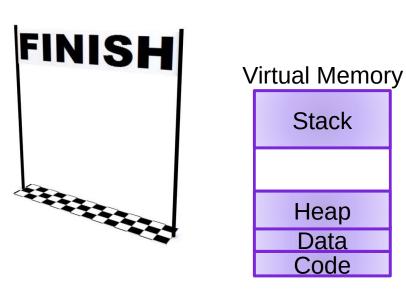




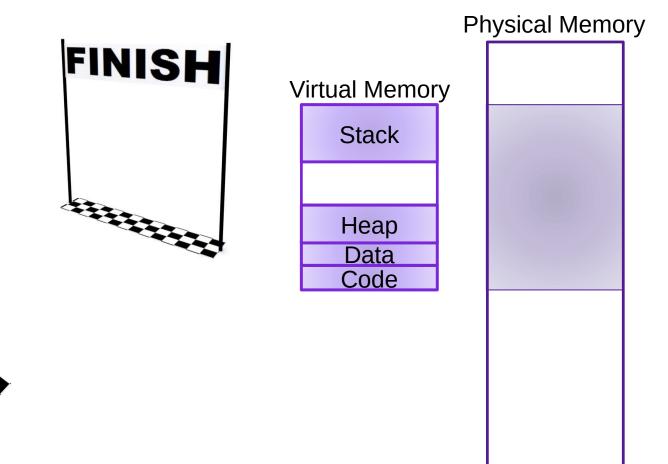


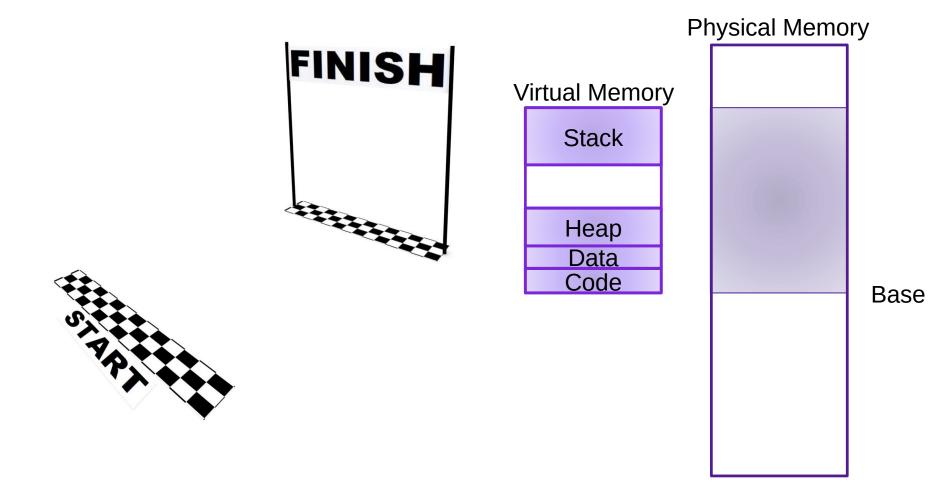


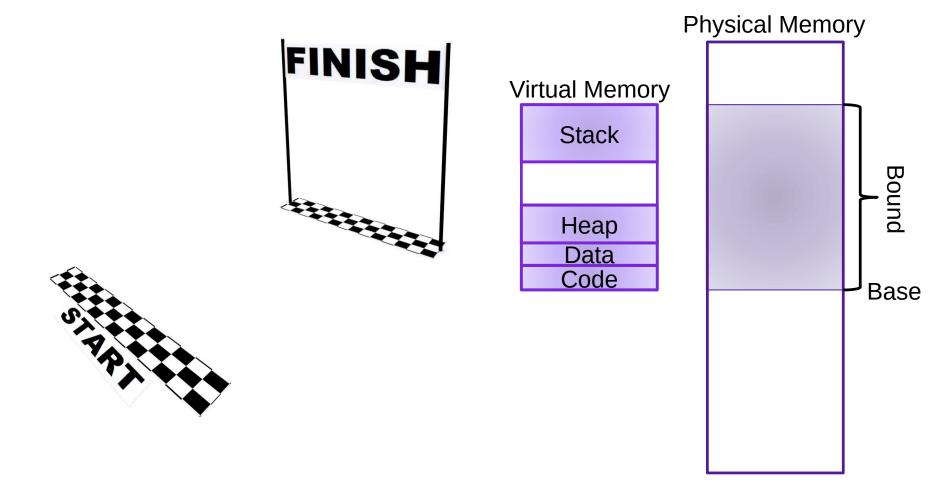


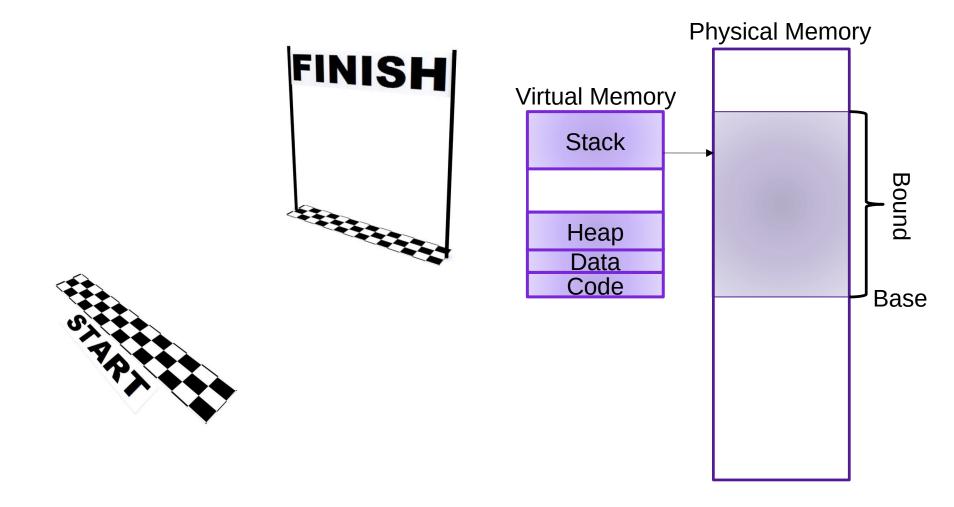


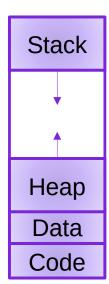
**Physical Memory** 



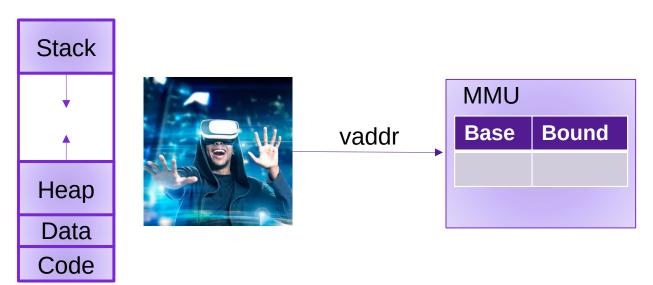


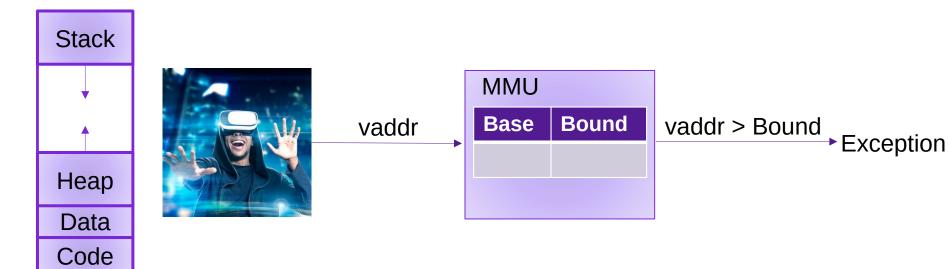


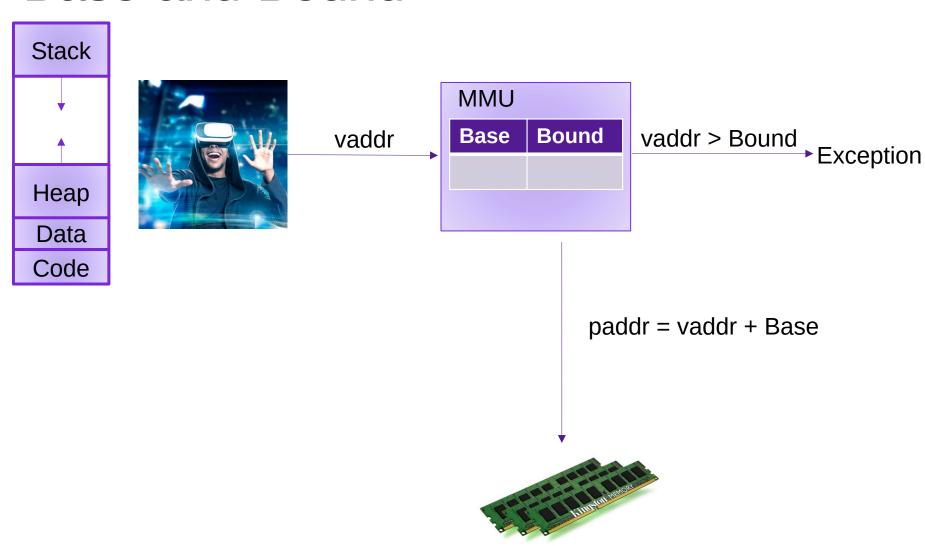


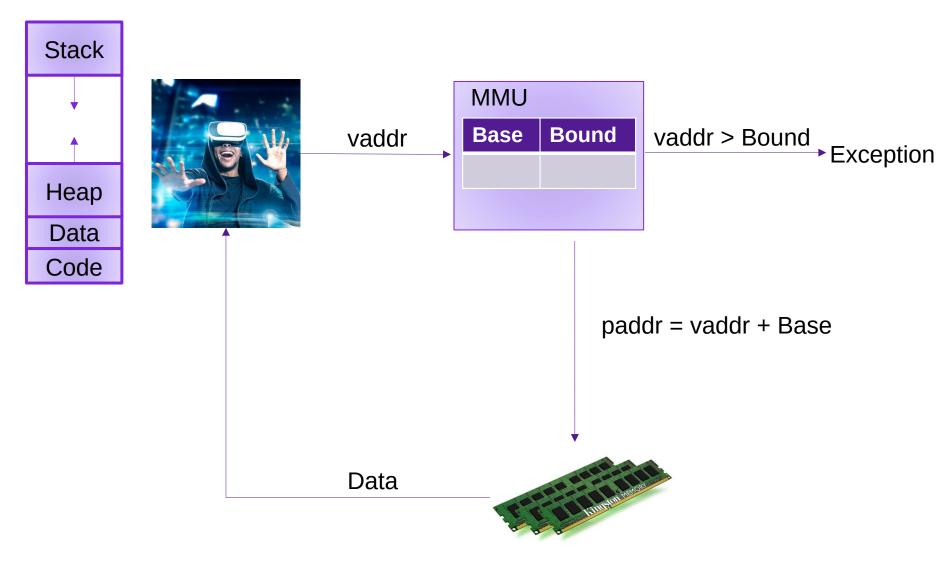












#### Exercise 1: Base-and-Bound

Assume that you are currently executing a process P with Base 0x1234 and Bound 0x100.

- What is the physical address that corresponds to the virtual address 0x47?
- What is the physical address that corresponds to the virtual address 0x123?

#### Exercise 1: Base-and-Bound

Assume that you are currently executing a process P with Base 0x1234 and Bound 0x100.

- What is the physical address that corresponds to the virtual address 0x47? 0x127b
- What is the physical address that corresponds to the virtual address 0x123?

#### Exercise 1: Base-and-Bound

Assume that you are currently executing a process P with Base 0x1234 and Bound 0x100.

- What is the physical address that corresponds to the virtual address 0x47? 0x127b
- What is the physical address that corresponds to the virtual address 0x123? invalid



- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
- Sharing: want option to overlap for communication
- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources

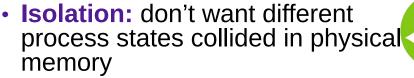




- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
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- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources









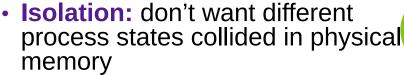
 Efficiency: want fast reads/writes to memory



- Sharing: want option to overlap for communication
- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources









 Efficiency: want fast reads/writes to memory



 Sharing: want option to overlap for communication



- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources





 Isolation: don't want different process states collided in physical memory



 Efficiency: want fast reads/writes to memory



 Sharing: want option to overlap for communication



 Utilization: want best use of limited resource



Virtualization: want to create illusion of more resources





 Isolation: don't want different process states collided in physical memory



 Efficiency: want fast reads/writes to memory



 Sharing: want option to overlap for communication



 Utilization: want best use of limited resource

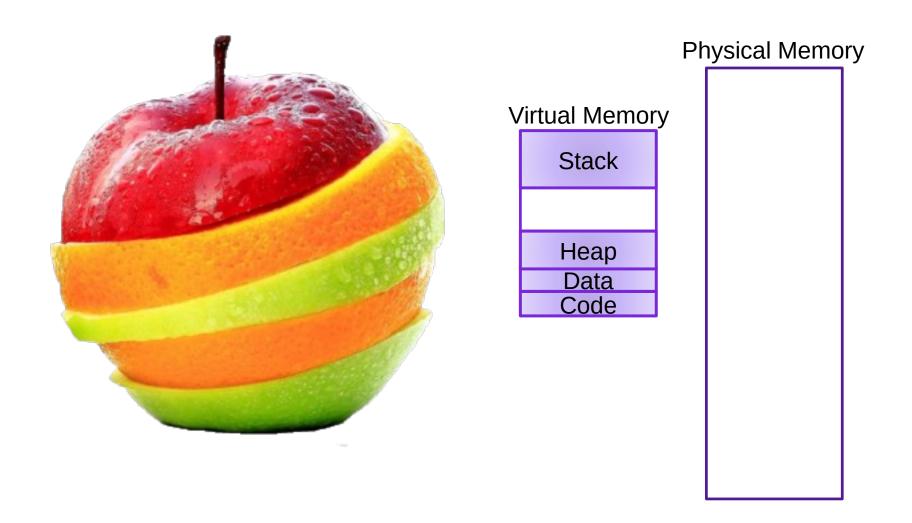


Virtualization: want to create illusion of more resources

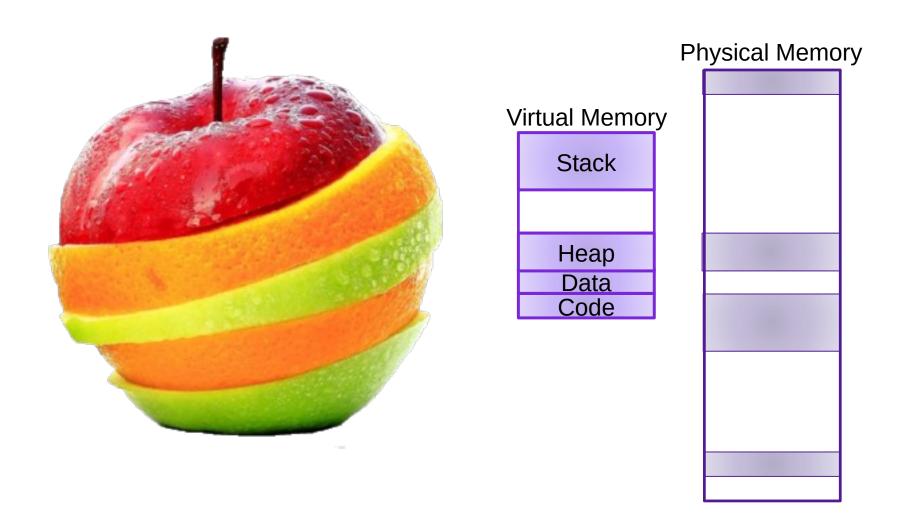




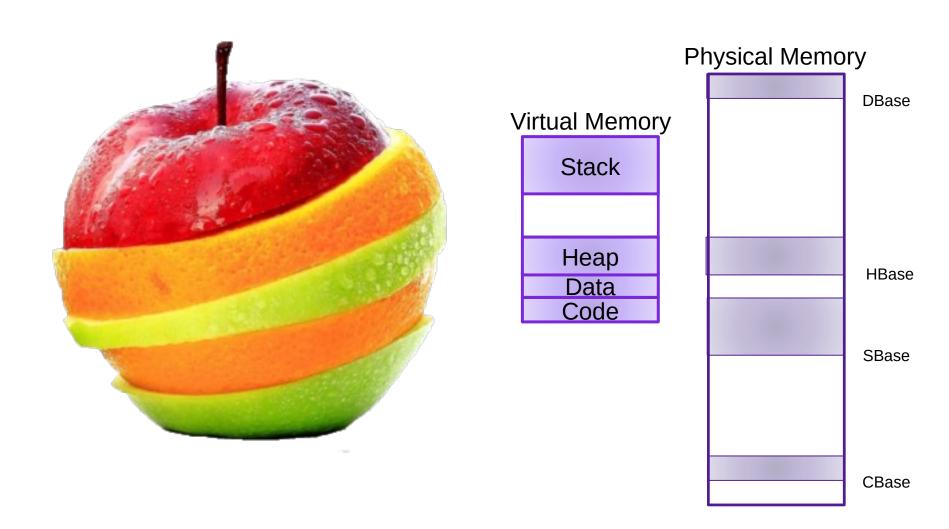
# Segmentation

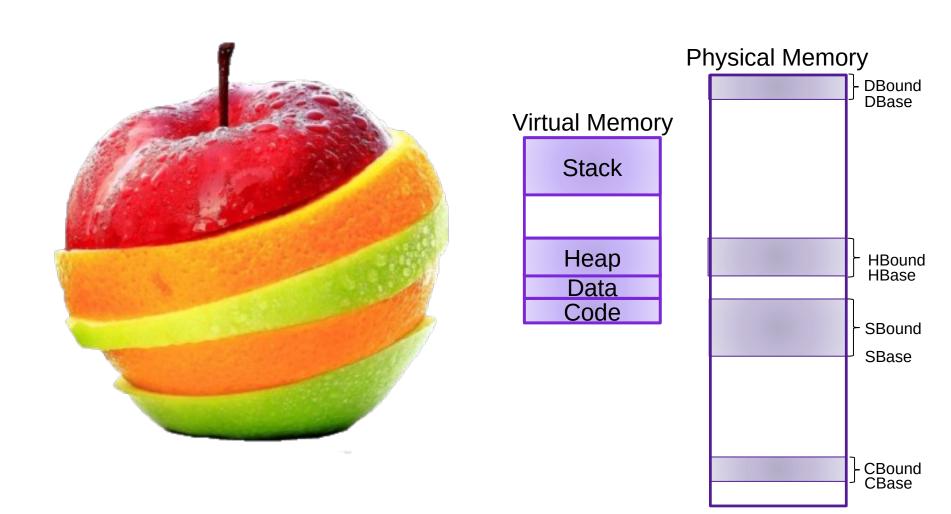


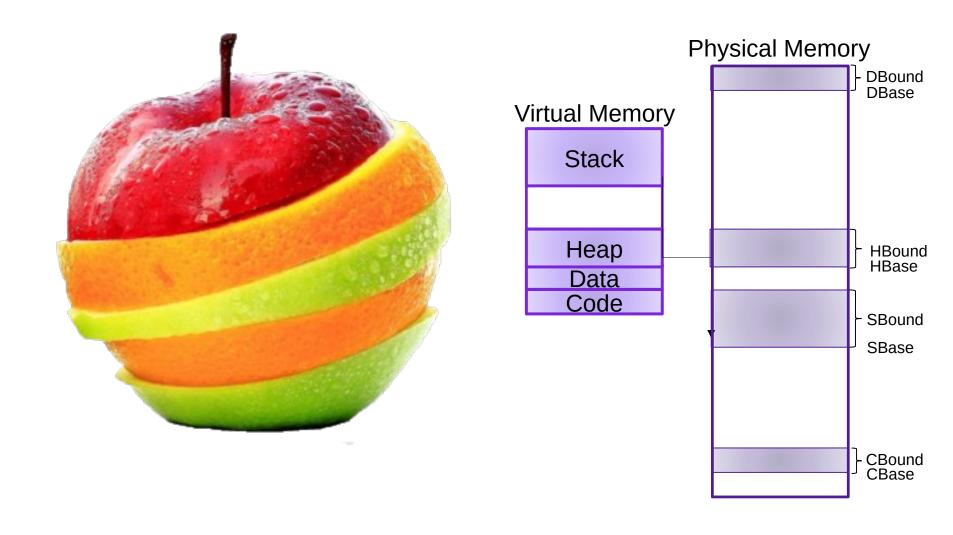
# Segmentation

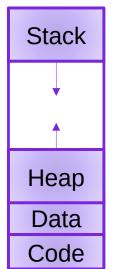


# Segmentation

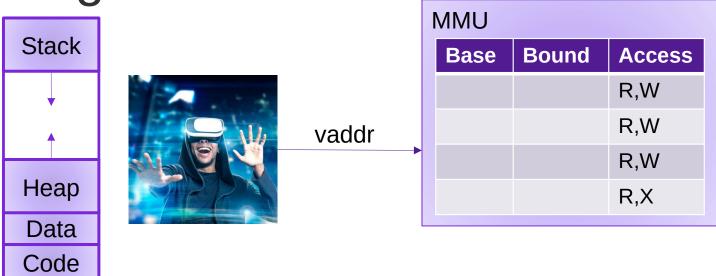


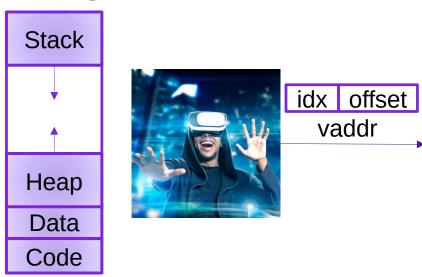




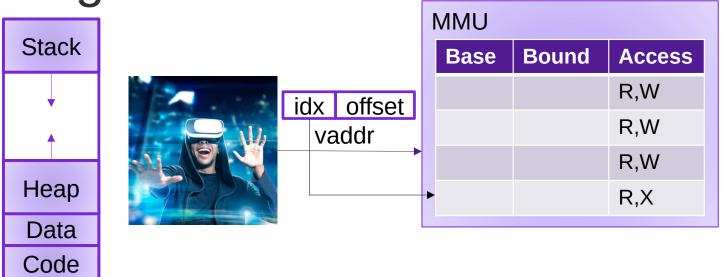








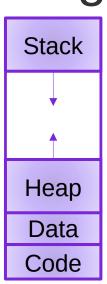
MMU		
Base	Bound	Access
		R,W
		R,W
		R,W
		R,X

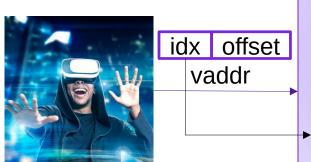




	MMU		
	Base	Bound	Access
			R,W
			R,W
			R,W
<b>•</b>			R,X

offset > Bound[idx] X or access not allowed ption



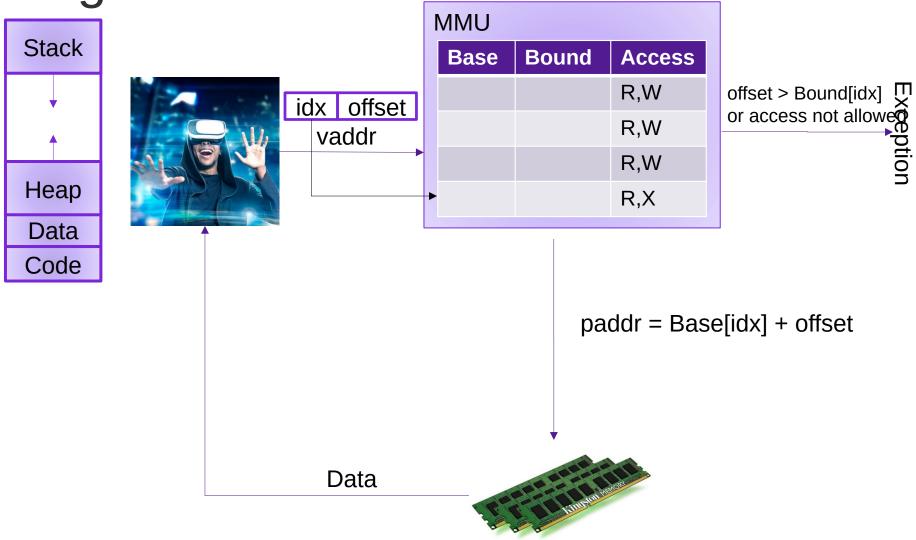


IVI	IVIU		
	3ase	Bound	Access
			R,W
			R,W
			R,W
•			R,X

11111

offset > Bound[idx] The or access not allowed by the one of the or access of the or access not allowed by the or access not allowed





Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001?
- What is the physical address that corresponds to the virtual address 0xD47?

Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001?
- What is the physical address that corresponds to the virtual address 0xD47?

Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001? 0000000001
- What is the physical address that corresponds to the virtual address 0xD47?

Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001? 0000000001 0x4748
- What is the physical address that corresponds to the virtual address 0xD47?

Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001? 0000000001 0x4748
- What is the physical address that corresponds to the virtual address 0xD47? 11 0101000111

Base	Bound	Access
0x4747	0x80	R,W
0x2424	0x40	R,W
0x0023	0x80	R,W
0x1000	0x200	R,X

- What is the physical address that corresponds to the virtual address 0x001? 0000000001 0x4748
- What is the physical address that corresponds to the virtual address 0xD47? 11 0101000111 0x1147



- Isolation: don't want different process states collided in physical memory
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 Efficiency: want fast reads/writes to memory



 Sharing: want option to overlap for communication



 Utilization: want best use of limited resource



Virtualization: want to create illusion of more resources





**Physical Memory** 

Virtual Memory

Stack

Неар

Data

Code

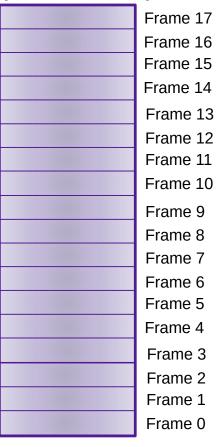


#### Virtual Memory

Stack

Heap Data Code

#### **Physical Memory**

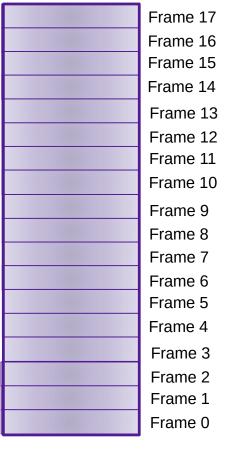




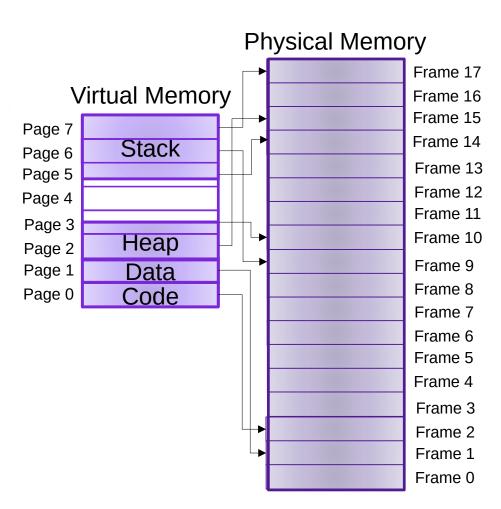
#### Virtual Memory

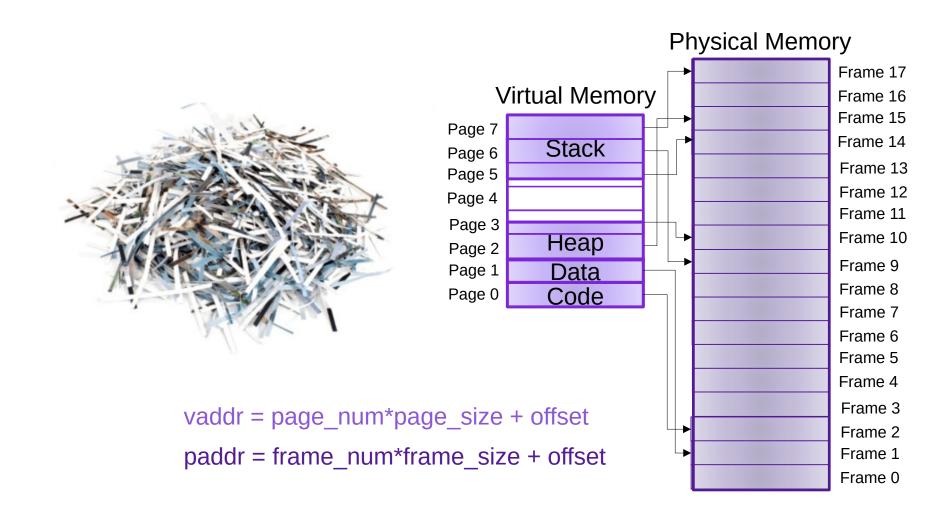
Page 7	
Page 6	Stack
Page 5	
Page 4	
Page 3	
Page 2	Неар
Page 1	Data
Page 0	Code

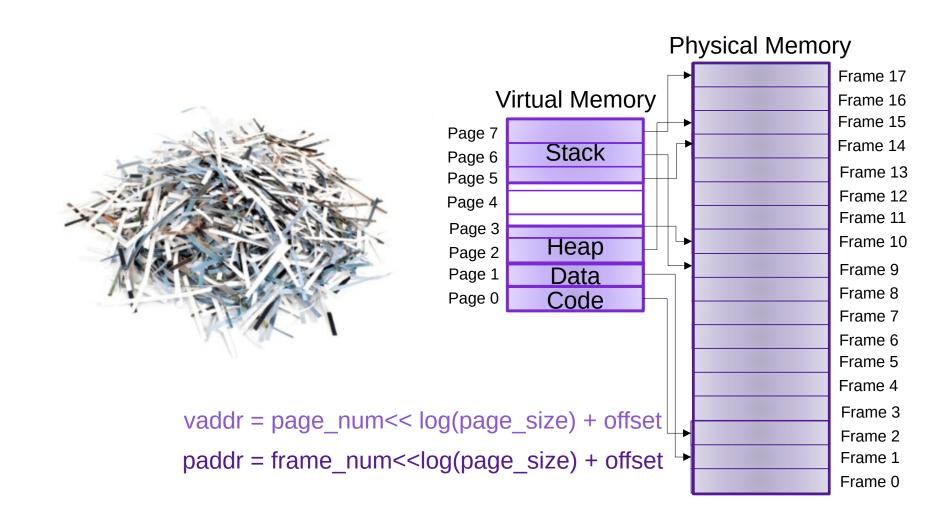
#### **Physical Memory**

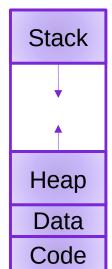




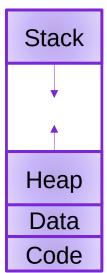








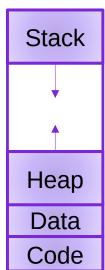






vaddr

MMU		
Frame	Access	
47	R,W	
NULL	R,W	
13	R,W	
42	R,X	

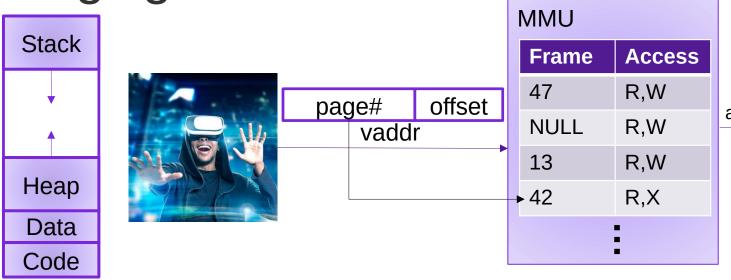




page#	offset
vadd	r

MMU		
Frame	Access	
47	R,W	
NULL	R,W	
13	R,W	
42	R,X	

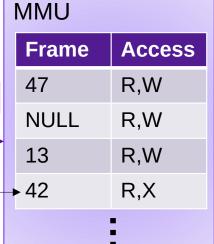




access not allowed coption

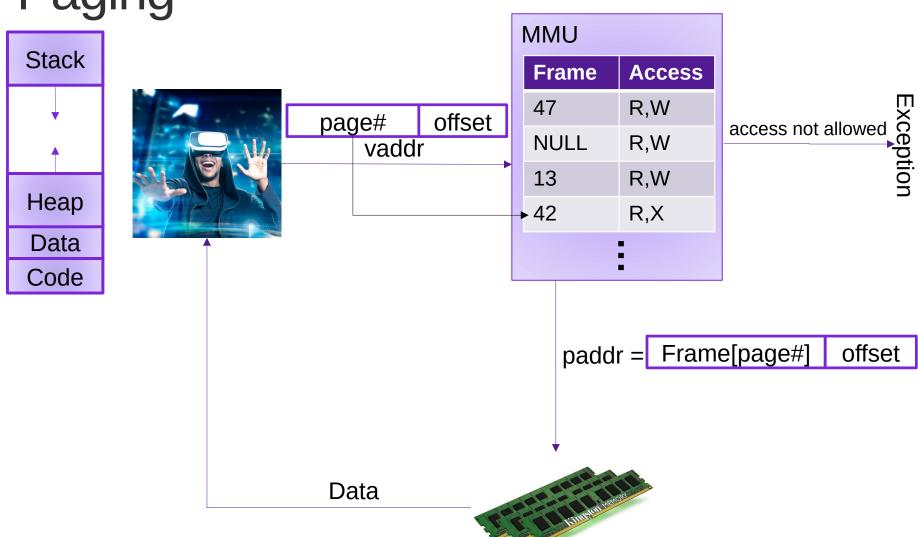






access not allowed ption





# Exercise 3: Paging

Assume that you are currently executing a process P with the following page table on a system with 16 byte pages:

Frame	Access
0x47	R,W
0xF4	R,W
NULL	R,W
0x23	R,X
	0x47 0xF4 NULL

- What is the physical address that corresponds to the virtual address 0x147?
- What is the physical address that corresponds to the virtual address 0x16E?

# Exercise 3: Paging

Assume that you are currently executing a process P with the following page table on a system with 16 byte pages:

<b>U</b> . <b>U</b>		
÷	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
-		

- What is the physical address that corresponds to the virtual address 0x147?
- What is the physical address that corresponds to the virtual address 0x16E?

_		
:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
_		

- What is the physical address that corresponds to the virtual address 0x147? 00010100 0111
- What is the physical address that corresponds to the virtual address 0x16E?

:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X

- What is the physical address that corresponds to the virtual address 0x147? 00010100 0111 0x237
- What is the physical address that corresponds to the virtual address 0x16E?

÷	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
-		

- What is the physical address that corresponds to the virtual address 0x147? 00010100 0111 0x237
- What is the physical address that corresponds to the virtual address 0x16E? 00010110 1110

Frame Access	
0x17 0x47 R,W	
0x16 0xF4 R,W	
0x15 NULL R,W	
0x14 0x23 R,X	

- What is the physical address that corresponds to the virtual address 0x147? 00010100 0111 0x237
- What is the physical address that corresponds to the virtual address 0x16E? 00010110 1110 0xF4E

:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14		R,X
:		

Assume that you are currently executing a process P with the following page table on a system with 16 byte pages:

Physical Memory

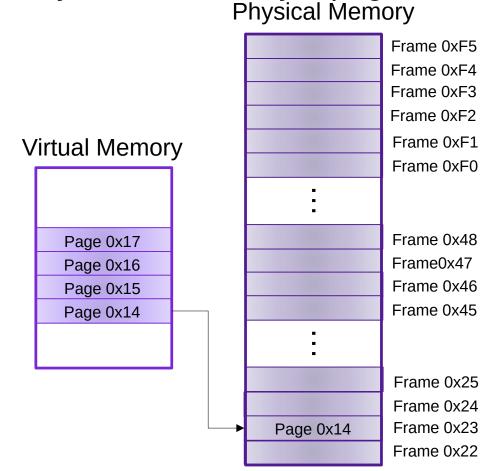
:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
:		

Virtual Memory

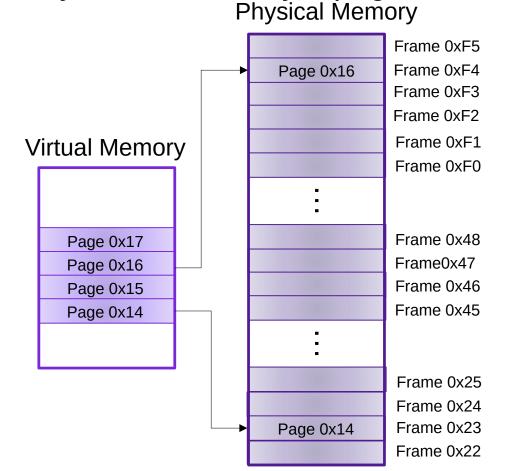
Page 0x17
Page 0x16
Page 0x15
Page 0x14

,	
	Frame 0xF5
	Frame 0xF4
	Frame 0xF3
	Frame 0xF2
	Frame 0xF1
	Frame 0xF0
:	
•	
	Frame 0x48
	Frame0x47
	Frame 0x46
	Frame 0x45
:	
-	
	Frame 0x25
	Frame 0x24
	Frame 0x23
	Frame 0x22

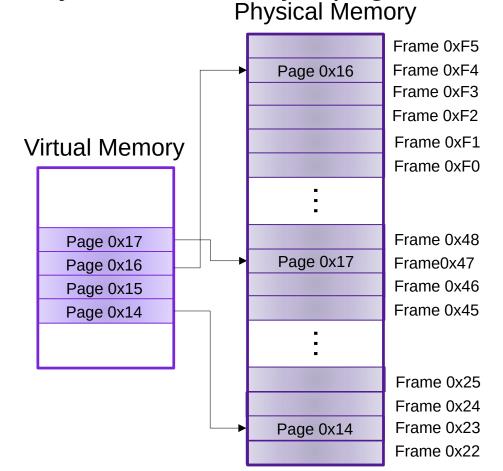
		<u> </u>
÷	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
:		



:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
÷		



:	Frame	Access
0x17	0x47	R,W
0x16	0xF4	R,W
0x15	NULL	R,W
0x14	0x23	R,X
:		



- each page table entry has a valid bit
- for valid entries, frame indicates physical address of page in memory
- a page fault occurs when a program requests a page that is not currently in memory
  - handled much like a cache miss

MMU		
V	Frame	Access
1	0x47	R,W
0	NULL	R,W
0	0x13	R,W
1	0xF1	R,X

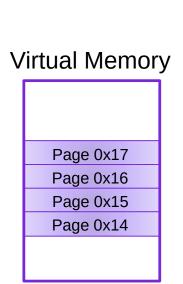
- each page table entry has a valid bit
- for valid entries, frame indicates physical address of page in memory
- a page fault occurs when a program requests a page that is not currently in memory
  - handled much like a cache miss
  - evict another page in memory to make space (which one?)

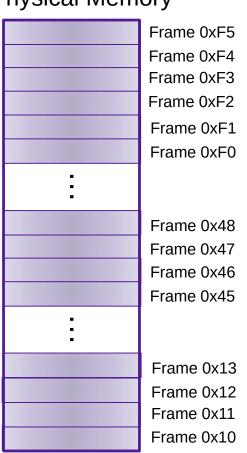
MMU		
V	Frame	Access
1	0x47	R,W
0	NULL	R,W
0	0x13	R,W
1	0xF1	R,X

- each page table entry has a valid bit
- for valid entries, frame indicates physical address of page in memory
- a page fault occurs when a program requests a page that is not currently in memory
  - handled much like a cache miss
  - evict another page in memory to make space (which one?)
  - takes time to handle, so context switch

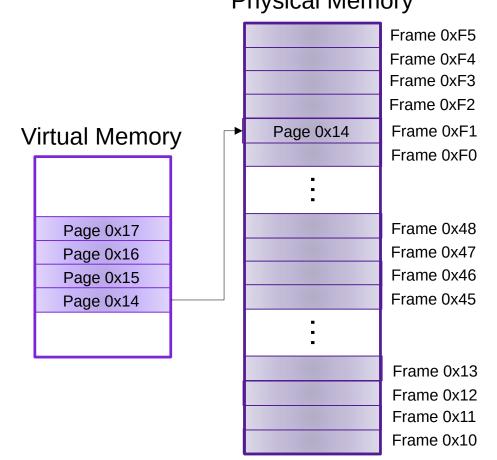
MMU					
V	Frame	Access			
1	0x47	R,W			
0	NULL	R,W			
0	0x13	R,W			
1	0xF1	R,X			

÷	V	Frame	Access
0x17	1	0x47	R,W
0x16	0	NULL	R,W
0x15	0	0x13	R,W
0x14	1	0xF1	R,X
:			

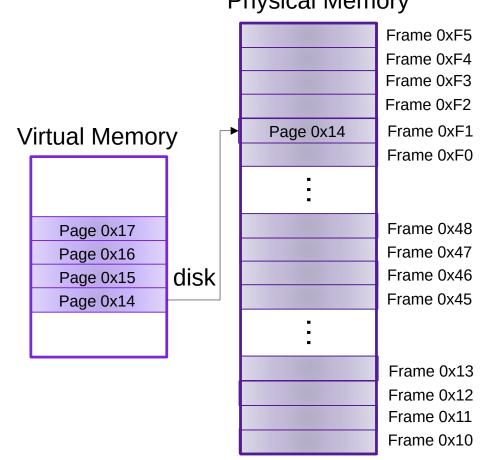




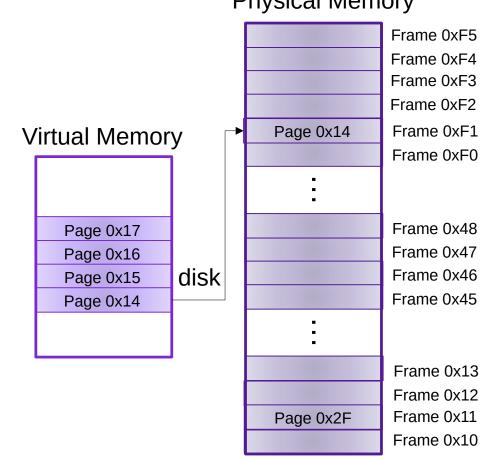
÷	V	Frame	Access
0x17	1	0x47	R,W
0x16	0	NULL	R,W
0x15	0	0x13	R,W
0x14	1	0xF1	R,X
•			



÷	V	Frame	Access
0x17	1	0x47	R,W
0x16	0	NULL	R,W
0x15	0	0x13	R,W
0x14	1	0xF1	R,X
:			

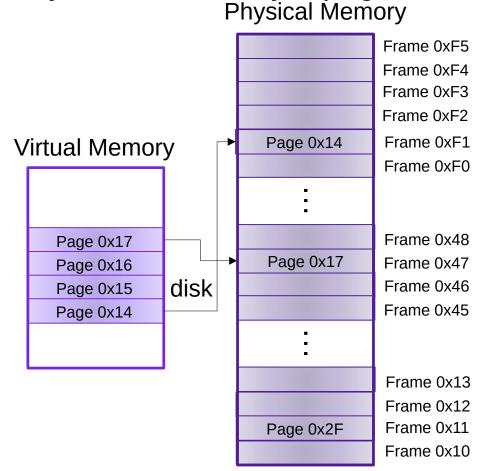


÷	v	Frame	Access
0x17	1	0x47	R,W
0x16	0	NULL	R,W
0x15	0	0x13	R,W
0x14	1	0xF1	R,X
:			

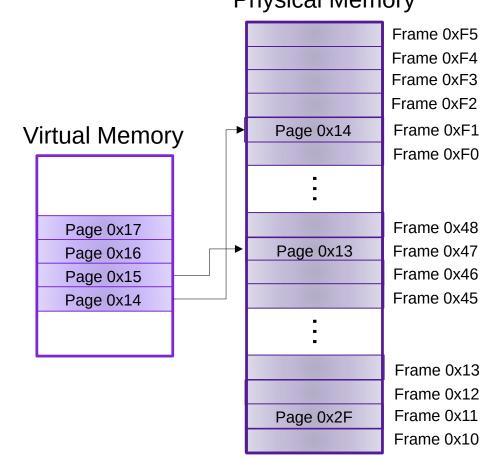


Assume that you are currently executing a process P with the following page table on a system with 16 byte pages:

: v Frame Access
 0x17 1 0x47 R,W
 0x16 0 NULL R,W
 0x15 0 0x13 R,W
 0x14 1 0xF1 R,X
 :



:	V	Frame	Access
0x17	0	0x47	R,W
0x16	0	NULL	R,W
0x15	1	0x47	R,W
0x14	1	0xF1	R,X
÷			



:	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7		0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947?
- What is the physical address that corresponds to the virtual address 0xF700?
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947?
- What is the physical address that corresponds to the virtual address 0xF700?
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47
- What is the physical address that corresponds to the virtual address 0xF700?
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47 0x2447
- What is the physical address that corresponds to the virtual address 0xF700?
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47 0x2447
- What is the physical address that corresponds to the virtual address 0xF700?  $0 \times 10^{-10}$
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47 0x2447
- What is the physical address that corresponds to the virtual address 0xF700? 0xF7 0x00 page fault
- What is the physical address that corresponds to the virtual address 0xF813?

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47 0x2447
- What is the physical address that corresponds to the virtual address 0xF700? 0xF7 0x00 page fault
- What is the physical address that corresponds to the virtual address 0xF813? 0xF8 0xF8

÷	V	Frame	Access
0xFA	1	0x47	R,W
0xF9	1	0x24	R,W
0xF8	0	NULL	R,W
0xF7	0	0x23	R,X

- What is the physical address that corresponds to the virtual address 0xF947? 0xF9 0x47 0x2447
- What is the physical address that corresponds to the virtual address 0xF700? 0xF7 0x00 page fault
- What is the physical address that corresponds to the virtual address 0xF813? 0xF8 0xF8 0xF8



- Isolation: don't want different process states collided in physical memory
- Efficiency: want fast reads/writes to memory
- Sharing: want option to overlap for communication
- Utilization: want best use of limited resource
- Virtualization: want to create illusion of more resources



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