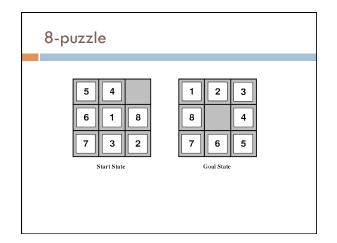
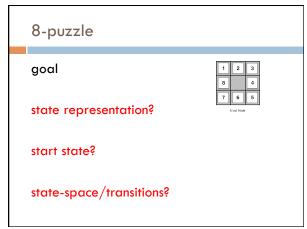


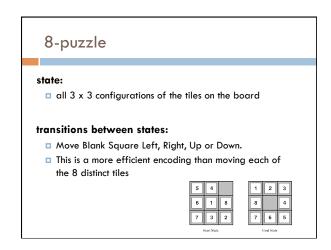
## Assignment 8... how did it go? Assignment 9 Due Sunday at 11:59 pm

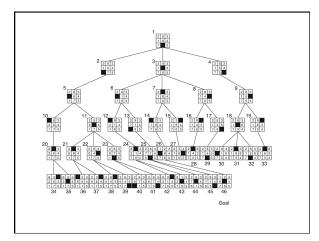
# Midterm next Tuesday (4/12) In-class Will focus on material since the second midterm up through today's class Can use 2 pages of notes (like last time) I'll post practice problems Lab Monday will be a review session

# Other search problems What problems have you seen that could be posed as search problems? What is the state? Start state Goal state State-space/transition between states









## Cryptarithmetic

Find an assignment of digits (0, ..., 9) to letters so that a given arithmetic expression is true. examples:

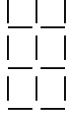
SEND + MORE = MONEY

FORTY

+ TEN + TEN

SIXTY F=2, O=9, R=7, etc. Remove 5 Sticks

Given the following configuration of sticks, remove exactly 5 sticks in such a way that the remaining configuration forms exactly 3 squares.



## Water Jug Problem

Given a full 5-gallon jug and a full 2-gallon jug, fill the 2-gallon jug with exactly one gallon of water.





## Water Jug Problem



State = (x,y), where x is the number of gallons of water in the 5-gallon jug and y is # of gallons in the 2-gallon jug

Initial State = (5,2)

Goal State = (\*,1), where \* means any amount

Operator	tabl

Name	Cond.	Transition	Effect
Empty5	-	$(x,y) \rightarrow (0,y)$	Empty 5-gal. jug
Empty2	_	$(x,y)\rightarrow(x,0)$	Empty 2-gal. jug
2to5	x ≤ 3	$(x,2) \rightarrow (x+2,0)$	Pour 2-gal. into 5-gal.
5to2	$x \ge 2$	$(x,0) \rightarrow (x-2,2)$	Pour 5-gal. into 2-gal.
5to2part	y < 2	(1,y)→(0,y+1)	Pour partial 5-gal. into 2- gal.

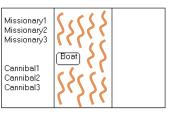
### Missionaries and Cannibals

Three missionaries and three cannibals wish to cross the river. They have a small boat that will carry up to two people. Everyone can navigate the boat. If at any time the Cannibals outnumber the Missionaries on either bank of the river, they will eat the Missionaries. Find the smallest number of crossings that will allow everyone to cross the river safely.

What is the "state" of this problem (it should capture all possible valid configurations)?

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MMMCCC B

MMCC

в мс

 $\mathsf{MC}$ 

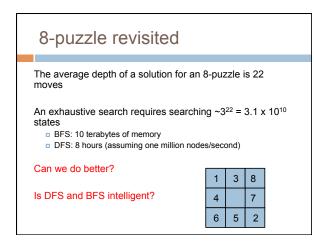
B MMCC

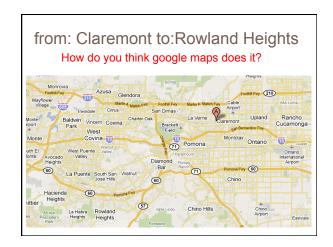
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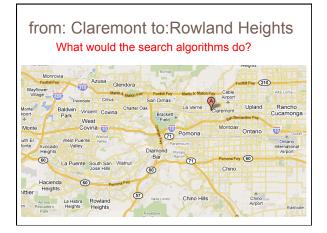
## 8-puzzle revisited

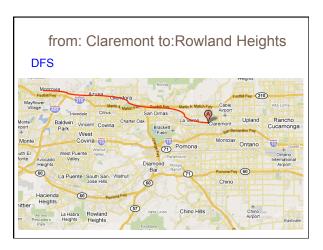
How hard is this problem?

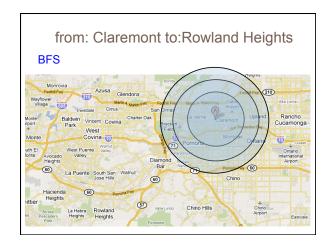


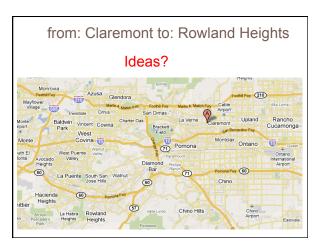


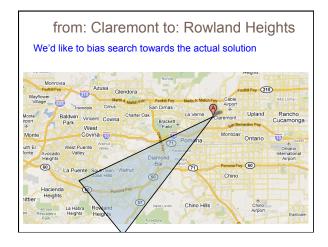












## Informed search

Order to\_visit based on some knowledge of the world that estimates how "good" a state is

□ *h*(*n*) is called an evaluation function

### **Best-first search**

- □ rank to\_visit based on h(n)
- □ take the most desirable state in to\_visit first
- □ different approaches depending on how we define *h*(*n*)

## Heuristic

### Merriam-Webster's Online Dictionary

Heuristic (pron. \hyu-'ris-tik\): adj. [from Greek heuriskein to discover.] involving or serving as an aid to learning, discovery, or problem-solving by experimental and especially trial-and-error methods

The Free On-line Dictionary of Computing (2/19/13)
heuristic 1. Of or relating to a usually speculative formulation serving as a guide in the investigation or solution of a problem: "The historian discovers the past by the judicious use of such a heuristic device as the 'ideal type'" (Karl J. Weintraub).

## Heuristic function: *h*(*n*)

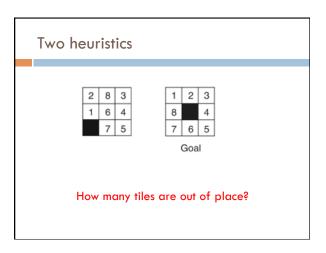
An estimate of how close the node is to a goal

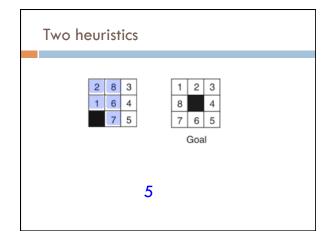
Uses domain-specific knowledge!

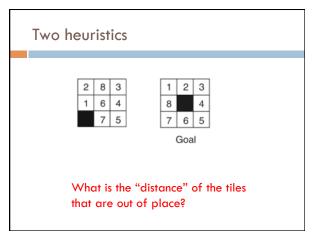
### Examples

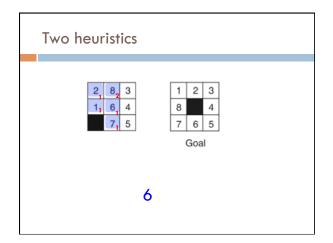
- Map path finding?
  - straight-line distance from the node to the goal ("as the crow flies")
- how many tiles are out of place
- sum of the "distances" of the out of place tiles
- Missionaries and cannibals?
  - number of people on the starting bank

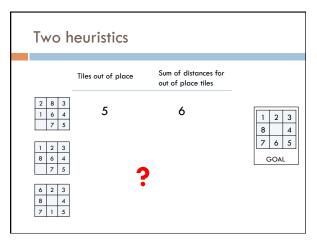
Two heuristics Which state is better? GOAL

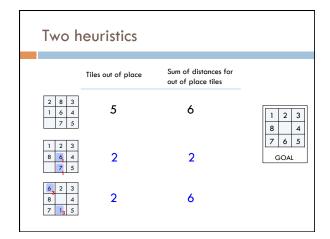


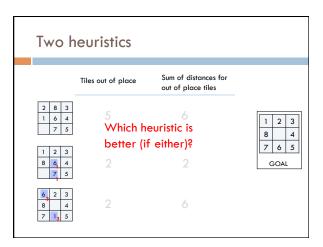


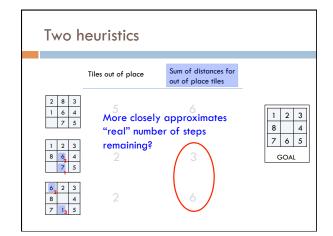


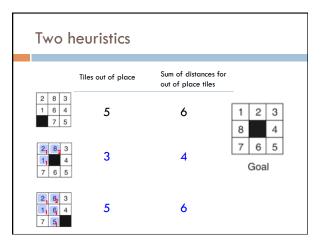


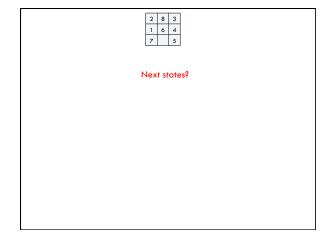


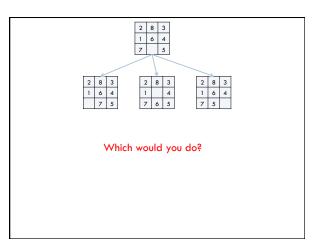


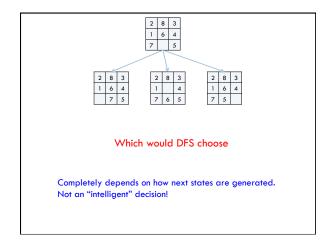


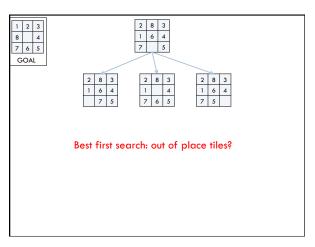


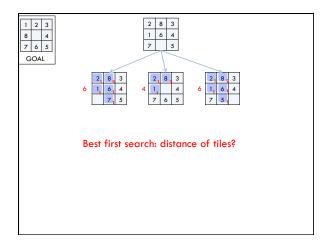


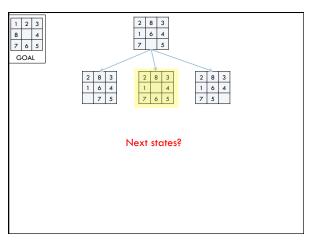


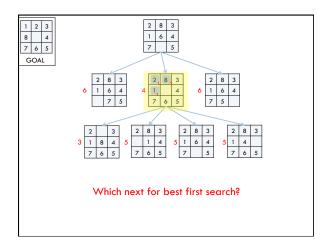


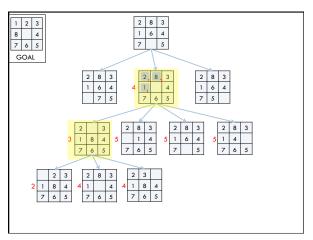


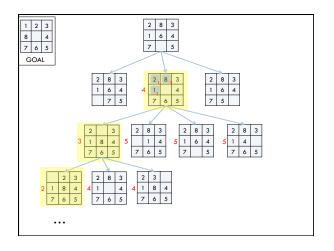












## Informed search algorithms Best first search is called an "informed" search algorithm Why wouldn't we always use an informed algorithm? Coming up with good heuristics can be hard for some problems There is computational overhead (both in calculating the heuristic and in keeping track of the next "best" state)

Informed search algorithms

Any other problems/concerns about best first search?

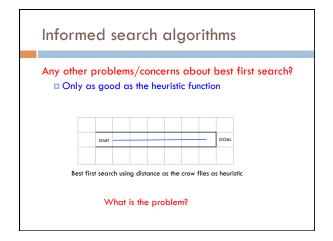
Informed search algorithms

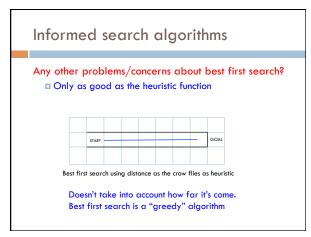
Any other problems/concerns about best first search?

Only as good as the heuristic function

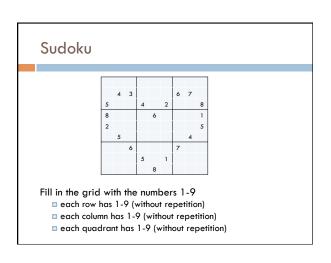
Best first search using distance as the crow flies as heuristic

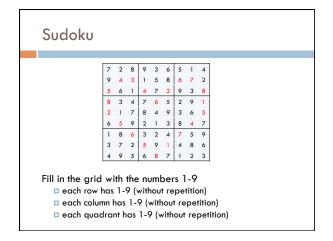
What would the search do?

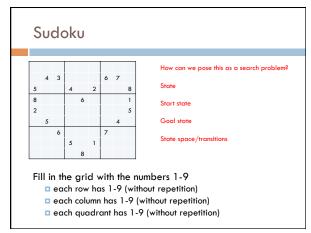


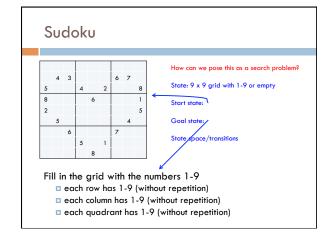


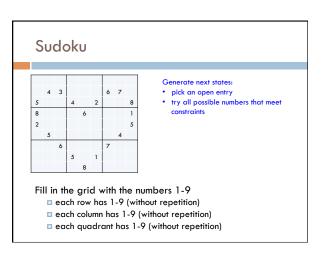
# Informed search algorithms Best first search is called an "informed" search algorithm There are many other informed search algorithms: A\* search (and variants) Theta\* Beam search

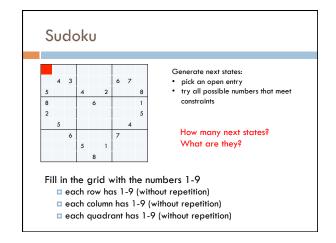


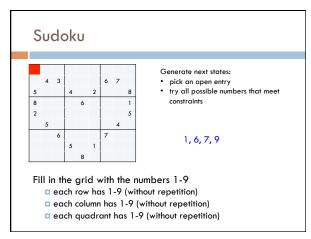


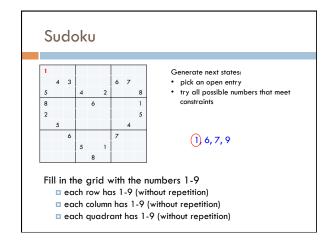


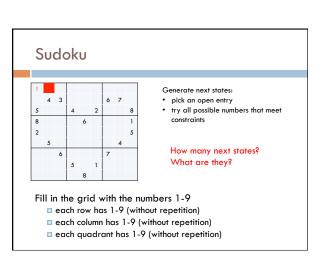


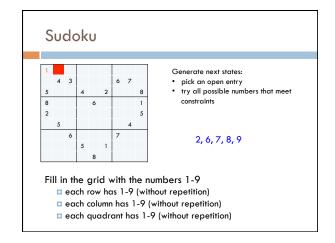


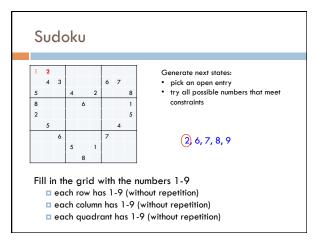


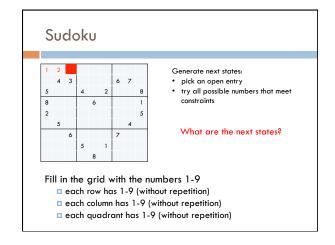


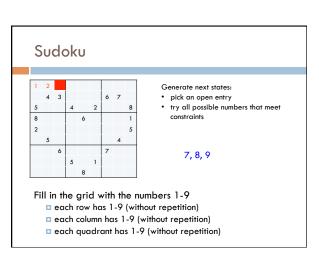




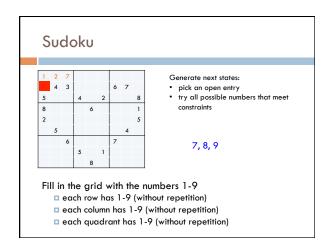


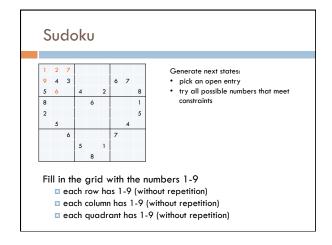


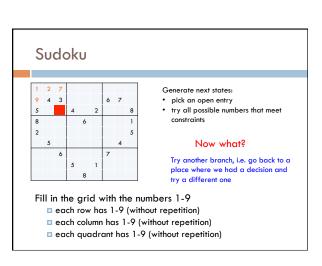


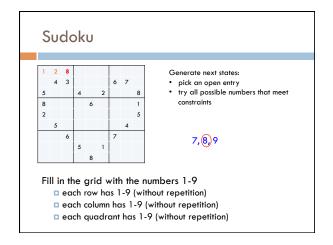


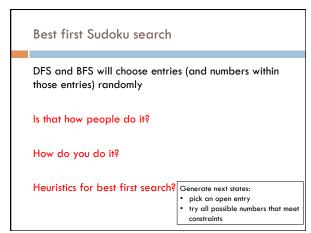
# Generate next states: • pick an open entry • try all possible numbers that meet constraints Fill in the grid with the numbers 1-9 • each row has 1-9 (without repetition) • each quadrant has 1-9 (without repetition)



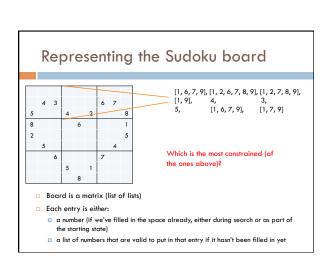








# DFS and BFS will choose entries (and numbers within those entries) randomly Pick the entry that is MOST constrained People often try and find entries where only one option exists and only fill it in that way (very little search) Generate next states: • pick an open entry • try all possible numbers that meet constraints



# Representing the Sudoku board [1, 6, 7, 9], [1, 2, 6, 7, 8, 9], [1, 2, 7, 8, 9], [1, 9], 4, 3, [1, 6, 7, 9], [1, 7, 9] Which is the most constrained (of the ones above)? Board is a matrix (list of lists) Each entry is either: a number (if we've filled in the space already, either during search or as part of the starting state) a list of numbers that are valid to put in that entry if it hasn't been filled in yet