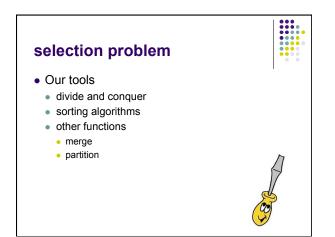


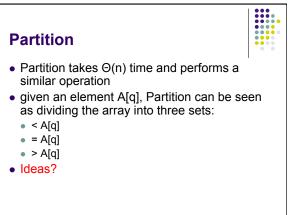


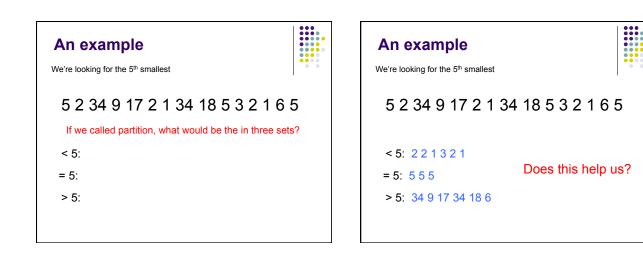
- More general problem: find the *k*-th smallest element in an array
  - i.e. element where exactly k-1 things are smaller than it
  - aka the "selection" problem
  - can use this to find the median if we want
- Can we solve this in a similar way?
  - Yes, sort the data and take the kth element
  - Θ(n log n)

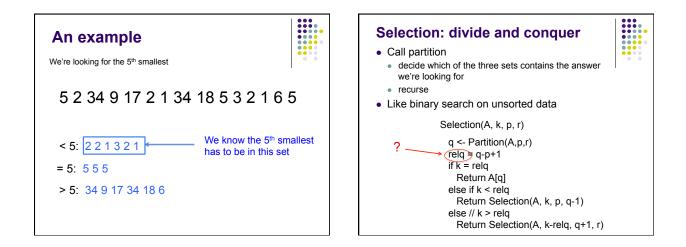


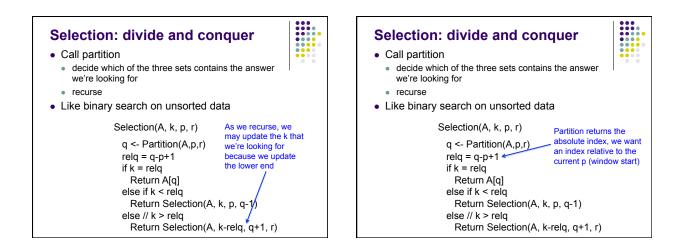
- Are we doing more work than we need to?
- To get the k-th element (or the median) by sorting, we're finding *all* the k-th elements at once
- We just want the one!
- Often when you find yourself doing more work than you need to, there is a faster way (though not always)

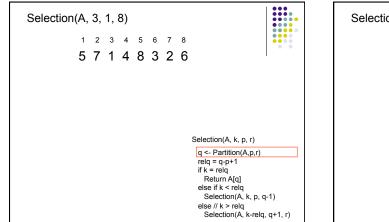




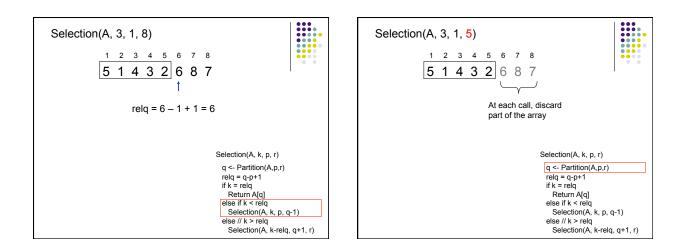


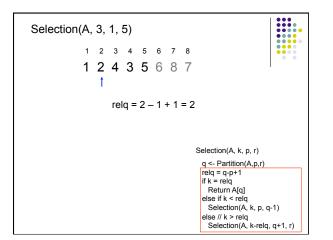


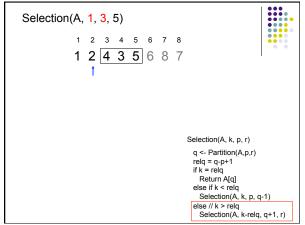


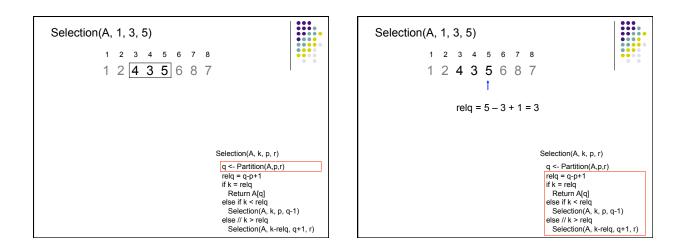


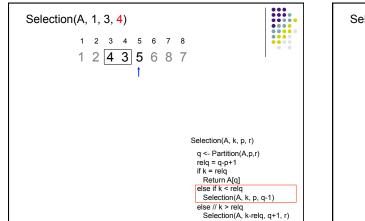
Selection(A, 3, 1, 8)									
	1	2	3	4	5	6	7	8	
	5	1	4	3	2	6 †	8	7	
relq = 6 - 1 + 1 = 6									
Selection(A, k, p, r)									
									q <- Partition(A,p,r) relq = q-p+1 if k = relq Return A[q]
									else if k < relq Selection(A, k, p, q-1) else // k > relq Selection(A, k-relq, q+1, r)

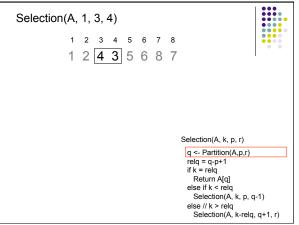


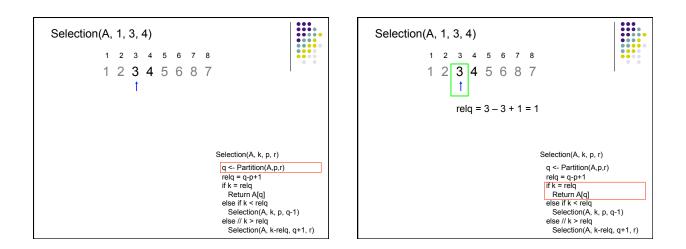


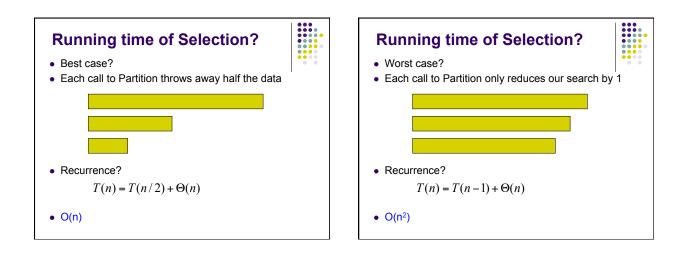


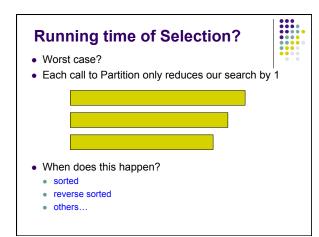












## How can randomness help us?

RSelection(A, k, p, r)

q <- RPartition(A,p,r) if k = q Return A[q] else if k < q Return Selection(A, k, p, q-1) else // k > q Return Selection(A, k, q+1, r)

## **Running time of RSelection?**

- Best case
  - O(n)
- Worst case
  - Still O(n<sup>2</sup>)
  - As with Quicksort, we can get unlucky
- Average case?

