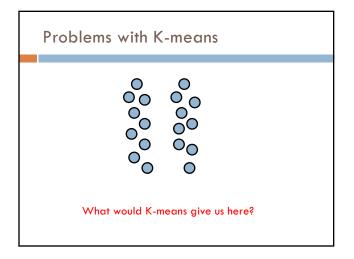
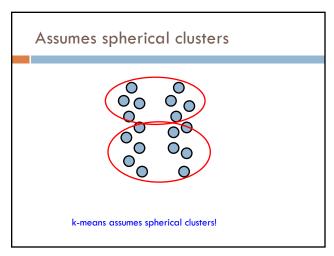
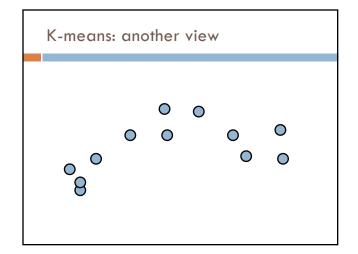


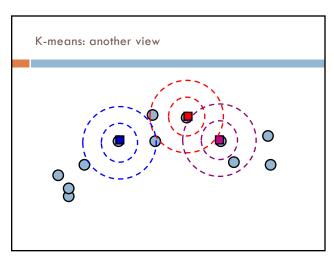
K-means Start with some initial cluster centers Iterate: Assign/cluster each example to closest center Recalculate centers as the mean of the points in a cluster

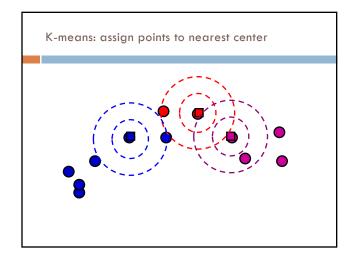
Problems with K-means Determining K is challenging Hard clustering isn't always right Assumes clusters are spherical Greedy approach

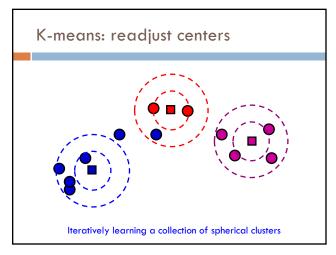


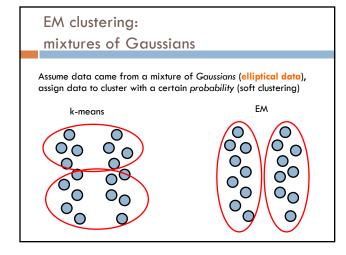












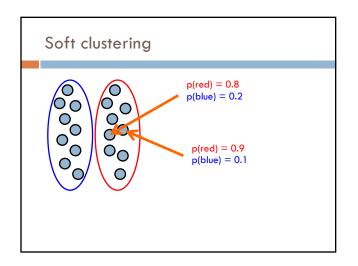
EM clustering

Very similar at a high-level to K-means

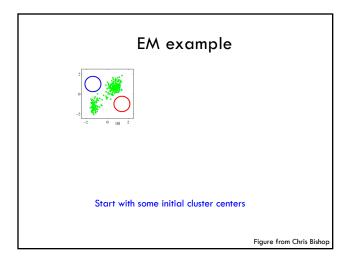
Iterate between assigning points and recalculating cluster centers

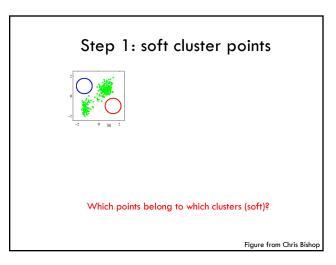
Two main differences between K-means and EM clustering:

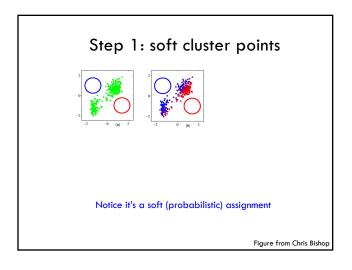
- 1. We assume elliptical clusters (instead of spherical)
- 2. It is a "soft" clustering algorithm

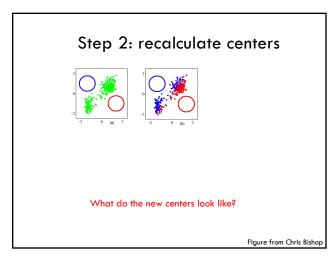


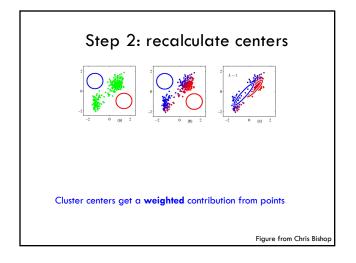
Start with some initial cluster centers Iterate: - soft assign points to each cluster Calculate: p(θ_c| x) the probability of each point belonging to each cluster - recalculate the cluster centers Calculate new cluster parameters, θ_c maximum likelihood cluster centers given the current soft clustering

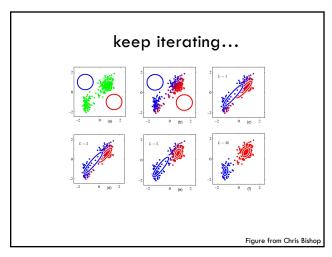






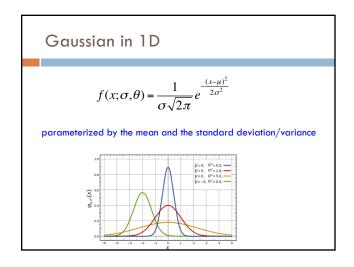


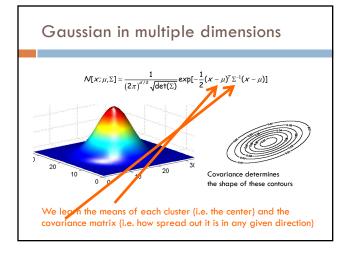


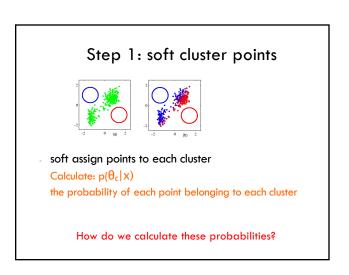


Model: mixture of Gaussians

How do you define a Gaussian (i.e. ellipse)?
In 1-D?
In m-D?







Step 1: soft cluster points





soft assign points to each cluster

Calculate: $p(\theta_c|x)$ the probability Reach point belonging to each cluster

Just plug into the Gaussian equation for each cluster! (and normalize to make a probability)

Step 2: recalculate centers







Recalculate centers:

calculate new cluster parameters, $\theta_{\rm c}$ maximum likelihood cluster centers given the current soft clustering

How do calculate the cluster centers?

Fitting a Gaussian

What is the "best"-fit Gaussian for this data?

10, 10, 10, 9, 9, 8, 11, 7, 6, ...

Recall this is the 1-D Gaussian equation:

$$f(x;\sigma,\theta) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Fitting a Gaussian

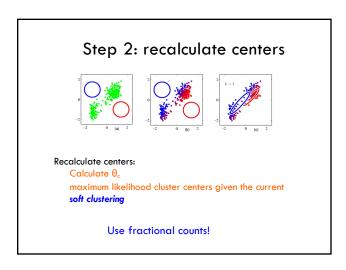
What is the "best"-fit Gaussian for this data?

10, 10, 10, 9, 9, 8, 11, 7, 6, ...

The MLE is just the mean and variance of the data!

Recall this is the 1-D Gaussian equation:

$$f(x;\sigma,\theta) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



Just like NB maximum likelihood estimation, except we use fractional counts instead of whole counts

Similar to k-means

Iterate:

Assign/cluster each point to closest center

Expectation: Given the current model, figure out the expected probabilities of the points to each cluster

Recalculate centers as the mean of the points in a cluster

Maximization: Given the probabilistic assignment of all the points, estimate a new model, θ_c

E and M steps

Expectation: Given the current model, figure out the expected probabilities of the data points to each cluster

Maximization: Given the probabilistic assignment of all the points, estimate a new model, θ_c

Iterate:

each iterations increases the likelihood of the data and is guaranteed to converge (though to a local optimum)!

EM

EM is a general purpose approach for training a model when you don't have labels

Not just for clustering!

□ K-means is just for clustering

One of the most general purpose unsupervised approaches

can be hard to get right!

EM is a general framework

Create an initial model, θ '

□ Arbitrarily, randomly, or with a small set of training examples

Use the model θ ' to obtain another model θ such that

 $\sum_{i} log \; P_{\theta}(data_{i}) > \sum_{i} log \; P_{\theta'}(data_{i}) \qquad \text{i.e. better models data} \\ \qquad \qquad \text{(increased log likelihood)}$

Let $\theta'=\theta$ and repeat the above step until reaching a local maximum

□ Guaranteed to find a better model after each iteration

Where else have you seen EM?

EM shows up all over the place

Training HMMs (Baum-Welch algorithm)

Learning probabilities for Bayesian networks

EM-clustering

Learning word alignments for language translation

Learning Twitter friend network

Genetics

Finance

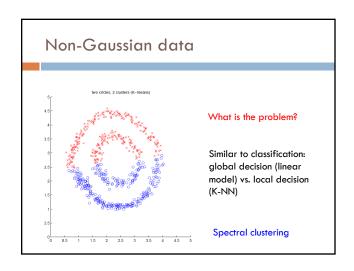
Anytime you have a model and unlabeled data!

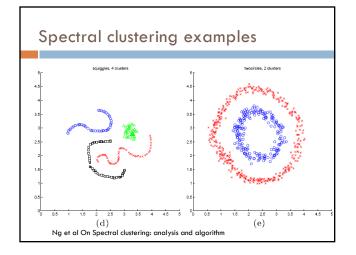
Other clustering algorithms

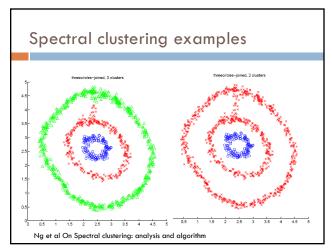
K-means and EM-clustering are by far the most popular for clustering

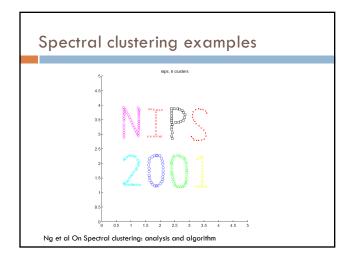
However, they can't handle all clustering tasks

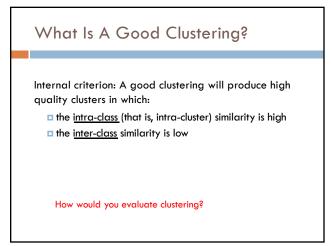
What types of clustering problems can't they handle?

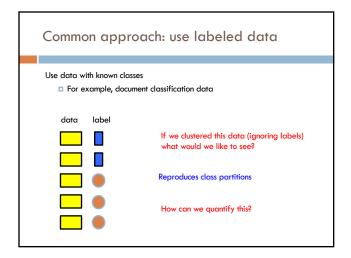


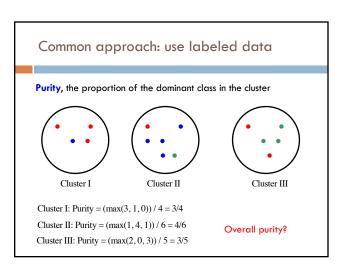












Overall purity

Cluster I: Purity = $(\max(3, 1, 0)) / 4 = 3/4$ Cluster II: Purity = $(\max(1, 4, 1)) / 6 = 4/6$ Cluster III: Purity = $(\max(2, 0, 3)) / 5 = 3/5$

Cluster average:

$$\frac{\frac{3}{4} + \frac{4}{6} + \frac{3}{5}}{3} = 0.672$$

Weighted average: $\frac{4 * \frac{3}{4} + 6 * \frac{4}{6} + 5 * \frac{3}{5}}{15} = \frac{3 + 4 + 3}{15} = 0.667$

Purity issues...

Purity, the proportion of the dominant class in the cluster

Good for comparing two algorithms, but not understanding how well a single algorithm is doing, why?

□ Increasing the number of clusters increases purity

Purity isn't perfect





Which is better based on purity?

Which do you think is better?

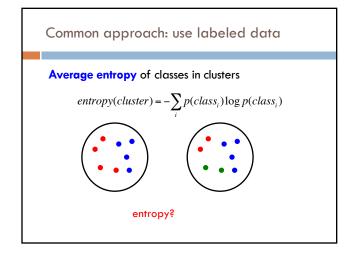
Ideas?

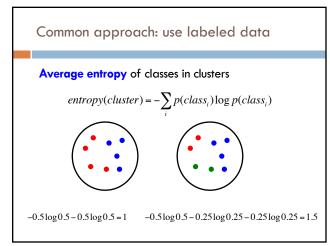
Common approach: use labeled data

Average entropy of classes in clusters

$$entropy(cluster) = -\sum_{i} p(class_{i}) \log p(class_{i})$$

where $p(class_i)$ is proportion of class i in cluster





Where we've been!

How many slides?

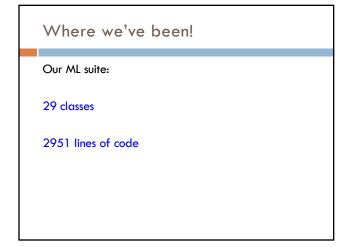
1,385 slides

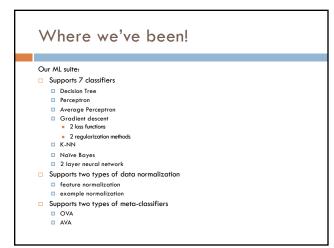
Where we've been!

Our ML suite:

How many classes?

How many lines of code?





Where we've been! Hadoop! - 532 lines of hadoop code in demos

