

Midterm

Average: 23.25

Top quartile: 26
Top half (median): 24.6
Bottom quartile: 21.4


After 5 weeks of cs52



| One last note on CS41B |
| :---: |
|  |




| Review: binary addition |
| :---: |
| 1110 <br> 01010 <br> $+\frac{01111}{11001}$ |
| Just to be sure, what are these numbers in decimal? |








What are some boolean operators?












## Ripple carry adder

To implement an n-bit adder, we chain together $n$ fulladders, each adder handles one bit position
$A=A_{3} A_{2} A_{1} A_{0}$
$B=B_{3} B_{2} B_{1} B_{0} \quad$ Adder for adding 4-bit numbers


## Signed addition

$$
\begin{array}{r}
0010 \\
+1110 \\
\hline ?
\end{array}
$$

Do the binary addition, making sure to keep track of the carries. Assume signed numbers for now.


| Signed addition |
| :---: | :---: |
| 1110  <br> 0010 2 <br> +1110 -2 <br> 0000 0 |
| Ripple carry adder will work for signed and unsigned numbers |




## $\mathrm{C}, \mathrm{N}, \mathrm{Z}$ and V bits

In addition to the sum, we often also calculate some other useful information:

- C: carry out bit of the adder
$\square$ Z: 1 if the total result is zero, 0 otherwise
$\square \mathrm{N}$ : sign bit of the result
- V: if there was "signed overflow": the result cannot be represented with the number of bits we're using


## Ripple carry adder/subtractor

$$
\text { If } D=0
$$

$\square$ Carry in for first adder $=0$
$\square B_{i}$ XOR $0=B_{i}$

If $D=1$

- Carry in for first adder $=1$ (+1 to sum)
$\square B_{i}$ XOR $1=$ NOT $B_{i}$ (flip all the bits of $B$ )

$V$ bit
$V$ : if there was "signed overflow": the result cannot be represented with the number of bits we're using
- Adding two positive numbers (too big positive)
- Subtracting a negative number from a positive number (too big positive)
- Adding two negative numbers (too big negative)
- Subtracting a positive number from a negative number (too big negative)

What are the cases where signed overflow can occur?


| Detecting overflow |
| :---: |
| 111 |
| 0011 |
| $+\frac{0101}{1000}$ |
| Yes. How do we detect it? |
|  |


| Detecting overflow |
| :--- |
| $\qquad$111 <br> 0011 <br> +0101 |
| - Added two positive numbers and got a negative <br> - In general: if the sign bits are the same (of the numbers <br> we end up adding), but the higher order bit of result is <br> different = overflow |


| Detecting overflow |
| :---: |
| 0011 <br> -1001 |
| Subtract these (as signed numbers). <br> Does overflow occur? |



| Detecting overflow |
| :--- |
| 000 |
|  |
|  |
| - Subtracted a negative number from a positive, should |
| have been positive |
| - In general: if the sign bits are the different (of the |
| numbers we end up subtracting), but the higher order |
| bit of result is different = overflow |


| Detecting overflow |
| :--- |
| $\qquad$10011 <br> 0110 <br> - Subtracted a negative number from a positive <br> - In general: if the sign bits are the same (of the numbers <br> we end up adding), but the higher order bit of result is <br> different = overflow |



